

# Unit 8

## Operations with Rational Numbers

Adding Rational Numbers

Subtracting Rational Numbers



Multiplying/Dividing Rational Numbers

Converting Fractions & Decimals

Name: \_\_\_\_\_

Math Teacher: \_\_\_\_\_

### Math 6/7 Unit 8 Calendar

| 2/10   | 2/11            | 2/12                               | 2/13                               | 2/14   |
|--|-----------------|------------------------------------|------------------------------------|--|
| Unit 8 Pre-test<br>Coin<br>Counters<br>Addition Intro  | Computer<br>Lab | Adding<br>Rational<br>Numbers      | Adding<br>Rational<br>Numbers      | Adding<br>Rational<br>Numbers &<br>Quiz      |
| IXL Skills Week of 2/25: N1, N2, N7  |                 |                                    |                                    |  |
| 2/17   | 2/18            | 2/19                               | 2/20                               | 2/21   |
|  <b>Winter Break!</b>  |                 |                                    |                                    |  |
| 2/24   | 2/25            | 2/26                               | 2/27                               | 2/28   |
| Subtracting<br>Rational<br>Numbers   | Computer<br>Lab | Subtracting<br>Rational<br>Numbers | Subtracting<br>Rational<br>Numbers | Subtracting<br>Rational<br>Numbers &<br>Quiz |
| IXL Skills Week of 3/4: N3, N4, N5, N6, P5   |                 |                                    |                                    |  |
| 3/2  | 3/3             | 3/4                                | 3/5                                | 3/6  |
| Multiplying &<br>Dividing<br>Rational<br>Numbers   | Computer<br>Lab | Review                             | Review                             | Unit 8 Test                                  |
| IXL Skills Week of 3/11: N8, N9, N10, N11, P6  |                 |                                    |                                    |  |

# Unit 8: Operations with Rational Numbers

## Standards, Checklist and Circle Map

### Georgia Standards of Excellence (GSE):

**MGSE7.NS.1a:** Describe situations in which opposite quantities combine to make 0.

**MGSE7.NS.1b:** Understand  $p + q$  as the number located a distance  $|q|$  from  $p$ , in the positive or negative direction depending on whether  $q$  is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.

**MGSE7.NS.1c:** Understand subtraction of rational numbers as adding the additive inverse,  $p - q = p + (-q)$ . Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.

**MGSE7.NS.1d:** Apply properties of operations as strategies to add and subtract rational numbers.

**MGSE7.NS.2a:** Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as  $(-1)(-1) = 1$  and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.

**MGSE7.NS.2b:** Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If  $p$  and  $q$  are integers, then  $-(p/q) = (-p)/q = p/(-q)$ . Interpret quotients of rational numbers by describing real-world contexts

**MGSE7.NS.2c:** Apply properties of operations as strategies to multiply and divide rational numbers.

**MGSE7.NS.2d:** Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats.

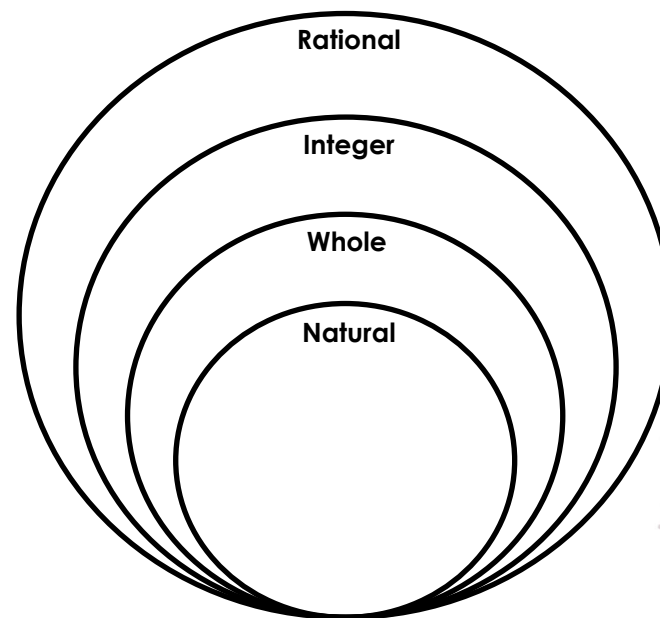
**MGSE7.NS.3:** Solve real-world mathematical problems involving the four operations with rational numbers.

**What Will I Need to Learn??** Mark a check next to each concept as you master them.

- \_\_\_\_\_ I can show integer addition and subtraction on a number line
- \_\_\_\_\_ I can understand that the sum of opposites is zero
- \_\_\_\_\_ I can add and subtract integers, including in real-life situations
- \_\_\_\_\_ I understand that subtracting is the same as adding the inverse
- \_\_\_\_\_ I can multiply integers
- \_\_\_\_\_ I can divide integers
- \_\_\_\_\_ I can convert fractions (rational numbers) to decimals
- \_\_\_\_\_ I can solve problems with rational numbers



| Vocabulary Term     | What does it mean? Definition  | What does it look like? Picture/Example |
|---------------------|--|---|
| Repeating decimal   | A decimal that repeats the same digits infinitely  |   |
| Terminating decimal | A decimal that stops at a certain place value  |   |
| Positive number     | A number greater than zero   |   |
| Negative number     | A number less than zero  |   |
| Zero Pair           | A pair of numbers whose sum is zero  |   |
| Natural numbers     | "Counting numbers" from one to infinity  |   |
| Whole numbers       | "Counting numbers" from zero to infinity (all natural numbers and zero)                            |   |
| Integers            | Whole numbers and their opposites  |   |
| Rational numbers    | A real number that can be written as an integer, a fraction, or a repeating or terminating decimal |   |



