

Math 6

Unit 1

Number System

Fluency

Greatest Common Factor (GCF)
Least Common Multiple (LCM)
Long Division
Operations with Decimals
Dividing Fractions

Name: _____

Math Teacher: _____

Unit 1 Pacing

Week 1: Getting to Know You, Procedures & Initial Assessments

Week 2: Factors, Multiples & Divisibility Rules

Week 3: Greatest Common Factor (GCF), Least Common Multiple (LCM)

Week 4: GCF/LCM Word Problems & Long Division

Week 5: Long Division with Remainders, Review and Test

Week 6: Dividing and Multiplying Decimals

Week 7: Adding and Subtracting Decimals & Mixed Decimal Practice

Week 8: Adding, Subtracting & Multiplying Fractions

Week 9: Dividing Fractions, Review & Test

IXL Login (<https://www.ixl.com/signin/ecms>)

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Unit 1: Number System Fluency

Standards, Checklist and Concept Map

Georgia Standards of Excellence (GSE):

MGSE6.NS.2: Fluently divide multi-digit numbers using the standard algorithm.

MGSE6.NS.3: Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.

MGSE6.NS.1: Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. *For example, create a story context for $(2/3) \div (3/4) = 8/9$ because $3/4$ of $8/9$ is $2/3$. (In general, $(a/b) \div (c/d) = ad/bc$.) How much chocolate will each person get if 3 people share $1/2$ lb of chocolate equally? How many $3/4$ -cup servings are in $2/3$ cup of yogurt? How wide is a rectangular strip of land with length $3/4$ mi and area $1/2$ square mi?*

MGSE6.NS.4: Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express the sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor. *For example, express $36 + 8$ as $4(9 + 2)$.*

What Will I Need to Learn??

- _____ I can divide numbers using the standard algorithm
- _____ I can interpret & solve division word problems
- _____ I can add and subtract decimals
- _____ I can multiply decimals
- _____ I can divide decimals
- _____ I can divide fractions using an algorithm
- _____ I can use pictures to represent division of fractions
- _____ I can find the GCF of 2 numbers ≤ 100
- _____ I can find the LCM of 2 numbers ≤ 12
- _____ I can solve real-world problems involving the number system

Unit 1 Circle Map

Create a **Circle Map** of important vocab and topics from the standards listed above.

Unit 1 IXL Tracking Log

Skill	Your Score
C.1 (Divisibility Rules)	
E.4 (Identify Factors)	
E.8 (Greatest Common Factor - GCF)	
E.10 (Least Common Multiple - LCM)	
E.12 (GCF & LCM Word Problems)	
E.13 (Sort Factors of Numerical Expressions)	
C.5 (Dividing Whole Numbers with 2-Digit Divisors)	
C.3 (Divide Numbers Ending in Zero – Word Problems)	
H.7 (Division with Decimal Quotients)	
G.1 (Adding and Subtracting Decimals)	
O.5 (Add, Subtract, Multiply or Divide Two Decimals)	
O.6 (Add, Subtract, Multiply or Divide Two Decimals – Word Problems)	
I.4 (Write Fractions in Lowest Terms)	
I.8 (Convert Between Improper Fractions and Mixed Numbers)	
J.1 (Add & Subtract Fractions with Like Denominators)	
J.3 (Add & Subtract Fractions with Unlike Denominators)	
K.6 (Multiplying Two Fractions)	
K.12 (Multiplying Mixed Numbers & Whole Numbers)	
L.2 (Reciprocals)	
L.5 (Divide Fractions)	
L.7 (Divide Fractions and Mixed Numbers)	

Unit 1 - Vocabulary

Term	Definition
Algorithm	A step-by-step method used to solve a problem
Difference	The result when two numbers are subtracted
Dividend	The number being divided
Divisibility	A number has divisibility when it can be divided evenly without a remainder
Divisor	A number that divides into the dividend
Factor	A whole number that divides exactly into another number
Greatest Common Factor (GCF)	The biggest number that will divide two or more numbers exactly
Least Common Multiple (LCM)	The smallest number that is the multiple of two or more numbers
Multiple	The product of a number and any whole number
Place value	The value of a digit depending on its place in a number
Prime number	A number that has exactly two factors, one and itself
Product	The result when two quantities are multiplied
Quotient	The number that results from dividing one number by another
Reciprocal	One of two numbers whose product is 1; the result of "flipping" a fraction
Simplify	To reduce the numerator and denominator of a fraction to the smallest numbers possible
Remainder	The part "left over" in division.
Sum	The result of adding

Unit 1 – Vocabulary – You Try

Term	Definition/Illustration/Example
Algorithm	
Difference	
Dividend	
Divisibility	
Divisor	
Factor	
Greatest Common Factor (GCF)	
Least Common Multiple (LCM)	
Multiple	
Place value	
Prime number	
Product	
Quotient	
Reciprocal	
Simplify	
Remainder	
Sum	

Unit 1 Pt. 1 Review: GCF/LCM and Long Division

Complete the following problems to review this unit.

You must show all work to receive credit!

- 1) Find the greatest common factor of 30 and 48.
- 2) Find the least common multiple of 10 and 6.
- 3) Which choice lists all the factors of 48?
a. 1, 2, 4, 12, 24, 48 b. 1, 2, 3, 4, 6, 8, 12, 16, 24, 48
c. 0, 1, 2, 4, 6, 8, 12, 16, 48 d. 1, 2, 3, 4, 6, 10, 12, 15, 18, 24, 48
- 4) Is it possible to have a Greatest Common Multiple? Yes No
Explain your reasoning. _____

- 5) Is it possible to have a Least Common Factor? Yes No
Explain your reasoning. _____

For #s 6 & 7, find the quotient, and write your remainders as a fraction AND a decimal.

6) $2 \overline{)537}$

Fraction:

Decimal:

7) $15 \overline{)6,138}$

Fraction:

Decimal:

- 8) Talia has 28 pencils and 42 erasers. She is splitting them into bags for new students. Each bag will have an equal number of pencils and erasers. What is the maximum number of bags she can make? How many pencils and erasers will be in each bag?
bags she can make: _____
pencils per bag: _____
erasers per bag: _____
- 9) Hot dogs come in packs of 8 and hot dog buns come in packs of 10. What is the least number of packs of each that can be bought to make hot dogs (one hot dog and one bun) with no hot dogs or buns left over?
total number of hot dogs: _____
packs of hot dogs: _____
packs of buns: _____
- 10) A shipment of 478 textbooks came to a school. The books are being given out in class sets of 25. How many classrooms will receive a full class set of textbooks?
- 11) There are 1,460 people waiting to ride a roller coaster. Each cart takes 30 people. How many carts will it take for everyone in line to have a turn?

Unit 1 Pt. 2 Review: Decimals and Fraction Division

Complete the following problems to review this unit.

You must show all work to receive credit!

