# Unit 7

**Rational Explorations**

**Numbers & their Opposites**

- Number Lines
- Real World Representations
- Absolute Value
- Order Rational Numbers
- Graph on Coordinate Plane
- Distance on Coordinate Plane
- Reflect on Coordinate Plane
- Draw Polygons on Coordinate Plane

---

**Name:** ____________________________

**Math Teacher:** ________________________

---

### Unit 7 IXL Tracking Log

<table>
<thead>
<tr>
<th>Required Skills</th>
<th>Skill</th>
<th>Your Score</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Week of 1/27</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.1 (Understanding Integers)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.2 (Integers on Number Lines)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.3 (Absolute Value and Opposites)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.New! (Understanding Opposite Integers)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.4 (Graph Integers on Horizontal &amp; Vertical Number Lines)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.5 (Comparing Integers)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.6 (Ordering Integers)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.7 (Put Integers in Order)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.8 (Integer Inequalities with Absolute Values)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>M.9 (Absolute Value and Integers: Word Problems)</td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Week of 2/3</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>P.New! (Rational Numbers on Number Lines)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P.1 (Rational Numbers: Equal or Not Equal)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P.2 (Compare Rational Numbers)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>P.3 (Put Rational Numbers in Order)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.1 (Objects on Coordinate Planes)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.2 (Graph Points on a Coordinate Plane)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.3 (Quadrants)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.4 (Coordinate Planes as Maps)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.5 (Distance Between Two Points)</td>
<td></td>
<td></td>
</tr>
<tr>
<td>X.6 (Follow Directions on a Coordinate Plane)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Georgia Standards of Excellence (GSE):

MGSE.6.NS.5: Understand that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, debits/credits); use positive and negative numbers to represent quantities in real-world contexts, explaining the meaning of 0 in each situation.

MGSE.6.NS.6: Understand a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to represent points on the line and in the plane with negative number coordinates.

MGSE.6.NS.6a: Recognize opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; recognize that the opposite of the opposite of a number is the number itself, e.g., -(-3) = 3, and that 0 is its own opposite.

MGSE.6.NS.6b: Understand signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; recognize that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.

MGSE.6.NS.6c: Find and position integers and other rational numbers on a horizontal or vertical number line diagram; find and position pairs of integers and other rational numbers on a coordinate plane.

MGSE.6.NS.7: Understand ordering and absolute value of rational numbers.

MGSE.6.NS.7a: Interpret statements of inequality as statements about the relative position of two numbers on a number line diagram.

MGSE.6.NS.7b: Write, interpret, and explain statements of order for rational numbers in real-world contexts.

MGSE.6.NS.7c: Understand the absolute value of a rational number as its distance from 0 on the number line; interpret absolute value as magnitude for a positive or negative quantity in a real-world situation.

MGSE.6.NS.7d: Distinguish comparisons of absolute value from statements about order.

MGSE.6.NS.8: Solve real-world and mathematical problems by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.

MGSE.6.G.3: Draw polygons in the coordinate plane given coordinates for the vertices; use coordinates to find the length of a side joining points with the same first coordinate or the same second coordinate. Apply these techniques in the context of solving real-world and mathematical problems.

What Will I Need to Learn??

- How to describe real-world situations using positive and negative numbers
- To represent numbers as locations on number lines
- To understand opposites (inverses) on a number line
- To graph ordered pairs (including negatives) on a coordinate plane
- To understand that opposites in ordered pairs indicate a reflection on a coordinate plane
- Interpret inequalities, comparing two numbers on a number line
- Order rational numbers
- Understand absolute value (distance from zero)
- Compare and order absolute value
- Determine the distance between points on a coordinate plane
- Draw polygons in the coordinate plane, given the coordinates for the vertices