# Unit 8 End of Unit Study Guide

## Knowledge and Understanding

- 1) What is the algorithm for adding with negative numbers?
- 2) a) What is the sum of two numbers that are the same distance from zero on the number line?  
  
b) What are they called?
- 3) Model the problem  $-6 - 2$  using + and - counters:

## Proficiency of Skills

- 4)  $10 - (-7) = \underline{\hspace{2cm}}$
- 5)  $(2)(12)(-5) = \underline{\hspace{2cm}}$
- 6)  $(-150) \div (-15) = \underline{\hspace{2cm}}$
- 7)  $(8.1) + (-1) + (-7.1) = \underline{\hspace{2cm}}$
- 8)  $(-1.3) - (-4.3) = \underline{\hspace{2cm}}$
- 9)  $(-5)(2 - 8) = \underline{\hspace{2cm}}$
- 10) Convert  $\frac{2}{9}$  to a decimal:  $\underline{\hspace{2cm}}$
- 11) Convert 1.08 to a fraction:  $\underline{\hspace{2cm}}$

## Application

- 12) Order from least to greatest:  $-\frac{1}{4}$ ,  $-\frac{6}{8}$ ,  $1\frac{4}{5}$ ,  $-0.5$ ,  $1.4$
- 13) If  $b$  represents a negative number, is  $b \cdot b$  a positive or negative number?

14) A submarine 530 feet below sea level descends an additional 100 feet before ascending 120 feet. What is the location of the submarine?

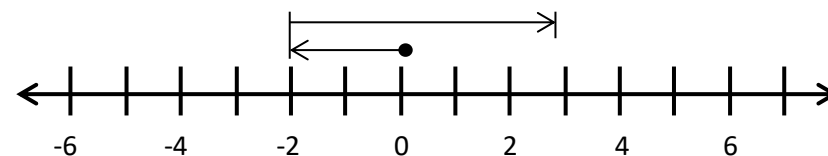
- a) 750 ft below sea level      b) 550 ft below sea level  
c) 510 ft below sea level      d) 510 ft above sea level

15) Name two integers have a product of -30 and a sum of -7.

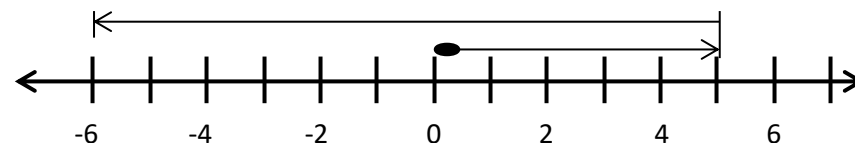
16) The temperature at 9 AM was  $11^{\circ}\text{F}$ . The temperature dropped 4 degrees per hour for the next three hours. What is the temperature at noon?

- a)  $-3^{\circ}\text{F}$       b)  $-7^{\circ}\text{F}$       c)  $-1^{\circ}\text{F}$       d)  $-2^{\circ}\text{F}$

17) What addition expression is represented by the model below?



18) What subtraction expression is represented by the model below?



19) When the following fractions are converted to decimals, which one will result in a repeating decimal?

- A.  $\frac{7}{10}$       B.  $\frac{5}{12}$       C.  $\frac{5}{8}$       D.  $\frac{3}{5}$

20) For your birthday, you decide to go parasailing over the ocean. You're peacefully sailing at 120 feet above sea level, and then you ascend 25 feet. Finally, you decide to dive into the ocean, and you fall 165 feet. Describe your new location. Justify your answer with an illustration, an equation, and/or complete sentences.

Solve for x in each equation below. SHOW ALL STEPS:

21.  $x - 4.23 = -9.05$

22.  $-8x = -60$

23.  $x + 4 = -9 \frac{1}{4}$

24.  $\frac{x}{-5} = -10$

25.  $3 \frac{1}{2}x = -70$

26.  $x + 8 = -42$

27. Fill in the table:

| <u>Fraction</u>                     | <u>Decimal</u> | <u>Percent</u> |
|-------------------------------------|----------------|----------------|
| <b>3 <math>\frac{1}{4}</math></b>   |                |                |
|                                     | <b>0.33</b>    |                |
| <b>- <math>\frac{1}{8}</math></b>   |                |                |
| <b><math>\frac{5}{6}</math></b>     |                |                |
|                                     | <b>-5.375</b>  |                |
|                                     | <b>16.4</b>    |                |
| <b>-8 <math>\frac{3}{11}</math></b> |                |                |

# Adding/Subtracting Fraction Review

## Adding Fractions with Like Denominators

Add the numerators.  
Denominator is unchanged.

$$\frac{1}{7} + \frac{3}{7} = \frac{1+3}{7} = \frac{4}{7}$$

## Adding Fractions with Unlike Denominators

$$\frac{1}{8} + \frac{2}{3}$$

Rewrite with common denominator

$$3 \times \frac{1}{8} + \frac{2 \times 3}{3 \times 8} = \frac{3}{24} + \frac{6}{24}$$

Add the numerators

$$\frac{3}{24} + \frac{6}{24} = \frac{9}{24}$$

## Subtraction Fractions with UNLIKE denominators

$$\frac{5}{6} - \frac{3}{9} =$$

1. Find the LCM of the denominators. This is your new denominator.

Multiples of 6 = 6, 12, 18  
Multiples of 9 = 9, 18, 27

LCM = 18

2. Rewrite the problem using the LCM.

$$\frac{5 \times 3}{6 \times 3} - \frac{3 \times 2}{9 \times 2} = \frac{15}{18} - \frac{6}{18}$$

Whatever you do to the numerator you must do to the denominator.