1) $\frac{3}{5} \div \frac{1}{5} =$

2) $13.12 + 6 + 7.1 =$

3) $(1.25)(2.3) =$

4) $\frac{5}{10} \div 10 =$

5) $72 - 1.68 =$

6) $5\frac{1}{2} \div 2\frac{1}{2} =$

7) A quarterback practiced for $28\frac{1}{2}$ hours in 4 weeks. How many hours did he practice per week?

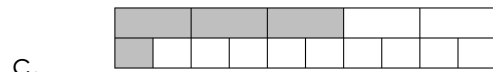
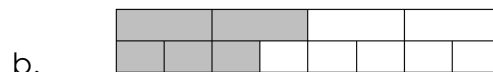
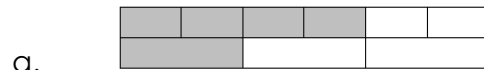
8) Sarah paid \$4.80 for 1.2 pounds of sunflower seeds. What is the cost for one pound of sunflower seeds?

9) A group of friends has ordered 3 pizzas to share. If each person ate $\frac{1}{4}$ of a pizza, and there is no pizza left over, how many friends split the pizza?

10) Emma has \$3 to buy school supplies. She buys 3 folders that are \$0.55 each. She wants to spend the remaining money on pencils that are \$0.05 each. How many pencils can she purchase?

11) Ian bought a milkshake for \$3.58 and a burger for \$5.17. If he paid with a \$10 bill, how much change did he receive?

12) Cameron is cutting a roll of cookie dough into pieces that are $\frac{1}{3}$ inch thick. If the roll of cookie dough is $\frac{4}{6}$ inches long, which model best represents the situation? Write and solve the division problem next to the model.



Divisibility Rules

Divisibility rules help you determine if a number can be evenly divided into another number.

2 If the last digit of a number is even, then the number is divisible by 2.

3 If the sum of all the digits in a number is divisible by 3, then the number is divisible by 3.

4 If the last two digits of a number are divisible by 4, then the number is divisible by 4.

5 If the last digit of a number is 0 or 5, then the number is divisible by 5.

6 If a number is divisible by both 2 and 3, then the number is divisible by 6.

7 If the last digit of a number is doubled and then subtracted from the rest of the number, and the answer is 0 or is divisible by 7, then the number is divisible by 7.

8 If the last three digits of a number are divisible by 8, then the number is divisible by 8.

9 If the sum of all the digits in a number is divisible by 9, then the number is divisible by 9.

10 If the last digit of a number is 0, then the number is divisible by 10.

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Divisibility Rules Practice

For each number below, test the divisibility rules for 2, 3, 4, 5, 6, 9, and 10 and circle which numbers they are divisible by. Some numbers are divisible by several numbers but some may not be divisible by any. Use your notes!

1) **42:** 2 3 4 5 6 9 10

2) **64:** 2 3 4 5 6 9 10

3) **540:** 2 3 4 5 6 9 10

4) **100:** 2 3 4 5 6 9 10

5) **139:** 2 3 4 5 6 9 10

6) **612:** 2 3 4 5 6 9 10

7) **30:** 2 3 4 5 6 9 10

8) **124:** 2 3 4 5 6 9 10

9) **126:** 2 3 4 5 6 9 10

10) **4428:** 2 3 4 5 6 9 10

11) **513:** 2 3 4 5 6 9 10

12) **330:** 2 3 4 5 6 9 10

Factors and Products

Factors are whole numbers that multiply together to make a **product**.

$$\begin{array}{c} \text{Factor} \quad \text{Factor} \\ \swarrow \quad \searrow \\ 2 \cdot 3 = 6 \\ \leftarrow \text{Product} \end{array}$$

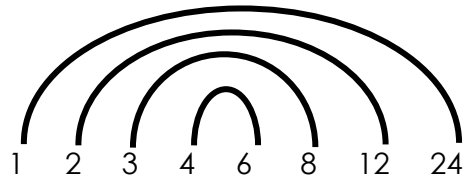


Products are answers you get when you multiply **factors**.

Example:

Find the factors of 24.

Use a factor rainbow.



Use a factor table.

24	
1	24
2	12
3	8
4	6

The factors of 24 are: 1, 2, 3, 4, 6, 8, 12 and 24

You Try:

Find all of the factors of the following numbers.

- 1) 18 2) 60 3) 45

- 4) 120 5) 19 6) 39

Multiples

Multiples are the product of a number and any whole number.

Example: Find the first 10 multiples of the number 2.

2: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20

2: 2, 4, 6, 8, 10, 12, 14, 16, 18, 20

You Try:

Find the first 6 multiples of the following numbers.

- 1) 7 2) 8 3) 5

- 4) 12 5) 20 6) 31

Extra Practice with Factors and Multiples

Find all of the factors of each number and the first 6 multiples.

- 1) 11

Factors: _____

Multiples: _____

- 2) 48

Factors: _____

Multiples: _____

GCF (Greatest Common Factor)

Definition: The biggest number that will divide two or more numbers exactly

Method #1: Make a list

Algorithm:

Method #2: Use a sled

Algorithm:

GCF Examples

There are two ways to find the GCF (Greatest Common Factor). You can simply list the factors, or you can use the SLED method.

Example:

Find the GCF by making a list of all of the factors.

24: 1, 2, 3, 4, **6**, 8, 12, 24

30: 1, 2, 3, 5, **6**, 10, 15, 30

The largest factor that 24 and 30 share in common is 6, so 6 is the GCF.

Find the GCF by using the SLED method.

First, set up a sled with the numbers on it. Divide by the common factors that the numbers share. Keep dividing until the only common factor that remains is 1.

2	24	30
3	12	15
4		5

The GCF is the product of the factors on the **left**, so the GCF is 2×3 which is 6. **"GCF is on the LEFT!"**

You Try:

Find the GCF for the following sets of numbers.

1) 16 and 72

2) 90 and 75

3) 54 and 18

LCM (Least Common Multiple)

Definition: The smallest number that is the multiple of two or more numbers

Method #1: Make a list

Algorithm:

Method #2: Use a sled

Algorithm:

LCM Examples

There are two ways to find the LCM (Least Common Multiple). You can simply list multiples of each number until you find one they have in common or you can use the SLED method.

Example:

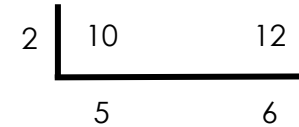
Find the LCM by making a list of the multiples.

10: 10, 20, 30, 40, 50, **60**, 70, 80

12: 12, 24, 36, 48, **60**

The smallest multiple that 10 and 24 have in common is 60, so 60 is the LCM.

Find the LCM by using the SLED method.



The LCM is the product of all of the factors, so the LCM is $2 \times 5 \times 6$ which is 60. **“LCM is all of them!”** Notice that the factors form the letter “L” for LCM.

You Try:

Find the LCM for the following sets of numbers.

