Unit 5

Area & Volume

Area Composite Area Surface Area Volume

1/15	1/16			
	1/10	1/17	1/18	
Unit 5 Test Or Computer Lab	Unit 5 Test Or Computer Lab	Unit 5 Pre-Test MSG Set Up Unit Preview	Area	
IXL Skills Week of 1/7: (6th Grade) FF.2, (Sixth Grade) CC.1 & (Sixth Grade) CC.5				
1/22	1/23	1/24	1/25	
Area	Area	Composite Area	Quiz (Area)	
IXL Skills Week of 1/14: (Sixth Grade) FF.5, (5 th Grade) EE.5 & (5 th Grade) EE.6				
1/29	1/30	1/31	2/1	
Composite Area Or Computer Lab	Composite Area	Surface Area	Quiz (Composite Area)	
L Skills Week of 1	/21: (5 th Grade) El	E.7, (6 th Grade) FF.	7	
2/5	2/6	2/7	2/8	
Surface Area	Surface Area	Volume of Rectangular Prisms with Fractional Edges	Quiz (Surface Area	
IXL Skills Week of 1/21: (6 th Grade) FF.15 & (6 th Grade) EE.1 & (6 th Grade) EE.3				
2/12	2/13	2/14	2/15	
Volume of Rectangular Prisms with Fractional Edges or Computer Lab	Unit 5 Post Test & Review Area, Composite Area, Surface Area and Volume	Unit 5 End of Unit Test	Unit 5 End of Unit Test	
	Or Computer Lab c of 1/7: (6 th Grac 1/22 Area ek of 1/14: (Sixth 1/29 Composite Area Or Computer Lab Computer Lab Composite Area Or Computer Lab Computer Lab Computer Lab Composite Area Or Computer Lab Computer Lab Computer Lab Computer Lab Computer Lab Computer Lab Computer Lab Computer Lab	Or Computer LabOr Or Computer Labc of 1/7: (6th Grade) FF.2, (Sixth Grade) 1/221/23AreaAreaAreaAreaek of 1/14: (Sixth Grade) FF.5, (5th Grade) 1/291/30Composite Area Or Computer LabComposite AreaAreaComposite AreaOr Computer LabComposite AreaSurface AreaSurface AreaSurface AreaSurface Areaek of 1/21: (6th Grade) FF.15 & (6th Grade)2/122/13Volume of Rectangular Prisms with Fractional Edges or Computer LabUnit 5 Post Test Area and Volume	Or Computer LabOr Computer LabMSG Set Up Unit Previewc of 1/7:(6th Grade) FF.2, (Sixth Grade) CC.1 & (Sixth1/221/231/24AreaAreaComposite AreaAreaAreaComposite Area1/291/301/31Composite AreaComposite AreaSurface AreaOr Computer LabComposite AreaSurface AreaVolume of Rectangular Prisms with Fractional EdgesSurface AreaVolume of Rectangular Prisms with Fractional EdgesUnit 5 Post Test & Review Area andUnit 5 End of Unit 5 End of Unit Test	

Name: _____

Math Teacher:

Unit 5: Area & Volume Standards, Checklist and Concept Map

Georgia Standards of Excellence (GSE):

<u>GSE6.G.1</u>: Find area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems

• Find the area of a polygon (regular or irregular) by dividing it into squares, rectangles, and/or triangles and find the sum of the areas of those shapes

<u>GSE6.C.2</u>: Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas **V** = *lwh* and **V** = *Bh* to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

<u>GSE6.G.4</u>: Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.

What Will I Need to Learn??

 	_ I can find the area of a polygon by splitting it up into squares, rectangles, and/or triangles, and finding the sum of all of the areas
 	_ I can find the volume of a right rectangular prism with fractional edges by packing it with unit cubes
 	_ I can apply the formula V = Iwh to find the volume of a right rectangular prism with fractional edge lengths
	l can represent 3-dimensional shapes with nets
 	I can use nets to determine the surface area of 3-dimensional figures
 	_ I can apply these concepts of area, volume, and surface area to solve real-world and mathematical problems

Unit 5 Circle Map: Make a Circle Map below of important vocab and topics from the standards listed to the left.