Math 6/7

Unit 7 Calendar

<table>
<thead>
<tr>
<th>1/27</th>
<th>1/28</th>
<th>1/29</th>
<th>1/30</th>
<th>1/31</th>
</tr>
</thead>
<tbody>
<tr>
<td>Unit 7 Pre-Test; MSG; Unit 6 Project Gallery Walk</td>
<td>Intro to Integers; Graphing on a Number Line</td>
<td>Comparing and Ordering</td>
<td>Absolute Value; Short Quiz</td>
<td>Graphing on a Coordinate Plane</td>
</tr>
<tr>
<td>2/3</td>
<td>2/4</td>
<td>2/5</td>
<td>2/6</td>
<td>2/7</td>
</tr>
<tr>
<td>Distance Between Points; Drawing Polygons; Reflections</td>
<td>Mercedes Benz Field Trip</td>
<td>Computer Lab</td>
<td>Mini Post-Test; Review</td>
<td>Unit 7 Test</td>
</tr>
</tbody>
</table>
# Unit 7 Vocabulary

<table>
<thead>
<tr>
<th>Vocabulary Term</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>absolute value</td>
<td>The distance between a number and zero on a number line.</td>
</tr>
<tr>
<td>coordinate plane</td>
<td>A plane, also called a coordinate grid or coordinate system, in which a horizontal number line and a vertical number line intersect at their zero points. (0,0)</td>
</tr>
<tr>
<td>Inequality</td>
<td>A statement that compares two quantities using the symbols $&gt;$, $&lt;$, $\geq$, or $\leq$.</td>
</tr>
<tr>
<td>integer</td>
<td>Any number from the set {... -4, -3, -2, -1, 0, 1, 2, 3, 4 ...} where ... means continues without end.</td>
</tr>
<tr>
<td>negative integer</td>
<td>A number that is less than zero.</td>
</tr>
<tr>
<td>Opposites</td>
<td>Two integers are opposites if they are represented on the number line by points that are the same distance from zero, but on opposite sides of zero. The sum of two opposites is zero.</td>
</tr>
<tr>
<td>ordered pair</td>
<td>A pair of numbers used to locate a point in the coordinate plane. An ordered pair is written in the form (x-coordinate, y-coordinate).</td>
</tr>
<tr>
<td>Origin</td>
<td>The point (0, 0) in a coordinate plane where the x-axis and the y-axis intersect.</td>
</tr>
<tr>
<td>positive integer</td>
<td>A number that is greater than zero. It can be written with or without a + sign.</td>
</tr>
<tr>
<td>Quadrants</td>
<td>The four regions in a coordinate plane separated by the x-axis and y-axis.</td>
</tr>
<tr>
<td>Reflection</td>
<td>A transformation in which a figure or ordered pair is flipped over a line of symmetry.</td>
</tr>
<tr>
<td>Sign</td>
<td>A symbol that indicates whether a number is positive or negative.</td>
</tr>
<tr>
<td>x-coordinate</td>
<td>The first number in an ordered pair. (It tells you how far left or right to go from the origin.)</td>
</tr>
<tr>
<td>y-coordinate</td>
<td>The second number in an ordered pair. (It tells you how far up or down to go from the origin.)</td>
</tr>
</tbody>
</table>

# Unit 7 Vocabulary – You Try

<table>
<thead>
<tr>
<th>Vocabulary Term</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>absolute value</td>
<td></td>
</tr>
<tr>
<td>coordinate plane</td>
<td></td>
</tr>
<tr>
<td>Inequality</td>
<td></td>
</tr>
<tr>
<td>integer</td>
<td></td>
</tr>
<tr>
<td>negative integer</td>
<td></td>
</tr>
<tr>
<td>opposites</td>
<td></td>
</tr>
<tr>
<td>ordered pair</td>
<td></td>
</tr>
<tr>
<td>origin</td>
<td></td>
</tr>
<tr>
<td>positive integer</td>
<td></td>
</tr>
<tr>
<td>quadrants</td>
<td></td>
</tr>
<tr>
<td>reflection</td>
<td></td>
</tr>
<tr>
<td>sign</td>
<td></td>
</tr>
<tr>
<td>x-coordinate</td>
<td></td>
</tr>
<tr>
<td>y-coordinate</td>
<td></td>
</tr>
</tbody>
</table>
Unit 7 Study Guide