- 1) 8 and 6 2) 12 and 20 3) 25 and 100

GCF and LCM

Find the GCF and LCM for each set of numbers.

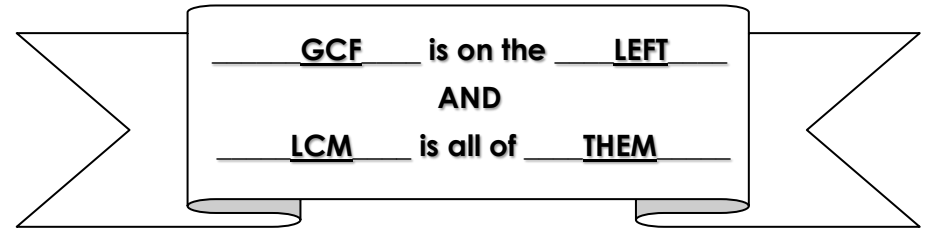
- 1) 15 and 40 2) 5 and 10
 GCF: _____ LCM: _____ GCF: _____ LCM: _____

- 3) 12 and 54 4) 24 and 64
 GCF: _____ LCM: _____ GCF: _____ LCM: _____



- 5) 7 and 10 6) 7 and 49
 GCF: _____ LCM: _____ GCF: _____ LCM: _____

- 7) 12 and 18 8) 16 and 36
 GCF: _____ LCM: _____ GCF: _____ LCM: _____

GCF and LCM in Problem Solving



TIP #1 – Look for **KEY** words that will tell you if you're finding GCF or LCM!

 WORDS GCF	 WORDS LCM
FACTORS – Think Division Grouping Sharing Same Amount Equally/Each Key Words: Greatest, Most, Maximum, Largest	MULTIPLES – Think Multiplication Repetition At the same time Same/Both Key Words: Same, Both, Smallest, Minimum, Least, Fewest, First

You Try:

Circle the key words in the problems below that let you know if you need to find the GCF or the LCM.


- Johnny is making goodie bags that include a lollipop and bubbles. If the lollipops come 4 to a pack, and the bubbles come 6 to a pack, what is the smallest number of bags that he can make and not have anything left over?
- Shannon is making identical balloon arrangements for a party. She has 24 white balloons and 16 blue balloons. She wants each arrangement to have the same number of each color. What is the greatest number of arrangements that she can make if every balloon is used?

TIP #2 – Draw a picture! Sometimes visualizing the problem will help it to make more sense!

Example 1:

Johnny is making goodie bags that include a lollipop and bubbles. If the lollipops come 4 to a pack, and the bubbles come 6 to a pack, what is the smallest number of bags that he can make and not have anything left over? How many packs of lollipops and bubbles should he buy?




The  **WORDS** is "smallest", so you're finding LCM.

The smallest number of bags w/o leftovers = 12. He needs 3 packs of lollipops and 2 packs of bubbles.

Example 2:

Shannon is making identical balloon arrangements for a party. She has 24 white balloons and 16 blue balloons. She wants each arrangement to have the same number of each color. What is the greatest number of arrangements that she can make if every balloon is used?



The  **WORDS** is "greatest", so you're finding GCF.

She can make 8 balloon arrangements.

You Try:

- 1) There are 40 girls and 32 boys who want to participate in 6th grade intramurals. **If each team must have the same number of girls and the same number of boys, what is the greatest number of teams that can participate in intramurals? How many girls and boys will be on each team?**

of teams _____

of girls _____

of boys _____

- 2) Fred is making some hot dogs for his company picnic. Buns come 12 to a pack and hot dogs come 8 to a pack. **What is the fewest number of hot dogs he can make and not have any leftover buns or hot dogs? How many packs of buns and packs of hot dogs should he buy?**

of hot dogs with buns that can be made _____

of packs of buns _____

of packs of hot dogs _____

- 3) At the Regal Cinemas grand opening, every 8th customer will receive a free drink and every 10th person will receive a free movie rental. **What number customer will be the first to receive both gifts?**

of customer to receive both gifts _____

- 4) Stephen is making a garden of 36 tomato plants and 45 corn plants. He wants to spread the plants out on as many rows as possible, so that each row has the same number of tomato plants and the same number of corn plants. **What is the maximum number of rows that Stephen can plant? How many tomato plants will be on each row? How many corn plants will be on each row?**

of plants per row _____

of tomato plants per row _____

of corn plants per row _____

- 5) Dayvon had a collection of baseball cards that he wants to divide evenly into his albums. He has 36 Braves cards and 48 Cubs cards. **What is the greatest number of albums he can use? How many Braves cards and Cubs cards will be in each album?**

of albums _____

of Braves cards per album _____

of Cubs cards per album _____

- 6) Two pigs entered a race around a track. Piggly takes 6 minutes to run one lap. Wiggly takes 5 minutes to run one lap. **If both pigs begin the race at the same time, what is the shortest number of minutes it will take for them to be back at the starting line? How many laps will each pig have made at that time?**

Time for both pigs to be at starting line _____

of laps for Piggly _____

of laps for Wiggly _____

- 7) Enzo and Beatriz are playing games at their local arcade. Incredibly, Enzo wins 5 tickets from every game, and Beatriz wins 11 tickets from every game. When they stopped playing games, Enzo and Beatriz had won the same number of total tickets. **How many tickets did each student win? How many games did Enzo and Beatriz each play?**

of tickets each student each won _____

games that Enzo played _____

games that Beatriz played _____

- 8) Tim has 39 pairs of headphones and 13 music players. Tim wants to sell all of the headphones and music players in identical packages. **What is the greatest number of packages Tim can make? How many headphones and music players will be in each package?**

packages Tim can make _____

headphones per package _____

music players per package _____

- 9) Audra has two rolls of streamers to use in decorating the school gym for a pep rally. The red streamers are 64 yards long and the blue streamers are 72 yards long. **What is the maximum length each streamer can be so that they are all of equal length? How many red streamers would she have? How many blue streamers would she have?**

Length of each streamer _____

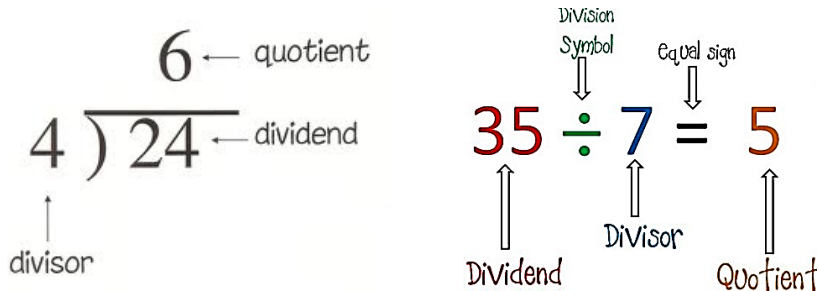
of red streamers _____

of blue streamers _____

Long Division

The purpose of division is to determine how many times the **divisor** fits into the **dividend**.