3. Subtract the numerators. The denominator stays the same.

$$\frac{15}{18} - \frac{6}{18} = \frac{9}{18}$$

4. Simplify

$$\frac{9 \div 9}{18 \div 9} = \frac{1}{2}$$

Divide by the Greatest Common Factor.

Math  
Fractions

## Adding Fractions with the same denominator

Write the sum of each fraction below. Remember: when adding fractions with the same denominator, simply add the numerators and keep the denominator the same.

$$\frac{3}{5} + \frac{1}{5} = \frac{4}{5}$$

numerator  
denominator



$$\frac{5}{5} + \frac{8}{5} = \boxed{\phantom{000}} \quad \frac{3}{7} + \frac{1}{7} = \boxed{\phantom{000}}$$

$$\frac{6}{3} + \frac{4}{3} = \boxed{\phantom{000}} \quad \frac{7}{4} + \frac{8}{4} = \boxed{\phantom{000}}$$

$$\frac{11}{9} + \frac{5}{9} = \boxed{\phantom{000}} \quad \frac{9}{8} + \frac{9}{8} = \boxed{\phantom{000}}$$

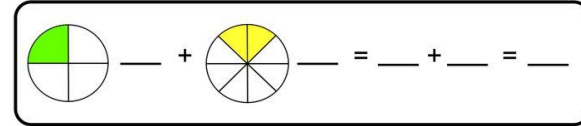
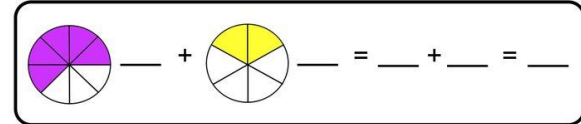
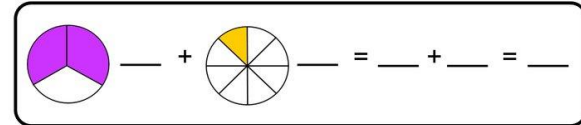
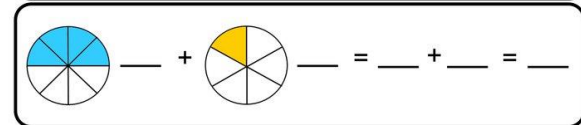
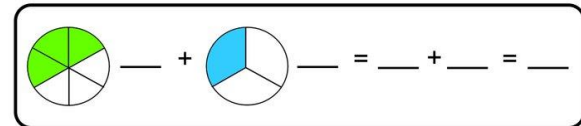
$$\frac{10}{12} + \frac{12}{12} = \boxed{\phantom{000}} \quad \frac{17}{22} + \frac{3}{22} = \boxed{\phantom{000}}$$

$$\frac{22}{50} + \frac{15}{50} + \frac{17}{50} = \boxed{\phantom{000}}$$

$$\frac{35}{100} + \frac{6}{100} + \frac{79}{100} + \frac{14}{100} = \boxed{\phantom{000}}$$



Directions: Write the fraction for each diagram. Then, add the fractions. Make sure the denominators are the same.



# Why Did Airhead Eat the Dollar He Brought to School?



Do each exercise and find your answer at the bottom of the page. Write the letter of the exercise in the box above the answer.

|                                 |                                 |                                  |                                   |                                  |                                  |
|---------------------------------|---------------------------------|----------------------------------|-----------------------------------|----------------------------------|----------------------------------|
| (S) $\frac{1}{2} + \frac{1}{3}$ | (O) $\frac{2}{5} + \frac{1}{2}$ | (T) $\frac{1}{2} + \frac{1}{4}$  | (L) $\frac{1}{3} + \frac{4}{9}$   | (Y) $\frac{1}{5} + \frac{2}{3}$  | (U) $\frac{5}{8} + \frac{1}{4}$  |
| (A) $\frac{1}{3} + \frac{5}{6}$ | (H) $\frac{1}{2} + \frac{7}{8}$ | (I) $\frac{3}{4} + \frac{2}{3}$  | (S) $\frac{7}{16} + \frac{9}{16}$ | (N) $\frac{1}{6} + \frac{4}{9}$  | (W) $\frac{1}{4} + \frac{4}{5}$  |
| (C) $\frac{1}{8} + \frac{2}{3}$ | (H) $\frac{1}{2} + \frac{1}{6}$ | (E) $\frac{3}{10} + \frac{1}{2}$ | (L) $\frac{4}{15} + \frac{1}{3}$  | (M) $\frac{3}{4} + \frac{7}{12}$ | (N) $\frac{5}{6} + \frac{3}{10}$ |
| $\frac{1}{12}$                  | $\frac{13}{18}$                 | $\frac{1}{6}$                    | $\frac{7}{9}$                     | $\frac{1}{8}$                    | $\frac{1}{3}$                    |
| $\frac{17}{40}$                 | $\frac{1}{6} + \frac{7}{18}$    | $\frac{3}{16}$                   | $\frac{3}{8} + \frac{1}{28}$      | $\frac{1}{2} + \frac{1}{20}$     | $\frac{5}{6} + \frac{2}{3}$      |
| $\frac{11}{18}$                 | $\frac{7}{18} + \frac{3}{5}$    | $\frac{3}{16}$                   | $\frac{1}{28} + \frac{11}{100}$   | $\frac{1}{2} + \frac{13}{36}$    | $\frac{1}{15} + \frac{1}{12}$    |
| $\frac{19}{36}$                 | $\frac{11}{12} + \frac{23}{24}$ | $\frac{7}{40}$                   | $\frac{1}{6} + \frac{11}{18}$     | $\frac{1}{4} + \frac{11}{18}$    | $\frac{5}{8} + \frac{11}{10}$    |
| $\frac{11}{12}$                 | $\frac{1}{15} + \frac{11}{24}$  | $\frac{7}{24}$                   | $\frac{1}{6} + \frac{11}{18}$     | $\frac{5}{8} + \frac{19}{36}$    | $\frac{11}{12} + \frac{2}{5}$    |
| $\frac{1}{4}$                   | $\frac{13}{18}$                 | $\frac{2}{3}$                    | $\frac{1}{9}$                     | $\frac{1}{8}$                    | $\frac{1}{3}$                    |
| $\frac{5}{12}$                  | $\frac{1}{6} + \frac{5}{6}$     | $\frac{7}{9}$                    | $\frac{3}{5}$                     | $\frac{7}{8}$                    | $\frac{19}{24}$                  |
| $\frac{3}{4}$                   | $\frac{1}{6} + \frac{5}{6}$     | $\frac{2}{3}$                    | $\frac{1}{5}$                     | $\frac{2}{8}$                    | $\frac{11}{18}$                  |
| $\frac{13}{18}$                 | $\frac{1}{6} + \frac{5}{6}$     | $\frac{7}{9}$                    | $\frac{1}{5}$                     | $\frac{2}{8}$                    | $\frac{4}{5}$                    |
| $\frac{5}{12}$                  | $\frac{1}{6} + \frac{5}{6}$     | $\frac{2}{3}$                    | $\frac{1}{5}$                     | $\frac{2}{8}$                    | $\frac{13}{15}$                  |