Unit 5 - Vocabulary

Term	Definition and/or Picture-Example
Area	
Base (of a triangle)	
Base (of a 3D figure)	
Congruent	
Cubic Units	
Edge	
Equilateral Triangle	

Term	Definition and/or Picture-Example
Face	
Isosceles Triangle	
Lateral Faces	
Net	
Parallel	
Parallelogram	
Perpendicular	

Term	Definition and/or Picture-Example
Polygon	
Regular Polygon	
Polyhedron	
Prism	
Pyramid	
Quadrilateral	
Rectangle	
Rectangular Prism	

Term	Definition and/or Picture-Example
Rhombus	
Right Triangle	
Scalene Triangle	
Square	
Surface Area	
Trapezoid	
Vertex (vertices)	
Volume	

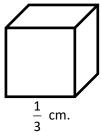
Math 6 - Unit 5: Area & Volume Review

Knowledge & Understanding

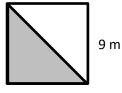
- How could you determine the area of a composite figure, such as the ones shown here?
- 2) What types of units are used to describe area?
- 3) What types of units are used to describe volume?

Proficiency of Skills

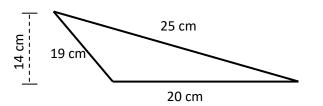
4) Determine the volume of the cube:



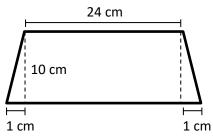
5) Find the area of the shaded section of the square: _____



6) Find the area of the triangle: _____

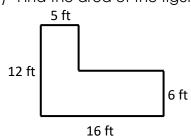


7) Determine the area of the trapezoid:



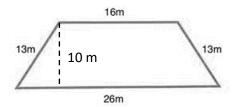
8) The surface area of a cube can be found by using the formula $SA = 6s^2$. Determine the surface area of a cube with a length of 8cm.

9) Find the area of the figure shown below:



Application

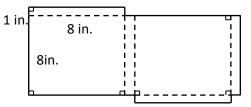
- 10) If carpet costs \$4 per square yard, how much would it cost to carpet a rectangular room that is 6 yards wide and 10 yards long?
- 11) What is the area of the trapezoid?



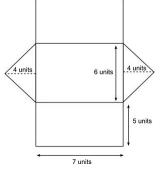
12) A rectangular prism is filled with small cubes of the same size. The bottom layer consists of 9 cubes, each with a volume of 2 cubic inches. If there are 3 layers of cubes in the prism, what is the volume of the rectangular prism?



13) A box is made of cardboard with no overlap. The net of the box is shown below. How many square inches of cardboard is needed to make the box?



14) Find the surface area of the net below?



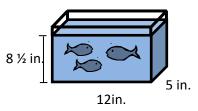
15) Mariah and Max are making a plaque. The center is a 10inch square, and the edges of the frame measure 12 inches long and 12 inches wide.

What is the area of the frame?



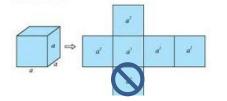
12 ft

16) A fish tank is shown below. What is the volume of the water in the tank?

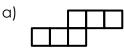


17) How many cubic feet are in a cubic yard?

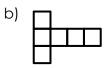
- 18) The volume of a rectangular prism can be found by using the formula V=Bh. If the base of a prism is square with a side length of 3 inches and the height of the prism is 2 ¼ inches, find the volume of the prism.
- 19) Andres is painting five faces of a storage cube (he isn't painting the bottom face). If each faces is 8 inches, how many square inches will he need to paint?



20) Which of the following nets could NOT be folded to form a cube?



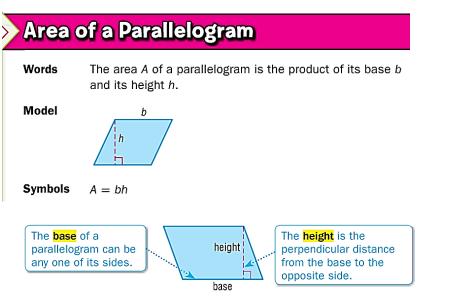






C

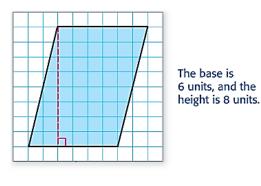
Area of Parallelograms



Parallelograms include special quadrilaterals, such as rectangles, squares, and rhombi.

Examples:

Find the area of the parallelogram.