Division is the inverse (opposite operation) of multiplication. You can use multiplication to **“undo” or check** your answer. Multiply the quotient by the divisor and you should get the dividend.



Example:

Divide:	$\begin{array}{r} 2 \\ 3 \overline{) 75} \\ \underline{6} \\ 15 \end{array}$ <p>3 goes into 7 2 times... with some extra!</p>
Multiply:	$\begin{array}{r} 2 \\ 3 \overline{) 75} \\ \underline{6} \end{array}$ <p>$2 \times 3 = 6$</p>
Subtract:	$\begin{array}{r} 2 \\ 3 \overline{) 75} \\ \underline{6} \\ 15 \end{array}$
Bring Down:	$\begin{array}{r} 2 \\ 3 \overline{) 75} \\ \underline{6} \\ 15 \end{array}$
Repeat:	$\begin{array}{r} 25 \\ 3 \overline{) 75} \\ \underline{6} \\ 15 \\ \underline{15} \\ 0 \end{array}$ <p>$15 \div 3 = 5$ $5 \times 3 = 15$</p>

You Try:

1) $\begin{array}{r} \\ 4 \overline{) 68} \\ \underline{} \\ \\ \underline{} \\ 0 \end{array}$	2) $\begin{array}{r} \\ 2 \overline{) 38} \\ \underline{} \\ \\ \underline{} \\ 0 \end{array}$
3) $\begin{array}{r} \\ 11 \overline{) 4697} \\ \underline{} \\ \\ \underline{} \\ \\ \underline{} \\ \\ \underline{} \\ 0 \end{array}$	4) $\begin{array}{r} \\ 7 \overline{) 98} \\ \underline{} \\ \\ \underline{} \\ 0 \end{array}$
5) $9 \overline{) 6,840}$	6) $4 \overline{) 4,456}$
7) $15 \overline{) 1575}$	8) $25 \overline{) 2575}$

Long Division and Remainders

What is a remainder? A remainder exists when your divisor doesn't go into your dividend evenly, meaning that you don't have enough remaining to make another group. It is the "Left Over" amount after you have divided.

Example:

1) $23 \div 4 =$

4 goes into 23 five whole times, but there are three more left. Those three won't allow us to make another group of 4, so 3 is the remainder.

How do we write remainders? Up until this point, you have probably been writing remainders as "R 3". Now that you know more about what a remainder is, you will need to write your remainders differently to reflect that a remainder represents a PART of the whole.



We can write a remainder in one of two ways: a FRACTION or a DECIMAL.

Examples:

<u>Problem</u>	<u>Instead of writing the quotient as...</u>	<u>Quotient as a Fraction</u>	<u>Quotient as a Decimal</u>
	👎	👍	👍
$13 \div 5$	2 R 3	$2 \frac{3}{5}$	2.6
$93 \div 2$	46 R 1	$46 \frac{1}{2}$	46.5

Remainders as Fractions

Divide: $139 \div 6$

Note: When you divide, the divisor (6) goes into the dividend (139), 23 whole times, but there is 1 left over that won't make another group of 6. 1 is the remainder. We write it as a fraction with the remainder over the divisor. "There is one left when we needed six to make another whole."

$$\begin{array}{r} 23 \frac{1}{6} \\ 6 \overline{) 139} \\ \underline{-0} \\ 13 \\ \underline{-12} \\ 19 \\ \underline{-18} \\ 1 \end{array}$$

You Try:

Find the quotient and write the remainder as a fraction.

1) $154 \div 4 =$

2) $121 \div 8 =$

3) $215 \div 20 =$

4) $45 \div 8 =$

5) $2856 \div 30 =$

6) $222 \div 15 =$

Remainders as Decimals

When you want to write your remainder as a decimal, you add a zero and continue to divide until you get a remainder of zero or you round your answer according to your instructions. If there is no decimal, you must add a decimal before you add a zero.

$$\begin{array}{r}
 25.2 \\
 5 \overline{) 126.0} \\
 \underline{-10} \\
 26 \\
 \underline{-25} \\
 10 \\
 \underline{-10} \\
 0
 \end{array}$$

You Try:

Find the quotient and write the remainder as a decimal.

1) $154 \div 4 =$

2) $121 \div 8 =$

3) $215 \div 20 =$

4) $45 \div 8 =$

5) $2856 \div 30 =$

6) $222 \div 15 =$



You Try:

1) $5 \overline{) 965}$

2) $10 \overline{) 187}$

3) $123 \div 12 =$

4) $708 \div 15 =$

5) $\frac{7694}{3} =$

6) $15 \overline{) 30465}$

Long Division Additional Practice

Find the quotient.

1) $308 \div 22 =$

2) $286 \div 11 =$

3) $1064 \div 38 =$

4) $1296 \div 18 =$

5) $130 \div 20 =$

6) $894 \div 8 =$

7) $5009 \div 10 =$

8) $894 \div 9 =$

Long Division Error Analysis

Sally is a silly little girl who makes mistakes! In Column #1, analyze her work and circle her mistake. In Column #2, explain what she did wrong. In Column #3, show how Silly Sally should work out the problem correctly. Show ALL work!

Silly Sally's Work (Circle her mistake):	What did Silly Sally do wrong?	Show Silly Sally how it's done! (Show ALL steps!)
$\begin{array}{r} 212 \\ 12 \overline{)384} \\ \underline{-24} \\ 144 \\ \underline{-144} \\ 000 \end{array}$		
$\begin{array}{r} 86 \\ 10 \overline{)8600} \\ \underline{-80} \\ 60 \\ \underline{-60} \\ 00 \end{array}$		
$\begin{array}{r} 28 \frac{31}{10} \\ 31 \overline{)878} \\ \underline{-62} \\ 258 \\ \underline{-248} \\ 10 \end{array}$		

Making Sense of Division Problems

You know that a divisor won't always go into a dividend evenly; and when that happens, you're left with a remainder. That "remaining" amount represents a part of the whole. But what exactly does this mean?

Sometimes, for your solution to make sense, you cannot include the remainder. In these cases, you must round your quotient up or down to the nearest whole number.

Examples:

Mickey is making bows for Minnie. Each bow needs 7 in of ribbon. If he has 15 in of ribbon, how many bows can he make?	Goofy's favorite ride holds 7 kids at a time. If 15 kids are in line, how many times will the ride have to go for everyone in line to have a turn?
a) Divide: $7 \overline{)15}$	a) Divide: $7 \overline{)15}$
b) Draw a picture:	b) Draw a picture:
c) What does the remainder represent?	c) What does the remainder represent?
d) Will you have to round your final answer up or down? (Will your remainder be included in your final answer?) Explain.	d) Will you have to round your final answer up or down? (Will your remainder be included in your final answer?) Explain.
e) How many bows can Mickey make?	e) How many times does the ride have to go for everyone to have a turn?

Interpreting Remainders

Round UP when the remainder must be included in the solution.