Knowledge and Understanding
1) What does the absolute value of a number tell you about the number? ____________________________

2) Describe how to use a number line to order integers. _______

Proficiency of Skills
3) Evaluate \(|-15| = \) __________

4) Evaluate \(|2| = \) __________

5) Order from least to greatest: \(-10, 0, |-12|, -12, |-9|\)

   ____, ____, ____, ____, ____, ______

6) Plot and label the following points on the coordinate plane
   A (-3, 2)     B (0, -3)     C (-2, -10)     D (8, -5)

   ![Diagram of coordinate plane]

7) Finish labeling the number line below. Plot a point on 4 and its opposite.

   ![Number line diagram]

Application
8) Kellen has reached the peak of Mathclassrocks Mountain at 1,000 feet above sea level. He hikes down 400 feet to check out an old cannon. How many more feet must he hike to reach sea level? (Hint: Drawing a picture may help to visualize the problem!!)

  _______ _______ _______ _______

9) The table below shows today’s temperature for 5 cities in Alaska.

<table>
<thead>
<tr>
<th>City</th>
<th>McKinley Park</th>
<th>Bethel</th>
<th>Fairbanks</th>
<th>King Salmon</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature</td>
<td>-22</td>
<td>-11</td>
<td>-20</td>
<td>-13</td>
</tr>
<tr>
<td>(°Celsius)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

   a) Write an inequality statement comparing the temperature of King Salmon and Bethel: _________________________

   b) Order the cities from warmest to coldest: _____________

   ________________________________________________
10) Graph point A (4, -8) on the coordinate plane.

a) Reflect the point across the x-axis.
b) What is the distance between point A and the reflected point? _____ units
   Justify your answer: ____________________________
   ____________________________

11) Andrew owes $6.50 in late fees to the library. Represent this value on the number line below. Mark the point A (Hint: If he OWES, is that a positive or negative number?)

a) Hayleigh owes $0.50 in late fees to the library. Plot a point for this value on the number line. Mark the point H.
b) How much more does Andrew owe than Hayleigh? _____

Use the map below for questions 12 – 14.

12) Name the ordered pair that represents the location of the gas station.

13) How many blocks apart are the hospital and the cemetery? ________ blocks

14) Name the building that is located in quadrant 3. ______

15) Graph (7, -3) and (7, 5) on the coordinate plane to the right.

a) Reflect both points across the y-axis to form the vertices of a rectangle.
b) Name the two reflected ordered pairs: _____ & _____
c) What is the perimeter of the rectangle? ________
d) What is the area of the rectangle? ________
16) If you reflected the ordered pair (-2, 5) across the x-axis, what would be the coordinates of the reflection?
   a) (-2, -5)  b) (2, 5)  c) (2, -5)  d) (-2, 5)

17) Which statement below is NOT true?
   a) -3 < -1
   b) -2 ≥ -5
   c) -4 ≤ -14
   d) -3 < 4

18) It is 89 degrees above zero in Miami. It is 20 degrees below zero in Anchorage. Use the number line below to determine how many degrees warmer it is in Miami than in Anchorage.

   a) 69°F  b) 79°F  c) 109°F  d) 129°F

19) A Bolivian monkey is jumping around on a number line. He starts at -3 and jumps 8 units to the right. Where is he now on the number line?

   a) -5  b) -11  c) -11  d) 5

Performance Task
20) A newly developed neighborhood has dedicated a portion of their land to be used as a children’s playground. The neighborhood would like to build a fence around a rectangular area of 100 square yards for a dog run. The coordinate planes below each represent the dedicated land. Each square on the grid represents one square yard. Each yard of fencing costs $12. Develop two plans for the neighborhood to choose from.