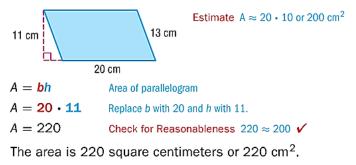




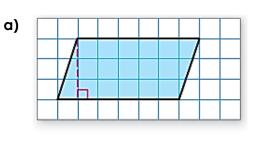
A = 48 Multiply.

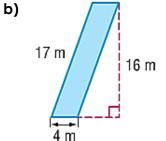
The area is 48 square units or 48 units².

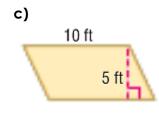
Find the area of the parallelogram.

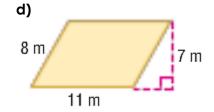


You Try:

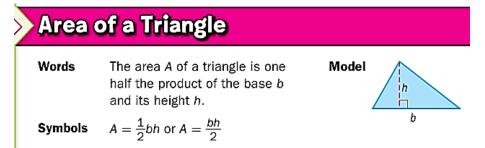






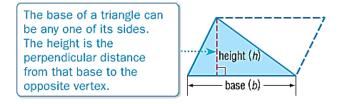


Area of Triangles



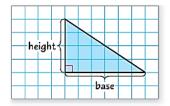
Congruent figures are figures that are the same shape and size.

A parallelogram can be formed by two congruent triangles. Since congruent triangles have the same area, the area of a triangle is one half the area of the parallelogram.



Examples:

Find the area of the triangle.



By counting, you find that the measure of the base is 6 units and the height is 4 units.

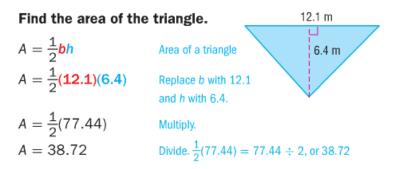
 $A = \frac{1}{2}bh$ Area of a triangle

 $A = \frac{1}{2}(6)(4)$ Replace b with 6 and h with 4.

 $A = \frac{1}{2}(24)$ Multiply.

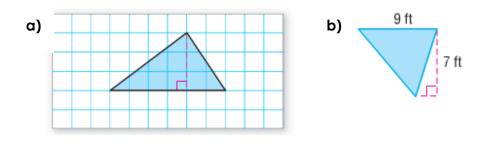
A = 12 Multiply.

The area of the triangle is 12 square units.



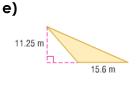
The area of the triangle is 38.72 square meters.

<u>You Try:</u>

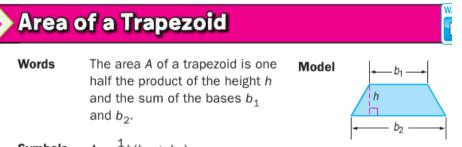






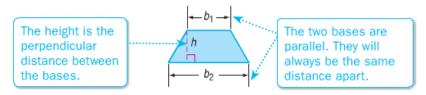


Area of Trapezoids



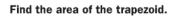
Symbols $A = \frac{1}{2}h(b_1 + b_2)$

A trapezoid has two bases, b_1 and b_2 . The height of a trapezoid is the distance between the bases.



When finding the area of a trapezoid, it is important to follow the order of operations. In the formula, the bases are to be added before multiplying by $\frac{1}{2}$ of the height *h*.

You Try:





The bases are 5 inches and 12 inches. The height is 7 inches.

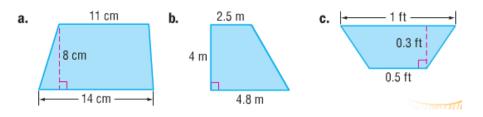
 $A = \frac{1}{2}h(b_1 + b_2)$ Area of a trapezoid $A = \frac{1}{2}$ (7)(5 + 12)Replace h with 7, b_1 with 5, and b_2 with 12. $A = \frac{1}{2}$ (7)(17)Add 5 and 12.A = 59.5Multiply.

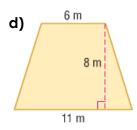
The area of the trapezoid is 59.5 square inches.

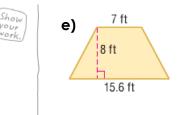
Find the area of the trapezoid.7 m
$$A = \frac{1}{2}h(b_1 + b_2)$$
Area of a trapezoid $A = \frac{1}{2}(9.8)(7 + 12)$ Replace h with 9.8,
 b_1 with 7, and b_2 with 12. $A = \frac{1}{2}(9.8)(19)$ Add 7 and 12. $A = 93.1$ Multiply.