Round DOWN when the solution must include whole pieces, and it does not make sense to include the remainder.

Would you round up or down? Circle UP or DOWN for each scenario.

- UP DOWN** How many buses are needed to transport students?
UP DOWN How many times can I listen to my favorite song (start to finish) in 1 hour?
UP DOWN How many packs of gum can I buy with \$5?
UP DOWN How many shelves are needed to hold a class set of workbooks?

Solve each problem. Circle A, B, C, or D to indicate the best way to interpret each remainder. Each choice will be used once.

A Round down to the whole number.	B Round up to the next whole number.
C Use a mixed number.	D Use a decimal.

- Ariana charges an hourly rate for babysitting. Last month, she made \$81 for 12 hours of babysitting. How much does she make per hour?
Circle one: **A B C D**
Solution: _____
- A group of 427 people are going on a field trip. Each bus can hold 40 people. How many buses are needed to take everyone on the trip?
Circle one: **A B C D**
Solution: _____
- Kevin and his sisters picked 105 pounds of grapes to sell at a local farmer's market. They split the grapes evenly into 30 bags. How many pounds of grapes were in each bag?
Circle one: **A B C D**
Solution: _____
- Mr. Hernandez owns a Game Stop. Each PS2 game takes up a width of 25 mm. If one shelf is 860 mm wide, how many games can Mr. Hernandez fit on the shelf?
Circle one: **A B C D**
Solution: _____

You Try:

- 1) **HOMEWORK** Lisa solved 448 math problems for homework over 28 days. If she solved the same number of problems each day, how many problems did she solve per day?

- 2) **AT HOME** Meg has a new bookcase for her bedroom with 6 shelves. Each shelf holds 8 books. If Meg has 50 books, how many books will not fit on the bookcase?

- 3) **MEALS** Sandra helped serve meals to 25 families. Each family received the same amount of food. If she served 275 pounds of food, how many pounds of food did each family receive?

- 4) **BATTERIES** A teacher bought a package of 17 batteries to put in her calculators. Each calculator uses 3 batteries. How many calculators can the teacher fill with batteries?

- 5) **FOOTBALL** The football team is raising money to have a new turf field installed. The cost of the turf field is \$48,780. The team has 18 months to raise the money. How much do they need to raise each month?

- 6) **WINDOWS** A window washing company has a contract to wash 3,082 windows on a 23-story building. If there are the same number of windows on each floor, how many windows are there on each floor?

- 7) **SCHOOL** There are 32 students in a math class. Each table in the classroom seats 6 students. How many tables will be needed to seat all of the students?

- 8) **DELIVERIES** Mr. Thomas is delivering bricks to a construction site. His truck holds 387 bricks at one time. The builder has ordered 2,800 bricks. How many trips will Mr. Thomas have to make to deliver all the bricks?

Place Value Review

Place Value Table									
Thousands	Hundreds	Tens	Ones		Tenths	Hundredths	Thousandths	Ten-Thousandths	Hundred-Thousandths
			3	.	4	5			

When reading a decimal you say "and" in place of the decimal and you use the name of the column of the last digit when reading a decimal. For example, 3.45 is read as *three and forty-five hundredths*.

You Try:

Write the following numbers:

- 1) six and eight tenths _____
- 2) forty-two and sixty-one thousandths _____
- 3) seventy and twelve hundredths _____
- 4) five ten-thousandths _____
- 5) one thousand fifty-two and thirty one hundredths _____

What is the value of the underlined digit?:

- 6) 12,345 _____
- 7) 0.983 _____
- 8) 9.36 _____
- 9) 158.9 _____
- 10) 6.4 _____

Place Value Additional Practice

Match the number on the right with its name on the left.

- | | |
|---------------|---------------------------------------|
| ___ 1. 356 | a. three and six tenths |
| ___ 2. 3.5 | b. thirty and six tenths |
| ___ 3. 3.56 | c. three and five tenths |
| ___ 4. 30.56 | d. three and fifty-six hundredths |
| ___ 5. 3,560 | e. three dollars and fifty-six cents |
| ___ 6. \$3.56 | f. three hundred fifty-six |
| ___ 7. 30.6 | g. three thousand, five hundred sixty |
| ___ 8. 30.65 | h. thirty and fifty-six hundredths |
| ___ 9. 3.6 | i. thirty and sixty-five hundredths |

Answer the following questions using the numbers above.

- 1) Which number above has the greatest value? _____
- 2) Which number above as the lowest value? _____
- 3) Circle the number with the greatest value. 3.5 or 3.56

Rounding Decimals

Find your **place** and look **next door**.
5 or greater, add one more.

All digits in front, stay the same.
All digits behind, zero's the name.

Round 1.362 to the nearest hundredths.

1.362 → 1.360

6 is at the hundredths place.
We look next door and find the number 2.
2 is less than 5 and so 6 remains the same.

Round 25.378 to the nearest tenths.

25.378 → 25.400

3 is at the tenths place.
We look next door and find the number 7.
7 is more than 5 and so we increase 3 to 4.

You Try:

Round to the nearest whole number.

1) \$3.45 _____ 2) 324.56 _____ 3) \$1032.01 _____

Round to the nearest hundredth place.

1) \$23.456 _____ 2) 341.565 _____ 3) \$12.0111 _____

Rounding Practice

Round each number to the given place.

- 1) Round 4.75 to the nearest tenth.
- 2) Round 5.694 to the nearest hundredth.
- 3) Round 6.092 to the nearest tenth.
- 4) Round 8,6952 to the nearest thousandth.
- 5) Round 7.824 to the nearest tenth.
- 6) Round 4.726 to the nearest hundredth.
- 7) Round 3.502 to the nearest hundredth.
- 8) Round 9.2477 to the nearest thousandth.

Round to write each number in dollars and cents.

- 1) \$3.509 _____
- 2) \$12.7435 _____
- 3) \$5.917 _____
- 4) \$9.6 _____

Round to the nearest dollar.

- 1) \$24.532 _____
- 2) \$1039.8332 _____
- 3) \$54.19 _____
- 4) \$9.2 _____

Place Value and Rounding Practice

In the number 23.76

- 1) What is the value of the 7? _____
- 2) What is the value of the 3? _____
- 3) What is the value of the 6? _____

In the number 12.734

- 4) What is the value of the 2? _____
- 5) What is the value of the 7? _____
- 6) What is the value of the 4? _____

Round to the nearest tenth.

- 7) 2.17 _____
- 8) 21.642 _____
- 9) 5.019 _____
- 10) 17.092 _____

Round to the nearest hundredth.

- 11) 32.201 _____
- 12) 1.4776 _____
- 13) 39.807 _____
- 14) 7.698 _____

Use <, > or = to make each statement true.