   Label the coordinates of the vertices and determine the price of the fencing for each plan (based on the perimeter). Then write a letter to the neighborhood explaining which design you recommend and why.
Using Integers to Represent Real-World Situations

Integers are whole numbers and their opposites. A number line shows both positive and negative integers.

-5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5

negative integers neither negative nor positive positive integers

You can use an integer to represent a situation. Positive integers show an increase or gain, or a location above or to the right. Negative integers show a decrease or loss, or a location below or to the left.

Represent each situation with an integer.

1. Kevin lost 8 pounds.
2. An elevator rose 6 floors.
3. A plant grew 5 cm.
4. A football team lost 9 yards.
5. The temperature dropped 2 degrees.
6. A location is 3 miles above sea level.
7. Max deposited $14 in his account.
8. Dinner cost Marcia $9.
9. Six students transferred out of the school.
10. There are fourteen hours before the start of a game.
11. Eleven people boarded a bus.
12. Beth saved $27.
13. A diver swims 12 feet below the water’s surface.
14. The top of a building is 32 feet above the sidewalk.
15. The bottom of a mine shaft is 18 feet below the ground.
16. A gain in altitude of 500 feet
17. Randy withdrew $35 from his account.
18. The low temperature for the day was 23 degrees below zero.

Example:
Write an integer for each situation.

a) A 10-yard loss in football can be represented as -10.
b) Earning $20 can be represented as -20.
c) Spending $6 can be represented as -6.
d) 16 feet under the ground can be represented as -16.

Key Words:

<table>
<thead>
<tr>
<th>Positive</th>
<th>Negative</th>
</tr>
</thead>
</table>

Integers & Graphing on a Number Line

______________ are whole numbers and their opposites.
______________ numbers are greater than zero.
______________ numbers are less than zero.

Opposites are numbers that are same distance from zero in opposite directions.

negative integers Zero is neither negative nor positive. positive integers

©2001 Discovery Education, All Rights Reserved.
Opposites

Positive numbers, such as 2, are graphed to the _______ of zero on a number line. Negative numbers, such as -2, are graphed to the _______ of zero on a number line.

Opposites are numbers that are the same ____________ from zero in opposite directions. Since 0 is not negative or positive, it is its own opposite.

Example:
Find the opposite of the given number.

1) The opposite of -12 is: 12 2) The opposite of 8 is: -8

You Try:
Find the opposite of the given number.

1) The opposite of -5 is: 2) The opposite of 0 is:

3) The opposite of 100 is: 4) The opposite of -34 is:

5) The opposite of -13 is: 6) The opposite of 7 is:

7) The opposite of -1000 is: 8) The opposite of 50 is:

9) The opposite of the opposite of -48 is:
**Absolute Value**

**WORDS** The absolute value of a number is the __________ between the number and zero on a number line.

**MODEL**

\[ \begin{align*}
-6 & -5 - 4 - 3 - 2 - 1 & 0 & 1 & 2 & 3 & 4 & 5 & 6 \\
\hline
\end{align*} \]

5 units 5 units

**SYMBOLS**

\[ |5| = 5 \] The absolute value of 5 is 5.

\[ |-5| = 5 \] The absolute value of -5 is 5.

___________ ____________ is always ____________!

Absolute value is a distance and distance is always positive.

**Example:**

\[ |125| = 125 \]

\[ |-5| + |25| = 5 + 25 = 30 \]

\[ |-8| - |-5| = 8 - 5 = 3 \]

\[ -|-16| = -16 \]

**You Try:**

**Find the absolute value for each of the problems below.**

1) \(|25|\) 2) \(|-150|\) 3) \(|-379|\)

4) \(|-2486|\) 5) \(|1273|\) 6) \(|-68|\)

7) \(|-5| + |16|\) 8) \(|-30| - |-12|\) 9) \(|-7| + |13| + |49|\)

10) Graph \(|-6|\) on the number line below and show that it is a distance from zero.