So, the area of the trapezoid is 93.1 square meters.

You Try:

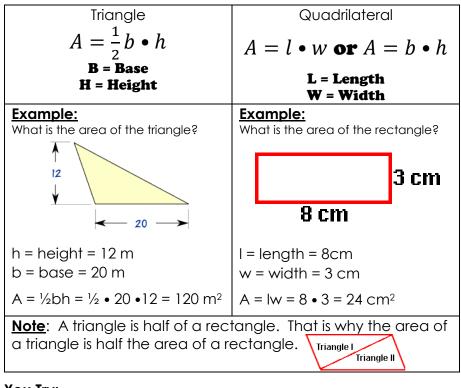






Area of Triangles and Quadrilaterals

Area is the amount of space INSIDE a figure. It is always measured in square units.

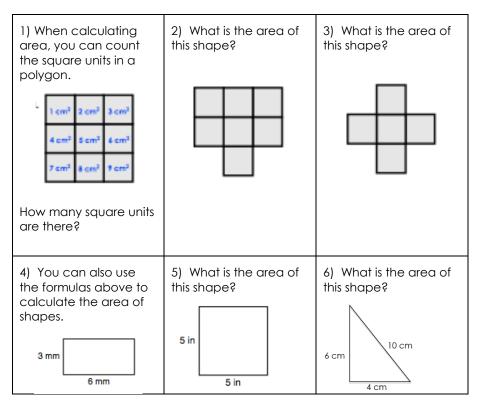


<u>You Try:</u>

Triangle	Square	Rectangle
\wedge		
h = 6ft b = 5ft	side = 8in	1 = 9cm w = 3cm
Formula:	Formula:	Formula:
Area:	Area:	Area:

<u>How</u>	<u>do you calculate area?</u>	Formulas for Area
Area is the of		Square:
	_ units needed to fill a	
	Or, the amount	Rectangle:
of	in a polygon.	
To calculat	e area, you must	Triangle:
	all the	
Area is always measured in		

<u>You Try:</u>



Solve. Include square units in your answer.	Substitute for the variables (Show work)	Write the Picture formula	Picture	Name of Polygon
			22 cm 8 cm	
			10 in 9 in 1 rt	
			9 4 5	

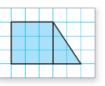
Additional Practice with Area

Area of Composite Figures

A **composite figure** is a figure made of two or more two-dimensional figures. The composite figure shown to the right is made of two rectangles.

Find the Area of a Composite Figure

You can decompose some trapezoids into a square and a triangle to find the area.



Area of Square $A = \ell \cdot w$ $A = 3 \cdot 3$, or 9

Area of Triangle $A = \frac{1}{2}bh$ $A = \frac{1}{2}(2)(3)$, or 3

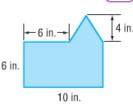
Then add the area of the square and the area of the triangle to find the area of the trapezoid. The area of the trapezoid is 9 + 3 or 12 square units.

You can find the area of a composite figure using the same strategy. To find the area of a composite figure, separate it into figures with areas you know how to find. Then add those areas.

Example

1. Find the area of the figure at the right.

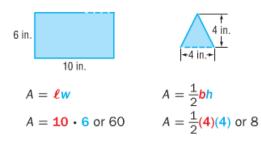
The figure can be separated into a rectangle and a triangle. Find the area of each.



Tutor

Area of Rectangle

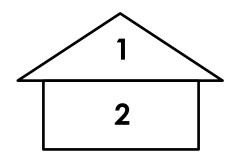
Area of Triangle



The base of the triangle is 10 - 6 or 4 inches.

The area is 60 + 8 or 68 square inches.

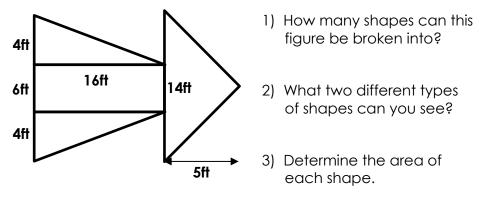
The figure below is a composite figure. How would you find its area?



The house is made up of two shapes that you are familiar with – a triangle and a rectangle. You can "decompose" or "take apart" the figure to find the area of each piece and then find the sum of those areas to get the total area.

<u>Try This:</u>

Find the area of the rocket figure below.