# LAST LINE

A careless zookeeper named Blake  
Fell into a tropical lake  
Said a fat alligator  
A few moments later ...



$$\frac{17}{40} - \frac{11}{18} = \frac{1}{6} - \frac{7}{18} = \frac{3}{16} - \frac{3}{16} = \frac{1}{16}$$

$$\frac{19}{36} - \frac{11}{12} = \frac{19}{36} - \frac{33}{36} = -\frac{14}{36} = -\frac{7}{18}$$

To decode the last line of this limerick: Do each exercise below and find your answer in the code. Each time the answer appears, write the letter of the exercise above it.

(D)  $\frac{7}{8} - \frac{1}{2}$

(Y)  $\frac{1}{2} - \frac{3}{5}$

(E)  $\frac{5}{6} - \frac{2}{9}$

(U)  $\frac{67}{100} - \frac{3}{10}$

(P)  $\frac{3}{4} - \frac{1}{6}$

(B)  $\frac{9}{10} - \frac{2}{5}$

(U)  $\frac{67}{100} - \frac{3}{10}$

(L)  $\frac{5}{6} - \frac{3}{8}$

(B)  $\frac{9}{10} - \frac{2}{5}$

(F)  $\frac{7}{12} - \frac{1}{3}$

(V)  $\frac{4}{5} - \frac{3}{8}$

(L)  $\frac{5}{6} - \frac{3}{8}$

(A)  $\frac{19}{20} - \frac{11}{20}$

(S)  $\frac{7}{9} - \frac{1}{4}$

(K)  $\frac{5}{8} + \left(\frac{2}{3} - \frac{1}{4}\right)$

(O)  $\frac{16}{16} - \left(\frac{3}{4} + \frac{1}{16}\right)$

(G)  $\left(\frac{2}{5} + \frac{1}{2}\right) - \frac{3}{10}$

(R) Razzle Shoes bought a  $\frac{1}{2}$ -page ad in the Times. Dazzle Shoes bought two ads that were  $\frac{1}{6}$  page each. How much more advertising did Razzle Shoes buy?

(K)  $\frac{5}{8} + \left(\frac{2}{3} - \frac{1}{4}\right)$

(T) Jill made a sauce in cooking class. She used  $\frac{1}{2}$  cup of milk,  $\frac{2}{3}$  cup of cream, and  $\frac{1}{4}$  cup of water. How much less water was used than milk and cream combined?

# Subtracting Fractions Practice

# Adding Integers

Adding the SAME Sign

Adding DIFFERENT Signs

# Adding Rational Numbers

To add rational numbers with the same sign, add their absolute values.

The sum is:

- positive if both integers are positive.
- negative if both integers are negative.

To add rational numbers with different signs, subtract their absolute values.

The sum is:

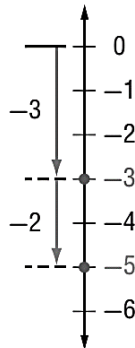
- positive if the positive integer's absolute value is greater.
- negative if the negative integer's absolute value is greater.
- **Remember:** What do you have more of, positives or negatives, and how many more do you have?

## Examples:

### 1. Find $-3 + (-2)$ .

Start at 0. Move 3 units down to show  $-3$ .

From there, move 2 units down to show  $-2$ .

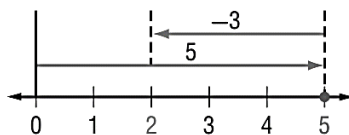


So,  $-3 + (-2) = -5$ .

### 2. Find $-26 + (-17)$ .

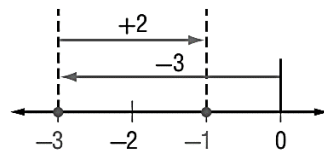
$$-26 + (-17) = -43$$

### 3. Find $5 + (-3)$ .



So,  $5 + (-3) = 2$ .

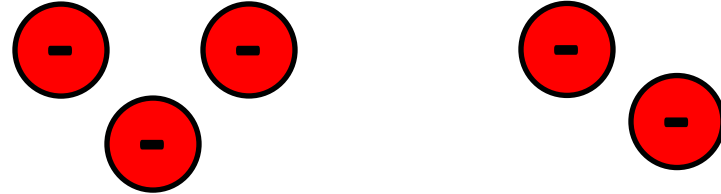
### 4. Find $-3 + 2$ .