------

**Absolute Value Practice**

Find the **opposite** of each integer.

1. 10 2. -25 3. 82

Find the **opposite of the opposite** of each integer.

4. -4 5. -15 6. 8

Evaluate each expression.

7. \(|31| + |-5|\) 8. \(|-16| - |4|\)

9. \(|-28| - |-1|\) 10. \(|11-2|\)

11. \(|44| + |-34|\) 12. \(|-101| - |-1|\)

13. **STOCKS** The net change for a certain stock is the dollar value change in the stock’s closing price from the previous day’s closing price. The net changes of three stocks were -3, 1, and -2. Which net change has the greatest absolute value?

14. **POPULATION** The population change from one year to the next of a town is -435. What is the absolute value of this population change?
Above and Below Sea Level

In the space to the right, draw the following and then answer the questions below to discover the shipwreck’s treasure.

A wavy line for sea level, a bird at +10 meters, a diver at +20 meters, an airplane taking off at +70 meters, a fish at -20 meters, a whale at -50 meters, a shipwreck at -90 meters, an underwater diver at -30 meters, a boat at sea level, and a submarine at -70 meters. Also draw a cliff with a height of +80 meters.

What is the treasure in the shipwreck? To find the treasure, draw the items on the next page and then answer the questions below and write the letters in the spaces that represent the correct answers.

1) How many meters from the top of the cliff to the shipwreck? _______ (O)
2) How many meters from the whale to the submarine? _______ (S)
3) How many meters from the airplane to the boat? _______ (A)
4) How many meters from the fish to the whale? _______ (E)
5) Which is farther from the submarine, the fish or the whale? How far is it from the submarine? _______ (I)
6) Which is closer to the shipwreck, the fish or the underwater diver? How far is it from the shipwreck? _______ (L)
7) The whale swims to sea level and then swims to the shipwreck. How far does he swim in all? _______ (R)
8) The submarine rises to sea level and then dives to the bottom of the sea. How far does the submarine travel in all? _______ (P)
9) The boat springs a leak and sinks to the bottom of the sea. How many meters did it sink? _______ (M)
10) The underwater diver wants to reach the submarine, how much farther does he need to swim? _______ (N)
11) The diver makes 3 trips from the boat (before it sinks) to the shipwreck. How many meters will he travel? _______ (D)
Comparing Integers & Absolute Values

To __________ integers, you can compare signs as well as the magnitude, or size, of the numbers. Greater numbers are graphed farther to the __________.

If two numbers are different signs, the __________ number is always greater than the negative number.

If two numbers are the same sign, use a __________ line to determine which number is greater.

Don’t forget, alligators always eat the bigger number.

3 __________ -2

You Try:

1) |8| __________ |-6|
2) |-6| __________ |6|
3) -122 __________ 300
4) |-4| __________ 4
5) |-12| __________ 9
6) |-21| __________ 0
7) 1 __________ |-1|
8) -2 __________ -4
9) |4| __________ -4
10) 20 __________ 0

Ordering Integers & Absolute Values

You can use a number line to order a set of integers. __________ can be ordered from least to greatest or from greatest to least.

Example:

Order the set {-9, 6, -3, 0} from least to greatest.

Method 1: Use a number line.

Graph the numbers on a number line.

The order from left to right is -9, -3, 0, and 6.

Method 2: Compare signs and values.

Compare negative numbers. Then compare positive numbers.

The negative integers are -9 and -3. -9 < -3
The integer 0 is neither positive nor negative.
The positive integer is 6.

So, the order from least to greatest is -9, -3, 0, and 6.

Before you put absolute values in order, find their value.