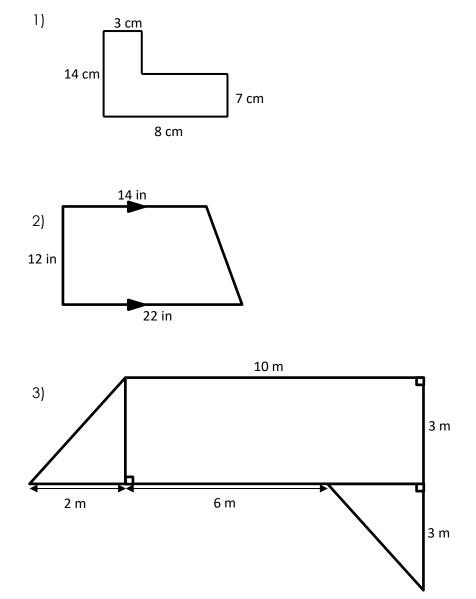


Shape	Shape #1	Shape #2	Shape #3	Shape #4
Formula	Area₄ = ½bh			
Work	½ • 16 • 4 8 • 4			
Solution	32 ft ²			

Lastly, add the area of each piece. Total Area = _

You Try:

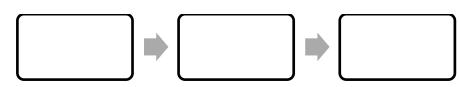
Find the area of each composite figure. Remember to show all work! (Hint: Often, you will have to draw in lines to decompose the figure. Pay careful attention to the side lengths that are given so you can figure out the side lengths that are missing!)



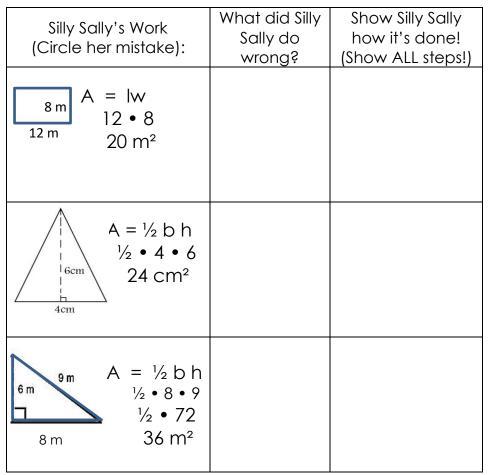
Area Error Analysis



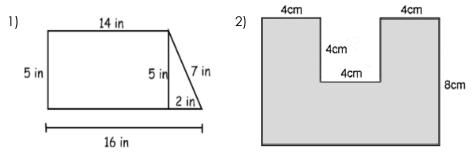
Fill in the Flow Map with the 3 steps to solving problems on area:

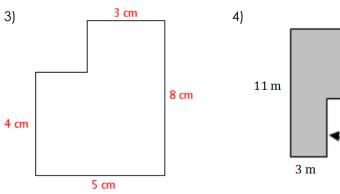


Silly Sally has struck again! Analyze her work in Column #1, and <u>circle her mistake</u>. In Column #2, explain what she did wrong. In Column #3, work out the problems correctly, showing ALL work!



Find the area of each composite figure:





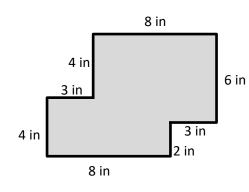
4 m

12 m

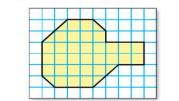
5 m

More Area Practice with Composite Figures

1) Find the area of the figure.



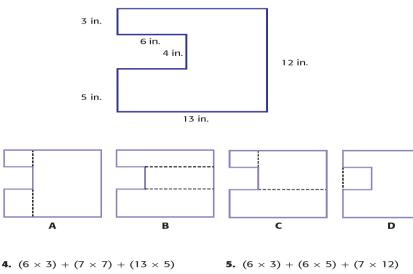
2) The shaded part of the grid represents the plans for a fish pond.



If each square on the grid represents 5 square feet, what is the approximate area of the fish pond?