So,  $-3 + 2 = -1$ .

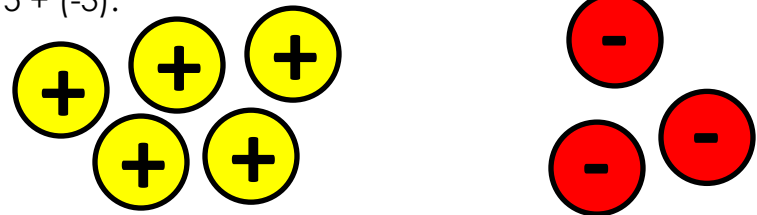
Find the sum using two-color counters.

Find  $-3 + (-2)$ .

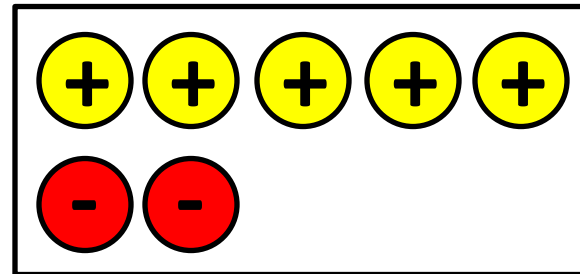


Three negatives ( $-3$ ) plus another two negatives ( $-2$ ) gives you five negatives ( $-5$ ).

Find  $5 + (-3)$ .

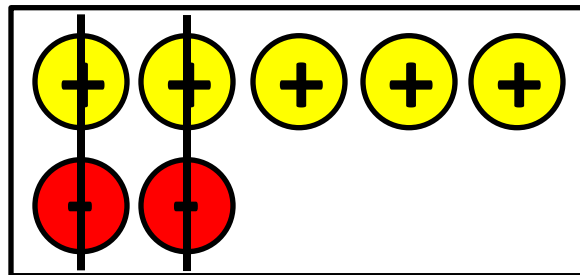


First, match up your zero pairs.



\*\*Remember that the sum of a number and its opposite is always 0. A number and its opposite are zero pairs.\*\*

Then cross out your zero pairs.



There are three positives left so,  $5 + (-2) = 3$ .



# Adding Integers with Models

| Problem         | Sum | With Counters | Number Line |
|-----------------|-----|---------------|-------------|
| 1) $3 + (-5) =$ |     |               |             |
| 2) $2 + (-8) =$ |     |               |             |
| 3) $4 + (-4) =$ |     |               |             |
| 4) $(-7) + 4 =$ |     |               |             |
| 5) $(-6) + 5 =$ |     |               |             |

What is the algorithm (rule) for adding integers with DIFFERENT signs?

| Problem        | Sum | With Counters | Number Line |
|----------------|-----|---------------|-------------|
| 1) $-5 + -2 =$ |     |               |             |
| 2) $-2 + -3 =$ |     |               |             |
| 3) $-2 + -4 =$ |     |               |             |
| 4) $7 + 4 =$   |     |               |             |
| 5) $-2 + -3 =$ |     |               |             |

What is the algorithm (rule) for adding integers with the SAME signs?

## You Try:

Use (+) and (-) counters or a number line to find the sum.

- 1)  $-5 + (-2)$       2)  $8 + 1$       3)  $-7 + 10$   
 4)  $16 + (-11)$       5)  $-22 + (-7)$       6)  $-50 + 50$   
 7)  $-10 + (-10)$       8)  $100 + (-25)$       9)  $-35 + (-20)$

Use any method to find the sum.

- 10)  $-7 + (-3) + 10$       11)  $-42 + 36 + (-36)$       12)  $-17 + 17 + 9$   
 13)  $5 + (-8)$       14)  $-3 + 3$       15)  $-3 + (-8)$   
 16)  $-7 + (-7)$       17)  $-8 + 10$       18)  $-7 + 13$

19)  $\frac{5}{8} + \frac{1}{8}$       20)  $-\frac{1}{4} + \frac{3}{4}$       21)  $-\frac{7}{15} + (-\frac{4}{15})$

22)  $-1.4 + (-1.3)$       23)  $1.4 + (-2.7)$       24)  $-28 + 1.6$

25)  $5 + 11 + (-5)$       26)  $7 + (-5) + 5$       27)  $9 + (-9) + 10$

Write an addition expression to describe each situation. Then find each sum.

28) **HAWK** A hawk is in a tree 100 feet above the ground. It flies down to the ground.

29) **RUNNING** Leah ran 6 blocks north then back 4 blocks south.

# More Adding Rational Numbers

If  $a = -3$ ,  $b = -5$  and  $c = 5$ , find the sum.

1)  $c + b$

2)  $a + |b|$

3)  $|a + b|$

4)  $a + b + c$

5)  $a + |c + b|$

6)  $a + c$

If  $x = -10$ ,  $y = 2$  and  $z = -1$ , find the sum.

7)  $x + z$

8)  $|z| + x$

9)  $|x + y + z|$

10)  $z + y$

11)  $x + y$

12)  $|x + y| + z$

Write an addition expression to describe each situation. Then find each sum.

13) **FOOTBALL** A team gains 20 yards. Then they lose 7 yards.

14) **MONEY** Roger owes his mom \$5. He borrows another \$6 from her.

15) **HOT AIR BALLOON** A balloon rises 340 feet into the air. Then it descends 130 feet.

16) **CYCLING** A cyclist travels downhill for 125 feet. Then she travels up a hill 50 feet.