- 15) 12.36 _____ 12.3
- 16) 1.234 _____ 123.4
- 17) 76,5 _____ 76.50
- 18) 1.4 _____ 1.4444...
- 19) 9.43 _____ 9.53
- 20) 8 _____ 8.0

Dividing Decimals

Dividing decimals is just like dividing any other number, but you have to make sure the decimal ends up in the right place in your answer.

Here are the basic steps for dividing decimals:

- 1) If necessary, make the divisor a _____ by moving the _____ all the way to the right.
- 2) Move the _____ in the dividend (the number under the "house") the same number of places that you moved it in the divisor. Add _____ if necessary.
- 3) Bring the _____ straight up. (Remember, in division the decimal is very _____ and it floats.)
- 4) Finish by simply, _____ as you normally would.

Examples:

$$1) 5 \overline{) 2.5}$$

$$2) 1.25 \overline{) 3.875}$$

You Try:

- 1) $2.32 \div 8 =$
- 2) $0.045 \div 0.09 =$
- 3) $16.75 \div 2.5 =$

4) Aleem has \$416.13 that he is going to give to his 3 friends Amanda, Jennifer and Audra. If he is giving each friend the same amount, how much will each person get?

5) How many quarters are in \$20?

Adding and Subtracting Decimals

Here are the basic steps for adding and subtracting decimals.

- 1) Always line up the decimal!
- 2) Fill in zeroes as placeholders at the end, especially if subtracting.
- 3) Add or Subtract
- 4) Bring the decimal down.
- 5) Check your work! Check whether your answer is reasonable by estimating.

Example:

1) $2.6 + 3.45 =$

2) $2.37 - 1.256 =$

You Try:

1) $16.75 + 5.091 =$

2) $312.55 - 16.2 =$

3) $29.1 - 0.68 =$

4) Savannah spent \$11.50 at the movies, and Quianna spent \$12.75. If they paid together, using a \$50 bill, how much change did they receive?

Multiplying Decimals

Here are the basic steps for multiplying decimals.

- 1) Multiply. (You do NOT need to line up the Decimal!)
- 2) Count the number of places behind the decimal in your problem. Your product must have the same number of places behind the decimal.

Example:

1) $3.67 \times 2.3 =$

2) $9 \cdot 0.54 =$

You Try:

1) $8.41 \times 0.5 =$

2) $2.13 (3.5) =$

3) $0.7 \cdot 0.8 =$

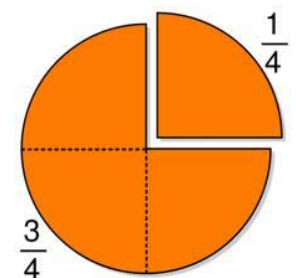
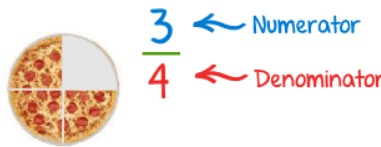
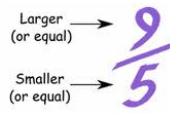

4) Hunter is building a ramp for his Tech Decks. The base will be a piece of wood that is 2.75 feet long and 2 feet wide. What is the area of the base? (Area of a rectangle = length x width.)

Operations with Decimals Practice

Answer bank:			
54.2241	107.133	16.760	38.7
31.011	88.56	29.927	45.168
0.35	51.6	43.608	0.109

- 1) $92 - 53.3 =$ _____ 2) $60.4 + 28.16 =$ _____
- 3) $19 + 88.133 =$ _____ 4) $5.45 \div 50 =$ _____
- 5) $78.38 - 34.772 =$ _____ 6) $8.256 \div 0.16 =$ _____
- 7) $9.41 \cdot 4.8 =$ _____ 8) $20.65 \div 59 =$ _____
- 9) $96.927 - 67 =$ _____ 10) $9.513 \cdot 5.7 =$ _____
- 11) $14.302 + 16.709 =$ _____ 12) $2 \cdot 8.38 =$ _____

Fractions Cheat Sheet

<p>A fraction is part of a whole.</p> 	<p>The <u>top</u> number of a fraction is called the <u>numerator</u>. The <u>bottom</u> number is the <u>denominator</u>.</p> 
<p>An <u>improper fraction</u> has a numerator that is <u>larger than or equal to</u> its denominator.</p> 	<p>A <u>mixed number</u> has a whole number <u>AND</u> a fraction.</p> 
<p>You can make any whole number into a fraction by <u>putting it over 1!</u></p> $5 = \frac{5}{1}$	<p>When the numerator and the denominator are the same, the fraction equals 1.</p> $\frac{5}{5} = 1$
<p>If the numerator > the denominator, the fraction's value is greater than 1.</p> $\frac{7}{4} > 1$ <p>If the denominator > the numerator, the fraction's value is less than 1.</p> $\frac{4}{7} < 1$	<p>The fraction bar shows division. The numerator is the dividend (the number in the "house") and the denominator is the divisor.</p> $\frac{4}{2} = 2 \overline{)4}$

Mixed Numbers to Improper Fractions

Converting mixed numbers to improper fractions:

Multiply the whole number by the denominator and add the numerator.

Keep the same denominator.

Then add.

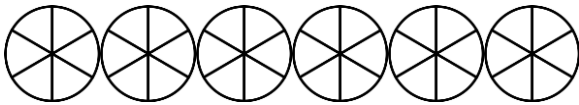
$$4 \frac{1}{3} = \frac{13}{3}$$

Multiply.

Example:

Convert $5\frac{1}{6}$ to an improper fraction.

First, shade $5\frac{1}{6}$ on the circles below:



Note that there are 31 pieces shaded. 5 wholes times the six pieces in each whole plus the one extra piece equals 31. That is the new numerator. You still need 6 pieces to make a whole, so the denominator remains 6.

$$\text{So, } 5\frac{1}{6} = \frac{31}{6}$$

You Try:

Convert the mixed numbers to improper fractions.

- | | | |
|-------------------|--------------------|---------------------|
| 1) $3\frac{1}{2}$ | 2) $2\frac{1}{3}$ | 3) $5\frac{2}{7}$ |
| 4) $1\frac{3}{7}$ | 5) $22\frac{2}{3}$ | 6) $12\frac{1}{12}$ |

Improper Fractions to Mixed Numbers

Converting improper fractions to mixed numbers:

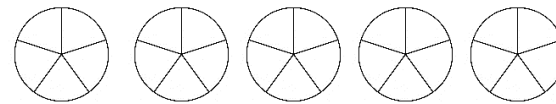
$$\frac{11}{5} \longrightarrow 2\frac{1}{5}$$

$$\begin{array}{r} 2 \\ 5 \overline{) 11} \\ \underline{-10} \\ 1 \end{array}$$

Example:

Convert $\frac{22}{5}$ to a mixed number.

First, shade in 22 pieces on the circles below:



Note that you should have filled 4 whole circles with 2 left over. That is because you need 5 pieces to make a whole and there are 4 complete groups of 5 in 22 with 2 left over.

$$\text{So, } \frac{22}{5} = 4\frac{2}{5}$$

You Try:

Convert the improper fractions to mixed numbers.