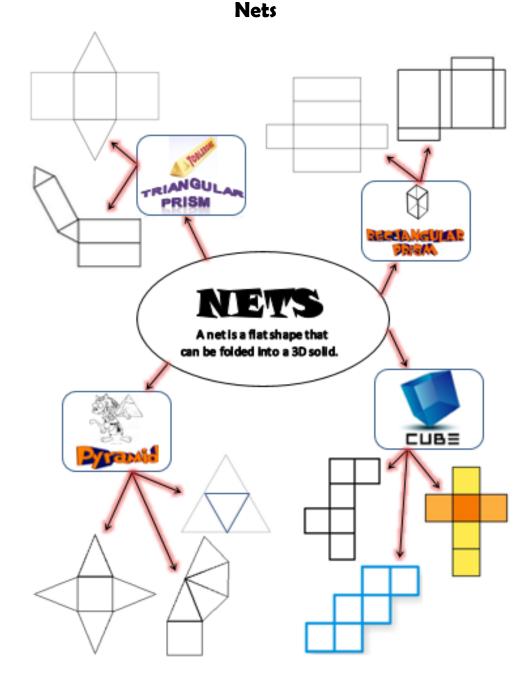
- F. 175 square feet
- G. 165 square feet
- H. 150 square feet
- I. 33 square feet





6. (13 × 12) – (6 × 4)

- _____
- **7.** $(13 \times 3) + (7 \times 4) + (13 \times 5)$



Pg.14a

Nets of 3-Dimensional Figures

Face is a flat _____ of a solid figure.

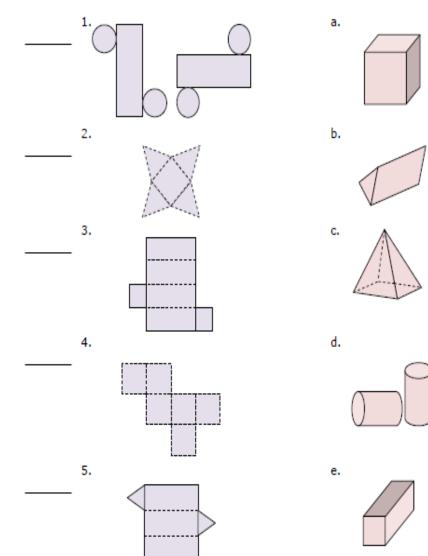
<u>Vertex</u> is a _____ where _____ or more edges of a solid figure meet or the pointed end of a cone opposite of its base.

FIGURE	FACES Look Like	BASE	How many faces?	NET
Cube				
Rectangular Prism				
Triangular Prism				
Square Pyramid				
Triangular Pyramid				
Cylinder				
Cone				

Matching Nets and 3-D Figures

Using Nets to Understand 3-D Figures - Matching Worksheet

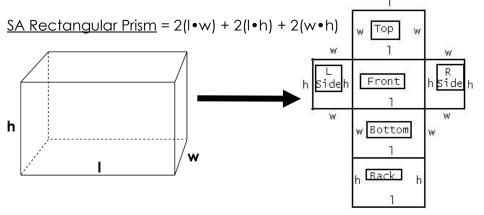
Write the letter of the shape that each net would create.



Using Formulas to Find Surface Area

A **formula** is a mathematical rule using variables. It allows us to easily find a value such as area, volume, circumference, perimeter, etc. Formulas are used often in math and science!

Formulas for Surface Area:



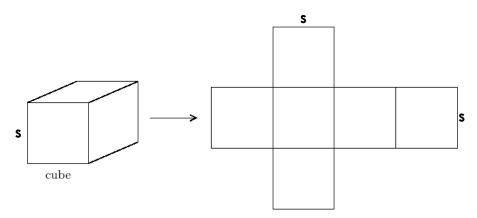
Using Formulas to Find Surface Area

So... what exactly IS surface area, anyway?



Draw a rectangular prism:	Draw the net of a rectangular prism:
How do you think you could calculate	the SURFACE AREA of a
RECTANGULAR PRISM?	

<u>SA Cube</u> = 6s²





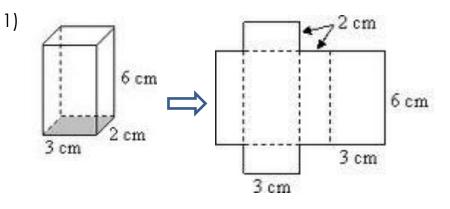
Draw a SQARE PYRAMID:	Draw the net of a SQARE PYRAMID :
How do you think you could calc PYRAMID ?	culate the SURFACE AREA of a SQARE



Draw a CUBE :	Draw the net of a CUBE :
How do you think you could calculate the SURFACE AREA of a CUBE ?	