Example:

Put the following numbers in order from LEAST to GREATEST:

|6|, |-12|, |-2|, |1|

|6| = 6  |12| = 12  |-2| = 2  |1| = 1

From least to greatest: |1|, |-2|, |6|, |-12|
You Try: Order from least to greatest.
1) 0, 3, -21, 9, -89, 8, -65, -56
2) 70, -9, 67, -78, 0, 45, -36, -19
3) 0, -1, |-2|, |3|
4) -24, |-20|, 21, -26
5) |1|, -1, |-2|, -2
6) 12, 8, -9, -12, 10, 16

Extra Practice

For #’s 1-4, write an integer for each situation:
1) 45 feet below sea level
2) a gain of 8 yards
3) a deposit of $528
4) 10 pound loss
5) Graph the set {-4, 3, 0, -3, 7, -5} on the number line.

6) The opposite of -57 is:
7) The opposite of -43 is:
8) The opposite of 1000 is:
9) The opposite of 325 is:

Find the absolute value for each of the problems below.
10) |4|
11) |-41|
12) -|11|
13) |-125|
14) |526|
15) -|-3|

Use the symbols <, >, = to compare the following numbers.
16) |66| _____ |33|
17) |-24| _____ |82|
18) 88 _____ -99
19) |-37| _____ 37

Put the numbers in order from least to greatest.
20) -89, 42, -26, 8
21) -91, -46, 52, 12, 0
The Coordinate Plane is a grid consisting of two perpendicular number lines, the (horizontal) \( \text{x-axis} \) and (vertical) \( \text{y-axis} \).
- The axes intersect at point \((0,0)\), also known as the "origin".
- The four open areas are called "quadrants".
- Points can be plotted on the plane using a pair of \( x \)- and \( y \)-coordinates called "ordered pairs".

Points and Ordered Pairs

Use the coordinate grid above to find the coordinates for each point and tell what quadrant they are in.

**Example:**
A: \((5, 6)\) Quadrant I

**You Try:**
B: \(( , )\) Quadrant ___  C: \(( , )\) Quadrant ___
D: \(( , )\) Quadrant ___  E: \(( , )\) Quadrant ___
F: \(( , )\) Quadrant ___

Plotting Points

ALL ordered pairs are written as \((x,y)\).
The 1\text{st} number tells how far to go \text{ACROSS} on the \text{X-axis}
The 2\text{nd} number tells how far to go \text{UP OR DOWN} the \text{Y-axis}.

Remember you have to walk \text{IN} a building before you can go \text{UP} or \text{DOWN} the elevator!
Use the coordinate plane below to graph the following points. Label each point with its letter.

**Example:**

M \((-5, 4)\)

**You Try:**

C \((0,0)\)  H \((4,3)\)  O \((-2,-1)\)  R \((-4,0)\)

A \((-2,3)\)  K \((3,-1)\)  T \((0,4)\)  S \((4,-3)\)

---

**Reflections on the Coordinate Plane**

A ____________ is a “mirror image” of an object that has been “flipped” over an axis. You can use what you know about number lines and opposites to compare locations on the coordinate plane. Consider the number line and coordinate plane below.

The number line shows that \(-4\) and \(4\) are opposites.

The coordinate plane shows that the points \((-4, 0)\) and \((4, 0)\) are the same distance from the \(y\)-axis in opposite directions. So, they are reflected across the \(y\)-axis. Notice that the \(y\)-coordinates did not change and that the \(x\)-coordinates are opposites.

**Example:**

**Name the ordered pair that is a reflection of \((-3, 2)\) across the \(x\)-axis.**

To reflect across the \(x\)-axis, keep the same \(x\)-coordinate, \(-3\), and take the opposite of the \(y\)-coordinate. The opposite of \(+2\) is \(-2\).

So, \((-3, 2)\) reflected across the \(x\)-axis is located at \((-3, -2)\).
You Try:

Find the ordered pair that is a reflection over the x-axis and then the y-axis of each of the points below.