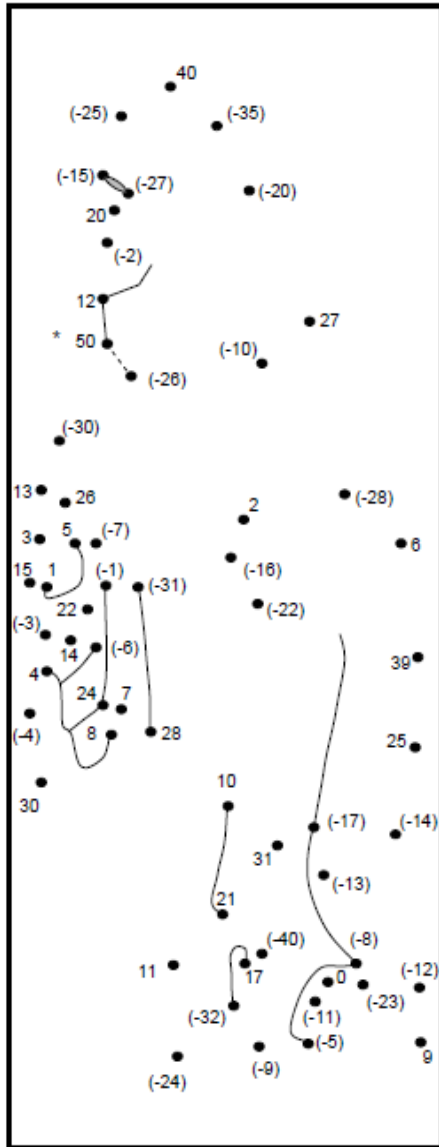
## ADDING INTEGERS

NAME:

ANSWER THE PROBLEMS BELOW AND CONNECT THE DOTS IN THE ORDER YOU CREATED.  
I STARTED THE PATTERN FOR YOU...NOW YOU DO THE REST.  
NOTE: PATTERNS ARE NOT CONNECTED TOGETHER

- PATTERN #1
- $$41 + 9 = \underline{50}$$
- $$(-9) + (-17) = \underline{(-26)}$$
- $$(-20) + (-11) = \underline{\quad}$$
- $$(-5) + 4 = \underline{\quad}$$
- $$(-14) + 7 = \underline{\quad}$$
- $$(-3) + 8 = \underline{\quad}$$
- $$13 + 13 = \underline{\quad}$$
- $$(-14) + (-16) = \underline{\quad}$$
- $$(-7) + 20 = \underline{\quad}$$
- $$(-4) + 7 = \underline{\quad}$$
- $$(-2) + 3 = \underline{\quad}$$
- $$21 + (-6) = \underline{\quad}$$
- $$5 + (-9) = \underline{\quad}$$
- $$17 + 13 = \underline{\quad}$$
- $$(-4) + 8 = \underline{\quad}$$
- $$0 + (-3) = \underline{\quad}$$
- $$5 + 9 = \underline{\quad}$$
- $$11 + 11 = \underline{\quad}$$
- $$(-14) + 8 = \underline{\quad}$$
- $$12 + 12 = \underline{\quad}$$
- $$11 + (-3) = \underline{\quad}$$
- $$3 + 4 = \underline{\quad}$$
- $$11 + 17 = \underline{\quad}$$
- $$0 + 11 = \underline{\quad}$$
- $$(-10) + (-14) = \underline{\quad}$$
- $$5 + (-14) = \underline{\quad}$$
- $$(-20) + (-20) = \underline{\quad}$$
- $$(-3) + 20 = \underline{\quad}$$
- $$(-10) + (-22) = \underline{\quad}$$
- $$2 + 19 = \underline{\quad}$$

LINE ENDS



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- PATTERN #2
- $$(-18) + 8 = \underline{\quad}$$
- $$(-3) + 5 = \underline{\quad}$$
- $$(-10) + (-6) = \underline{\quad}$$
- $$(-11) + (-11) = \underline{\quad}$$
- $$6 + 4 = \underline{\quad}$$
- $$33 + (-2) = \underline{\quad}$$
- $$1 + (-18) = \underline{\quad}$$
- $$(-18) + 5 = \underline{\quad}$$
- $$(-8) + 0 = \underline{\quad}$$
- $$2 + (-25) = \underline{\quad}$$
- $$2 + (-2) = \underline{\quad}$$
- $$(-9) + (-2) = \underline{\quad}$$
- $$(-3) + (-2) = \underline{\quad}$$
- $$6 + 3 = \underline{\quad}$$
- $$(-20) + 8 = \underline{\quad}$$
- $$(-3) + (-11) = \underline{\quad}$$
- $$35 + (-10) = \underline{\quad}$$
- $$20 + 19 = \underline{\quad}$$
- $$3 + 3 = \underline{\quad}$$
- $$(-19) + (-9) = \underline{\quad}$$
- $$6 + 21 = \underline{\quad}$$
- $$(-4) + (-16) = \underline{\quad}$$
- $$(-30) + (-5) = \underline{\quad}$$
- $$20 + 20 = \underline{\quad}$$
- $$25 + (-50) = \underline{\quad}$$
- $$(-5) + (-10) = \underline{\quad}$$
- $$(-5) + (-22) = \underline{\quad}$$
- $$9 + 11 = \underline{\quad}$$
- $$3 + (-5) = \underline{\quad}$$
- $$8 + 4 = \underline{\quad}$$