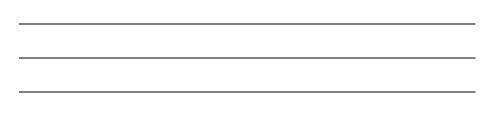
You Try:

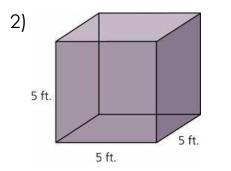
Using either method (nets or formulas), find the surface area.

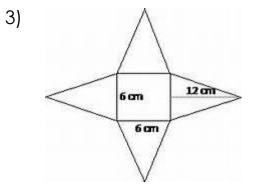


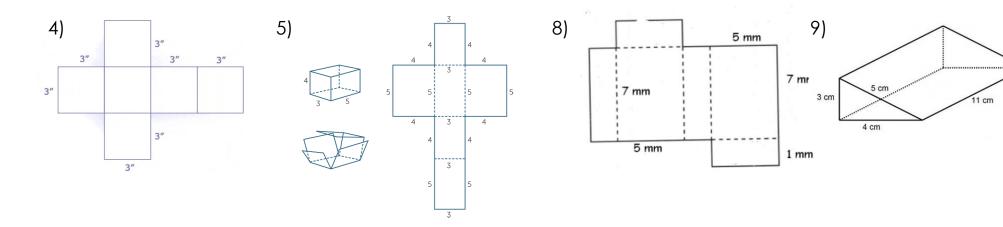
Complete the following statement:

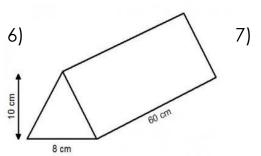
When I need to find the surface area of a 3-dimensional (3-D) figure, I can do that by...



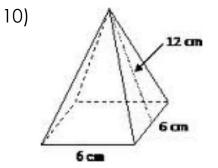


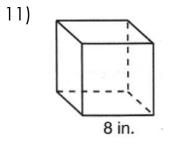






7) Find the Surface Area of a cube with side length 4cm.





Surface Area in the Real World

Solve each of the problems by drawing a net and finding the surface area.

1) A pizza box is 15 inches wide, 14 inches long, and 2 inches tall. How many square inches of cardboard were used to create the box?



4) Sydney is painting a rectangular toy box for her little brother. She will paint all 4 sides and the top (she will NOT paint the bottom). If the toy box is 20 inches tall, 12 inches wide, and 25 inches long, how many square inches will she need to paint?



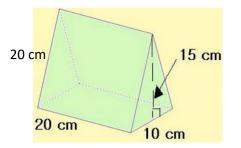
2) What is the surface area of a Rubik's Cube that is 6 cm tall?



3) Angelo is making a replica of an Egyptian pyramid. He is making a square pyramid with a base that is 3 feet long and 3 feet wide. The triangular sides of the pyramid each have a height of 14 feet. How much material will Angelo need to cover the pyramid?

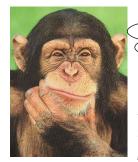


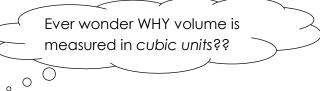
5) DeAndre is making a tent for his hamster. It is 20 cm long, and the triangular bases are 15 cm high and 10 cm wide (see picture below). How much material will he need to make the tent?



Volume of Rectangular Prisms

Volume is the amount of space inside a 3D object, measured in cubic units.





Since volume measures the amount of space INSIDE a figure, it's like you're packing the figure with little tiny cubes!!

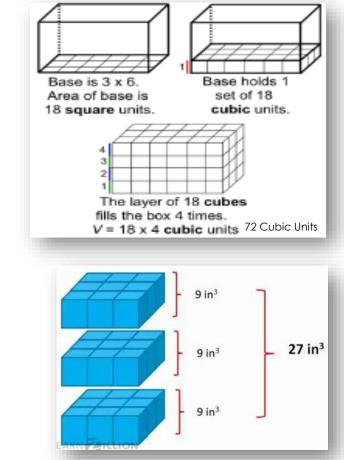
Here's a visual of a <u>rectangular</u> <u>prism</u> being packed with unit cubes...

Here's a visual of

packed with unit

a cube being

cubes...