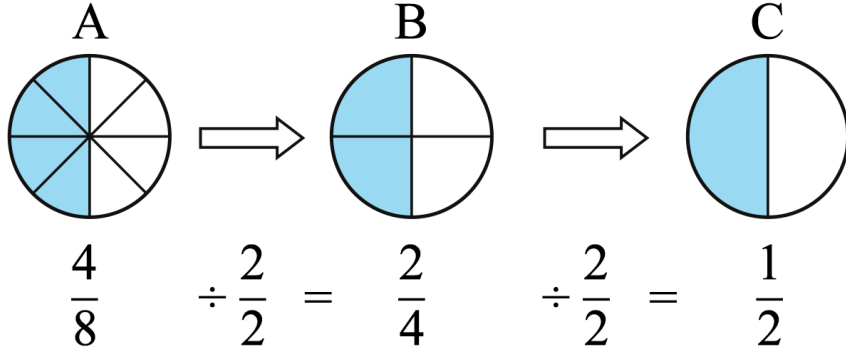
- | | | |
|-------------------|-------------------|-------------------|
| 1) $\frac{20}{7}$ | 2) $\frac{33}{4}$ | 3) $\frac{13}{2}$ |
| 4) $\frac{17}{3}$ | 5) $\frac{40}{8}$ | 6) $\frac{48}{7}$ |

Simplifying Fractions

To simplify fractions you need to find a common factor that is shared between the numerator and the denominator. Then divide the numerator and the denominator by that common factor. You know you are done when your numerator and denominator only share a factor of one.

Example:

Simplify $\frac{4}{8}$



You Try:

Simplify the fractions.

1) $\frac{5}{15} =$

2) $\frac{12}{24} =$

3) $\frac{6}{24} =$

4) $\frac{50}{70} =$

5) $\frac{21}{24} =$

6) $\frac{504}{522} =$

Adding and Subtracting Fractions

SAME DENOMINATORS	DIFFERENT DENOMINATORS
<p>STEPS</p> <ol style="list-style-type: none"> Write the problem vertically (if needed). Solve: add/subtract the numerators. The denominator stays the same. Simplify the answer (if needed). 	<p>STEPS</p> <ol style="list-style-type: none"> Write the problem vertically (if needed). Make common denominators. 2 ways: <ol style="list-style-type: none"> Find a common multiple. Multiply the denominators together and use their product as the new denominator. Solve: add/subtract the numerators. The denominator stays the same. Simplify the answer (if needed).
<p>Example: $\frac{2}{10} + \frac{3}{10} =$</p> $\begin{array}{r} \frac{2}{10} \\ + \frac{3}{10} \\ \hline \frac{5}{10} \end{array}$ <p>Cancel 5: $\frac{5}{10} = \frac{2}{5}$</p> <p>GCF = 5</p>	<p>Example: $\frac{5}{6} - \frac{2}{12} =$</p> $\begin{array}{r} \frac{5}{6} = \frac{5 \cdot 2}{6 \cdot 2} = \frac{10}{12} \\ - \frac{2}{12} \\ \hline \frac{8}{12} \end{array}$ <p>Cancel 4: $\frac{8}{12} = \frac{2}{3}$</p> <p>GCF = 4</p>
SUBTRACTION WITH UNGROUPING	<p>STEPS</p> <ol style="list-style-type: none"> Write the problem vertically (if needed). Make common denominators (if needed). Ungroup the mixed number by taking 1 from the whole number and making it a fraction. Use the denominator to determine what the fraction will be. <p>Ex) $2 \frac{4}{5} = 1 \frac{4}{5} + \frac{4}{5} = 1 \frac{8}{5}$</p> Solve: add/subtract the numerators. The denominator stays the same. Simplify the answer (if needed).

Adding Fractions Practice

Add. Simplify if possible.

1) $\frac{1}{8} + \frac{4}{8} =$	2) $\frac{1}{6} + \frac{2}{6} =$
3) Find the Least Common Multiple (LCM) of 3 & 4.	4) $\frac{1}{3} + \frac{1}{4} =$
5) $\frac{5}{8} + \frac{3}{10} =$	6) $\frac{1}{2} + \frac{3}{8} =$
7) $\frac{7}{12} + \frac{1}{6} =$	8) $\frac{1}{10} + \frac{1}{100} =$
9) $1\frac{1}{6} + 3\frac{4}{6} =$	10) $3\frac{5}{6} + 4\frac{2}{3} =$

Subtracting Fractions Practice

Subtract. Simplify if possible.

1) $\frac{2}{4} - \frac{1}{4} =$	2) $\frac{7}{6} - \frac{1}{6} =$
3) Find the Least Common Multiple (LCM) of 6 & 8.	4) $\frac{5}{6} - \frac{5}{8} =$
5) $\frac{3}{4} - \frac{1}{6} =$	6) $\frac{1}{3} - \frac{2}{15} =$
7) $\frac{8}{15} - \frac{2}{5} =$	8) $\frac{11}{12} - \frac{5}{6} =$
9) $3\frac{4}{7} - 2\frac{1}{7} =$	10) $3 - \frac{2}{3} =$

Mixed Adding & Subtracting Fractions Practice

Add or Subtract. Simplify if possible.

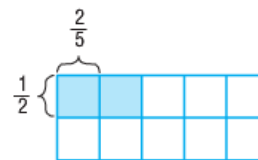
1) $\frac{5}{10} + \frac{3}{10} =$	2) $\frac{7}{9} - \frac{4}{9} =$
3) $\frac{5}{12} + \frac{3}{4} =$	4) $\frac{5}{6} - \frac{3}{4} =$
5) $\frac{7}{10} + \frac{3}{4} =$	6) $\frac{7}{9} - \frac{1}{2} =$
7) $4\frac{1}{2} + 3\frac{2}{2} =$	8) $2\frac{8}{9} - 1\frac{1}{9} =$
9) $20\frac{1}{2} + 12\frac{3}{7} =$	10) $9\frac{3}{4} - 6\frac{1}{3} =$

Review of Multiplying Fractions

Multiply Fractions

Words Multiply the numerators and multiply the denominators.

Models



Numbers $\frac{2}{5} \times \frac{1}{2} = \frac{2 \times 1}{5 \times 2}$

Symbols $\frac{a}{b} \times \frac{c}{d} = \frac{a \times c}{b \times d}$, where b and d are not 0.

Don't forget that if you **simplify before you multiply** you won't have to simplify your answer and you will work with simpler numbers.

Example:

$$\frac{7}{\cancel{6}_2} \times \frac{\cancel{3}^1}{9} = \frac{7}{18}$$

You Try:

1) $\frac{1}{2} \cdot \frac{3}{5} =$

2) $\frac{1}{3} \cdot \frac{3}{4} =$

3) $\frac{2}{3} \cdot \frac{5}{6} =$

4) $\frac{12}{4} \cdot \frac{7}{3} =$

5) $1\frac{1}{5} \cdot \frac{20}{3} =$

6) $\frac{5}{6} \cdot 2 =$

Dividing Fractions Using Models

Step 1 Create a common denominator.