LINE ENDS

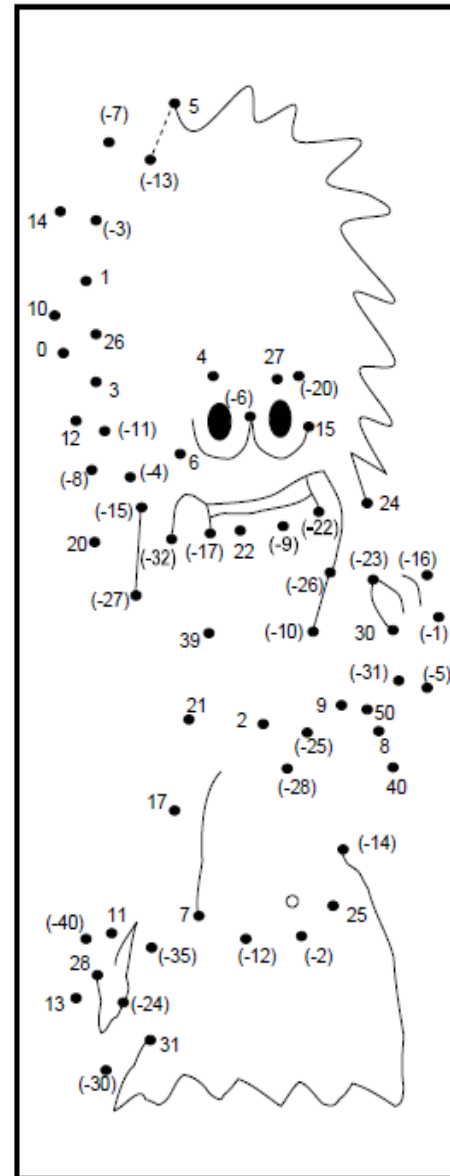
## ADDING INTEGERS

NAME:

ANSWER THE PROBLEMS BELOW AND CONNECT THE DOTS IN THE ORDER YOU CREATED.  
I STARTED THE PATTERN FOR YOU...NOW YOU DO THE REST.  
NOTE: PATTERNS ARE NOT CONNECTED TOGETHER

- PATTERN #1
- $$(-3) + 8 = \underline{5}$$
- $$(-18) + 5 = \underline{-13}$$
- $$(-14) + 7 = \underline{\quad}$$
- $$0 + (-3) = \underline{\quad}$$
- $$5 + 9 = \underline{\quad}$$
- $$(-2) + 3 = \underline{\quad}$$
- $$6 + 4 = \underline{\quad}$$
- $$13 + 13 = \underline{\quad}$$
- $$2 + (-2) = \underline{\quad}$$
- $$(-4) + 7 = \underline{\quad}$$
- $$8 + 4 = \underline{\quad}$$
- $$(-9) + (-2) = \underline{\quad}$$
- $$(-8) + 0 = \underline{\quad}$$
- $$5 + (-9) = \underline{\quad}$$
- $$9 + 11 = \underline{\quad}$$
- $$(-5) + (-10) = \underline{\quad}$$
- $$3 + 3 = \underline{\quad}$$
- $$(-4) + 8 = \underline{\quad}$$
- $$(-14) + 8 = \underline{\quad}$$
- $$6 + 21 = \underline{\quad}$$
- $$(-4) + (-16) = \underline{\quad}$$
- $$21 + (-6) = \underline{\quad}$$
- $$12 + 12 = \underline{\quad}$$
- $$(-9) + (-17) = \underline{\quad}$$
- $$(-11) + (-11) = \underline{\quad}$$
- $$5 + (-14) = \underline{\quad}$$
- $$11 + 11 = \underline{\quad}$$
- $$1 + (-18) = \underline{\quad}$$
- $$20 + 19 = \underline{\quad}$$
- $$(-10) + (-22) = \underline{\quad}$$

LINE ENDS

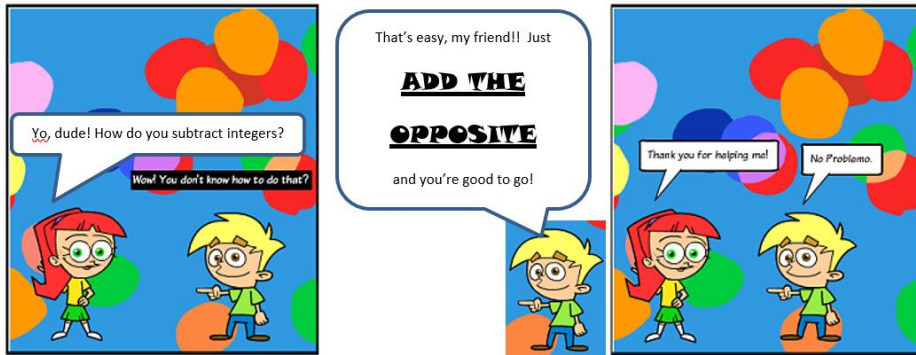


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- PATTERN #2
- $$(-18) + 8 = \underline{\quad}$$
- $$(-3) + 5 = \underline{\quad}$$
- $$25 + (-50) = \underline{\quad}$$
- $$6 + 3 = \underline{\quad}$$
- $$41 + 9 = \underline{\quad}$$
- $$11 + (-3) = \underline{\quad}$$
- $$(-20) + (-11) = \underline{\quad}$$
- $$17 + 13 = \underline{\quad}$$
- $$2 + (-25) = \underline{\quad}$$
- $$(-10) + (-6) = \underline{\quad}$$
- $$(-5) + 4 = \underline{\quad}$$
- $$(-3) + (-2) = \underline{\quad}$$
- $$20 + 20 = \underline{\quad}$$
- $$(-19) + (-9) = \underline{\quad}$$
- $$(-3) + (-11) = \underline{\quad}$$
- $$35 + (-10) = \underline{\quad}$$
- $$3 + (-5) = \underline{\quad}$$
- $$(-20) + 8 = \underline{\quad}$$
- $$3 + 4 = \underline{\quad}$$
- $$33 + (-2) = \underline{\quad}$$
- $$(-14) + (-16) = \underline{\quad}$$
- $$(-7) + 20 = \underline{\quad}$$
- $$(-20) + (-20) = \underline{\quad}$$
- $$11 + 17 = \underline{\quad}$$
- $$0 + 11 = \underline{\quad}$$
- $$(-10) + (-14) = \underline{\quad}$$
- $$(-30) + (-5) = \underline{\quad}$$
- $$(-3) + 20 = \underline{\quad}$$
- $$2 + 19 = \underline{\quad}$$
- $$(-5) + (-22) = \underline{\quad}$$