<table>
<thead>
<tr>
<th>Original Point</th>
<th>Reflected over x-axis</th>
<th>Reflected over y-axis</th>
</tr>
</thead>
<tbody>
<tr>
<td>(-2,5)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(-3,-1)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(1,-4)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
</tbody>
</table>

Original Point | Reflected over x-axis | Reflected over y-axis |
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>(-2,2)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(4,5)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(3,-3)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
</tbody>
</table>
**You Try:**

Find the ordered pair that is a reflection over the x-axis and then the y-axis of each of the points below.

<table>
<thead>
<tr>
<th>Original Point</th>
<th>Reflected over x-axis</th>
<th>Reflected over y-axis</th>
</tr>
</thead>
<tbody>
<tr>
<td>(-2,5)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(-3,-1)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
<tr>
<td>(1,-4)</td>
<td>( , )</td>
<td>( , )</td>
</tr>
</tbody>
</table>
**Distance on a Coordinate Plane**

When two ordered pairs have the same x-coordinate or y-coordinate, they are on the same line. The distance between these two points can be found by **counting the spaces** between the points.

Point A = (-3,3)  
Point B = (2,3)  
Point C = (-3,4)

Points A and B have the same second coordinate. The distance between them is 5 units.

Points A and C have the same first coordinate. The distance between them is 7 units.

You can also use **absolute value** to determine the distance between points!

- Notice Point A = (-3,3) and Point B = (2,3). They have the same y-coordinate, _____.
- That means you’re finding the distance between the x-coordinates, ____ and _____.
- -3 is 3 units from the y-axis, or \(|-3| = ____
- 2 is 2 units from the y-axis, or \(|2| = ____
- \(|-3| + |2| = ____ units

**Examples:**

1) On the coordinate plane below, (2,9) and (2,3) have the same x-coordinate. The distance between them is 6 units. You can figure this out by:

2) Area of a triangle = \(\frac{1}{2} (b \cdot h)\). In the figure below, the base is the distance from A to C and which is ________.

The height is the distance from B to C which is ________.

What is the area of the triangle? ________
You Try:
Use the graph below to answer the questions in Part 1:

PART 1
1) Write the ordered pair next to each point on the graph.

2) Determine the length of each side of the rectangle.
   If you have room, you may also label them on the graph.
   \[ \overline{AB} = \quad \overline{BC} = \]
   \[ \overline{CD} = \quad \overline{DA} = \]

3) What is the perimeter of rectangle ABCD? __________
4) What is the area of rectangle ABCD? ____________
5) Determine the length of the triangle’s base and height:
   \[ \overline{PQ} = \quad \overline{QR} = \]

6) What is the area of \( \triangle PQR \)? ____________

PART 2

Bugs Bunny’s home is located at point B (-5, 4). Yosemite Sam’s home is located at point Y (6, 4). Sylvester’s home is located at point S (6, -2). Daffy Duck’s home is located at point D (-5, -2).

7) Plot each character’s home on the graph above. Label them B, Y, S and D. Connect their homes in the same order they are listed (then connect B & D).

8) What polygon was formed?

9) Find the distance from each house (length of sides):
   \[ \overline{BY} = \quad \overline{YS} = \]
   \[ \overline{SD} = \quad \overline{DB} = \]

10) If they march in a parade that begins at Bugs’ house, goes around the rectangle and ends at Bugs’ house, how many units did they travel?
Area and Perimeter of Polygons

When two ordered pairs have the same x-coordinate or y-coordinate, they are on the same line. The ______ between these two points can be found by counting the spaces between the points.

Example:
A rectangle has vertices A(1,1), B(1,3), C(5,3), and D(5,1). Find the length of the sides of the rectangle.

\[
\overline{AB} = 2 \quad \overline{BC} = 4 \quad \overline{CD} = 2 \quad \overline{DA} = 4
\]

You Try:
A rectangle has the following vertices: D(-1, -1), E(-1, 3), F(2, 3), and G(2, -1)

1) Find the length of each side of the rectangle.

\[
\overline{DE} = \quad \overline{EF} = \quad \overline{FG} = \quad \overline{GD} =
\]

2) Find the perimeter of the rectangle above.