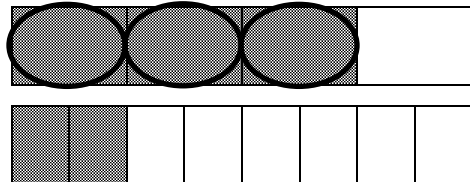
Step 2 Draw a picture to represent the first fraction or mixed number.

Step 3 Circle groups of pieces. The second fraction's numerator tells us how many pieces should be in each group.

Step 4 Your answer is how many groups you have circled.

Example:

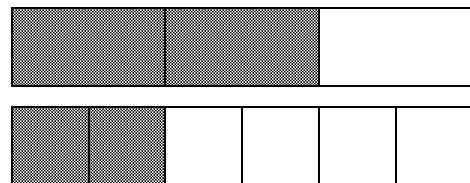
Divide $\frac{3}{4} \div \frac{2}{8} = \frac{3}{4} \div \frac{1}{4}$



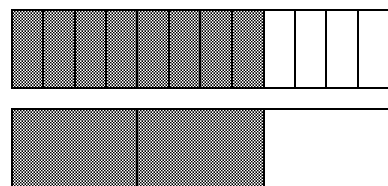
$\frac{3}{4} \div \frac{1}{4} = 3$

You Try:

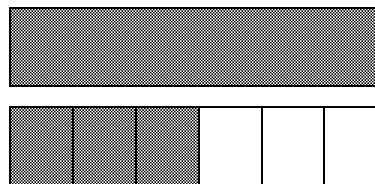
1) $\frac{2}{3} \div \frac{2}{6} =$



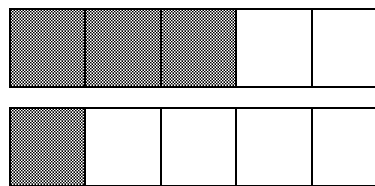
2) $\frac{8}{12} \div \frac{2}{3} =$



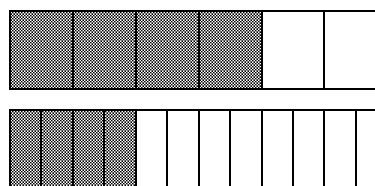
3) $1 \div \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$



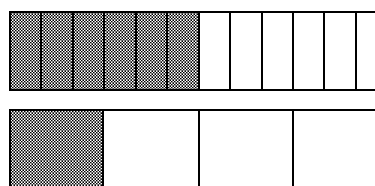
4) $\frac{3}{5} \div \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$



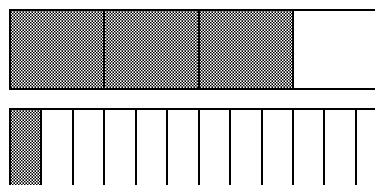
5) $\underline{\hspace{1cm}} \div \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$



6) $\underline{\hspace{1cm}} \div \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$



7) $\underline{\hspace{1cm}} \div \underline{\hspace{1cm}} = \underline{\hspace{1cm}}$



Dividing Fractions Using Common Denominators

Step 1 Find a common denominator and convert each fraction to have that denominator.

Step 2 Divide straight across.

Step 3 Simplify your new fraction.

Example:

Step 1 $\frac{4}{5} \div \frac{2}{3} = \frac{12}{15} \div \frac{10}{15}$

Step 2 $\frac{12}{15} \div \frac{10}{15} = \frac{12 \div 10}{1}$

Step 3 $\frac{12 \div 10}{1} = 12 \div 10 = 1\frac{1}{5}$

You Try:

1) $\frac{5}{7} \div \frac{1}{7} =$

2) $\frac{3}{8} \div \frac{1}{4} =$

3) $\frac{4}{6} \div \frac{1}{3} =$

4) $1\frac{5}{9} \div \frac{7}{18} =$

5) $6 \div 3\frac{1}{3} =$

6) $10\frac{3}{2} \div 6\frac{1}{2} =$

Reciprocals

A reciprocal is one of two numbers whose product is 1. It is the result of "flipping" a fraction.

Example:

Find the reciprocal.

1) $\frac{3}{4}$ the reciprocal is $\frac{4}{3}$

2) 2 the reciprocal is $\frac{1}{2}$

3) $4\frac{1}{5} = \frac{21}{5}$ the reciprocal is $\frac{5}{21}$

You Try:

Find the reciprocal

1) $\frac{2}{3}$

2) $\frac{3}{13}$

3) $\frac{9}{10}$

4) $4\frac{3}{8}$

5) 5

6) $7\frac{5}{9}$

7) 2

8) $10\frac{2}{19}$

9) $3\frac{2}{3}$

Dividing Fractions Using an Algorithm

K – Keep the first fraction (Make sure you change all mixed numbers to improper fractions first.)

C – Change the problem from division to multiplication.

F – Flip the second fraction (change it to its reciprocal)

Example:

K (Keep)	C (Change)	F (Flip)
$\frac{4}{5} \div \frac{2}{3}$	$\frac{4}{5} \times \frac{2}{3} =$	$\frac{4}{5} \cdot \frac{3}{2} =$

You Try:

1) $\frac{5}{8} \div \frac{2}{3} =$	2) $\frac{3}{10} \div \frac{1}{2} =$	3) $\frac{9}{10} \div \frac{1}{4} =$
4) $\frac{3}{8} \div 9 =$	5) $\frac{10}{11} \div \frac{5}{6} =$	6) $\frac{5}{9} \div \frac{13}{9} =$
7) $1\frac{3}{4} \div \frac{7}{8} =$	8) $3 \div 1\frac{1}{8} =$	9) $3\frac{2}{3} \div 2\frac{2}{3} =$

Dividing Fractions Practice

Divide. Use any of the methods we have learned to find the quotient. Answer as a mixed number if possible.

1) $\frac{7}{2} \div \frac{10}{4} =$	2) $\frac{1}{3} \div \frac{1}{2} =$	3) $\frac{2}{4} \div \frac{1}{3} =$
4) $\frac{25}{3} \div \frac{14}{4} =$	5) $\frac{2}{4} \div \frac{1}{2} =$	6) $4\frac{1}{2} \div 2\frac{2}{3} =$
7) $7\frac{2}{4} \div \frac{5}{8} =$	8) $4\frac{1}{2} \div 3\frac{2}{3} =$	9) $1\frac{2}{3} \div \frac{27}{4} =$
10) $\frac{17}{5} \div \frac{13}{4} =$	11) $\frac{4}{5} \div 1\frac{2}{3} =$	12) $\frac{18}{5} \div 4\frac{1}{2} =$