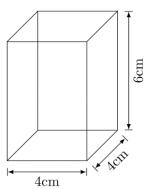


Volume is the ______ of _____ units needed to fill the space in a three dimensional (3D) figure. <u>Volume is always measured in cubic units.</u> We calculate volume you must find the area of the ______ then multiply it by the ______. This can be written as ______ • ____.

OR ______ • _____ for a rectangular prism.

Example:

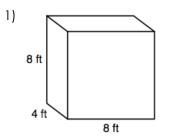
Find the volume of the rectangular prism below.

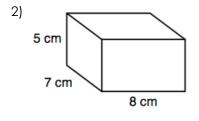


$$V = B \bullet h$$
$$V = I \bullet w \bullet h$$
$$V = 4 \bullet 4 \bullet 6$$
$$V = 96 \text{ cm}^3$$

<u>You Try:</u>

Find the volume.





3) 4 ft 6 ft 10 ft	4) 6 cm 8 cm 4 cm
5) Find the volume of a rectangular prism with B = 78ft ² and h = 23 ft.	6) Find the volume of a rectangular prism with I = 4.2cm, w = 3.8cm, and h = 6cm.
7) Find the volume of a rectangular prism with I = 8 ¼ in., w = 9in and h = 15in.	 8) Find the missing dimension of the rectangular prism. L = 14 cm W = ? H = 3 cm V = 294 cm

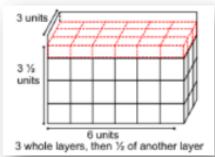
Volume of Rectangular Prisms with Fractional Edges

Let's calculate the volume of a rectangular prism with a length of 6 units, a width of 3 units, and a height of 3 $\frac{1}{2}$ units.

Look at the picture! \rightarrow

The bottom layer contains 6 units across and 3 units back, for a total of 18 units.

Then, there are 3 ½ layers of 18 units. (You have 3 layers, and then half of another layer.)



So, the total volume of this figure is 18 + 18 + 18 + 9 = 63 cubic units.

Let's calculate the amount of water that Nora can pour into her fish tank that is 10 inches long, 6 inches wide, and 5 ¼ inches deep.

The bottom of the tank is 10 inches long and 6 inches wide, so the bottom layer is 60 cubic inches.

Then, there are 5 ¼ layers of 60 units. The volume of the tank is...

5 layers of 60 + ¼ layer

60 + 60 + 60 + 60 + 60 + 15 = 315 cubic inches

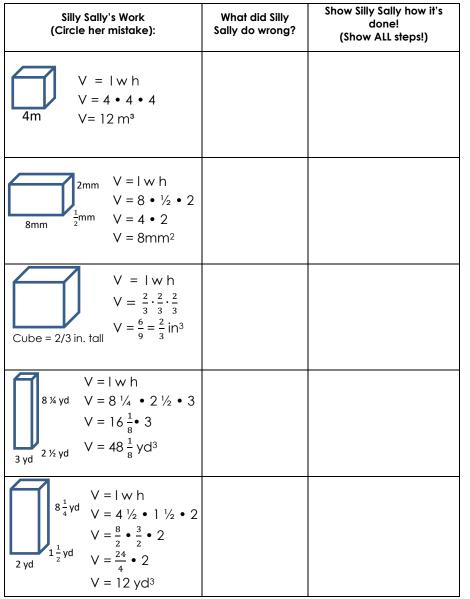
<u>You Try:</u>

Find the volume of a rectangular prism with a length of 3cm, a width of $2\frac{1}{2}$ cm, and a height of 4 cm.

Volume Error Analysis 🔹



Sally is a silly little girl that makes silly mistakes! <u>CHOOSE ANY 4</u> <u>PROBLEMS BELOW</u>. Analyze her work in Column #1, and <u>circle her</u> <u>mistake</u>. In Column #2, explain what she did wrong. In Column #3, show how Silly Sally should work out the problem. Show ALL work!



More Volume Practice

Determine the Volume of each rectangular prism or cube below. Include units and show your work!

1. A cube that is 12 yards wide

2. The box with dimensions of 6 ft \bullet 4 ft \bullet 1 $\frac{1}{2}$ ft

3. Determine the Volume of a rectangular truck bed that is 12 feet long, 5 1/4 feet wide, and 3 feet deep.

4. How much water can be poured into a cubic tank that is 2 $^{\prime\!\!/}_{\!\!/}$ feet long?

5. What is the volume of a gift box that is 3 ½ inches wide, 2 inches tall, and 6 inches long?