3) Find the area of the rectangle above.
Find the Missing Points

If the points on the coordinate plane below are three of the vertices of a rectangle, what are the coordinates of the fourth vertex? Remember that opposite sides of a rectangle are congruent (equal)!

Example:

You Try:

Graph the given coordinates below to find the missing ordered pair to finish the rectangle.

((-3, 5), (-3, -2), (1, 5))

((-4, 2), (-4, -3), (2, 2))

1) What is the missing point? __________________________

2) What is the perimeter of the rectangle? ___________

3) What is the area of the rectangle? ________________

1) What is the missing point? __________________________

2) What is the perimeter of the rectangle? ___________

3) What is the area of the rectangle? ________________
Reflecting a Polygon

Using what we know about reflections, we can reflect a polygon across an axis as well. Simply reflect each ________ and then redraw the figure.

Example:
Graph the following points to form a rectangle and then reflect it across the Y axis.

A(1, 3)  B(4, 3)  C(1, -2)  D(4, -2)

A′ (-1, 3)  B′ (-4, 3)  C′ (-1, -2)  D′ (-4, -2)

A′ is said A “prime” and it represents the new, reflected, point. That way it is easy to match up the original point with its reflection.

Remember: Perimeter is the sum of all the sides. Find the distance of each side and add them together.

Area is the base times the height. Find those distances and then find the product.

You Try:
Graph the following points to form a rectangle and then reflect it across the Y axis.

A(2.5)  B(5.5)  C(2,-5)  D(5, -5)

A′ ( , )  B′ ( , )  C′ ( , )  D′ ( , )

1) What is the perimeter of the new rectangle?

2) What is the area of the new rectangle?

Graph the following points to form a rectangle and then reflect it across the X axis.

A(-4, 3)  B(-4,1)  C(3,3)  D(3, 1)

A′ ( , )  B′ ( , )  C′ ( , )  D′ ( , )

1) What is the perimeter of the new rectangle?

2) What is the area of the new rectangle?
Extra Practice

For #’s 1-4, write an integer for each situation:
1) withdraw $20  
2) a gain of 3 days vacation  
3) 27 feet below sea level  
4) 10 units to the right on a number line

5) Graph the set \{-2, 2, 0, -1, 6, -4\} on the number line.

\[ \begin{array}{ccccccc}
-7 & -6 & -5 & -4 & -3 & -2 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\
\end{array} \]

6) The opposite of \(-23\) is:  
7) The opposite of \(-16\) is:  
8) The opposite of \(150\) is:  
9) The opposite of \(56\) is:

Find the absolute value for each of the problems below.

10) \(|8| \)  
11) \(|-91| \)  
12) \(-|100| \)  
13) \(|-13| \)  
14) \(|729| \)  
15) \(-|-2| \)

Use the symbols <, >, = to compare the following numbers.

16) \(15 \underline{\quad} 12 \)  
17) \(|-32| \underline{\quad} |37| \)  
18) \(68 \underline{\quad} -79 \)  
19) \(|-47| \underline{\quad} 47 \)  

Put the numbers in order from LEAST to GREATEST.

20) \(-23, 58, 9, -38, 0 \)

21) \(-71, -56, 2, 92, -7 \)

Graph the given coordinates below to find the missing ordered pair to finish the rectangle.

\((-2, 2), (-2, 5), (-5, 2) \)

Graph the given coordinates below to find the missing ordered pair to finish the rectangle.

Use the rectangle above and the coordinate plane to find the reflection of the rectangle across the x and y axis.

Reflection over the x-axis:
\(A'(\,\,\,), B'(\,\,\,), C'(\,\,\,), D'(\,\,\,)\)

Reflection over the y-axis:
\(A'(\,\,\,), B'(\,\,\,), C'(\,\,\,), D'(\,\,\,)\)