LINE ENDS

## ~ Subtracting Integers ~



Example 1: Subtract  $5 - (-8) \rightarrow$  Instead of *subtracting -8*, **ADD positive 8**

Example 2: Subtract  $-3 - (4) \rightarrow$  Instead of *subtracting 4*, **ADD negative 4**

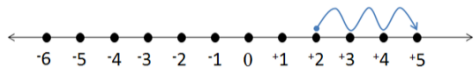
Example 3: Subtract  $-7 - (-2) \rightarrow$  Instead of *subtracting -2*, **ADD positive 2**

★ Why does this work?? Take a look at the visuals below: ★

Using a number line:

$$2 - (-3) =$$

If you were subtracting  $2 - 3$ , you would start at 2 and move back 3. But since you're subtracting a *negative* 3, you'll do the opposite!!

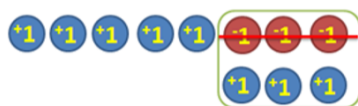


$$2 - (-3) = 2 + +3 = 5$$

Using counters:

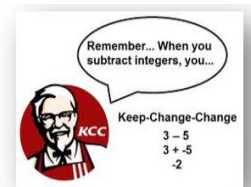
$$5 - (-3) =$$

Begin with 5 positive counters. You don't have 3 negatives to take away, so you must add in enough zero pairs to be able to take 3 away. That leaves you with 8 positives!!



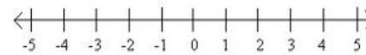
$$+5 - (-3) = +8$$

## ~ Subtracting Integers Practice ~

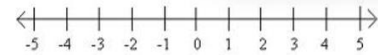


For #s 1-4, illustrate the subtraction on a number line.

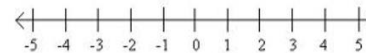
1)  $3 - 5 =$  \_\_\_\_\_



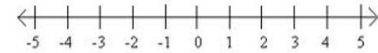
2)  $-1 - 1 =$  \_\_\_\_\_



3)  $-2 - (-2) =$  \_\_\_\_\_



4)  $3 - (-2) =$  \_\_\_\_\_



For #s 5-8, draw counters to illustrate the subtraction. Remember to use zero pairs if needed!



5)  $-2 - (-1) =$  \_\_\_\_\_

6)  $4 - 5 =$  \_\_\_\_\_

7)  $-4 - 2 =$  \_\_\_\_\_

8)  $3 - (-3) =$  \_\_\_\_\_

Evaluate the following problems, and SHOW your WORK:

9)  $14 - 15 =$  \_\_\_\_\_

10)  $-3 - (-4) =$  \_\_\_\_\_

11)  $0 - (-6) =$  \_\_\_\_\_

12)  $-52 - 4 =$  \_\_\_\_\_

13)  $-86 - (-86) =$  \_\_\_\_\_

14)  $13 - (-10) =$  \_\_\_\_\_

15)  $3 - 8 =$  \_\_\_\_\_

16)  $-16 - (-16) =$  \_\_\_\_\_

17)  $0 - 4 =$  \_\_\_\_\_

18)  $-6 - 8 + (-32) =$  \_\_\_\_\_

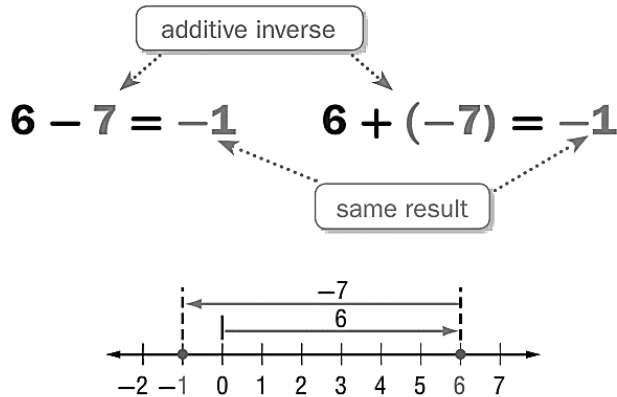
19)  $45 + (-30) - (-5) =$  \_\_\_\_\_

20)  $-912 - 4 + -16 =$  \_\_\_\_\_

# Subtracting Rational Numbers

Are you able to add rational numbers? Then you are able to subtract integers.

To subtract an integer, add its additive inverse. In other words, you subtract rational numbers by adding the opposite.



## Examples:

### 1. Find $8 - 13$ .

$$8 - 13 = 8 + (-13) \quad \text{To subtract 13, add -13.}$$

$$= -5 \quad \text{Simplify.}$$

Check by adding  $-5 + 13 \stackrel{?}{=} 8$   
 $8 = 8 \checkmark$

### 2. Find $-10 - 7$ .

$$-10 - 7 = -10 + (-7) \quad \text{To subtract 7, add -7.}$$

$$= -17 \quad \text{Simplify.}$$

Check by adding  $-17 + 7 \stackrel{?}{=} -10$   
 $-10 = -10 \checkmark$

## You Try:

### Subtract.

1)  $5 - 2$

2)  $6 - (-7)$   
 $6 + 7 = 13$

3)  $-3 - 2$   
 $-3 + (-2) = -5$

4)  $8 - 13$   
 $8 + (-13) = -5$

5)  $-7 - (-7)$   
 $-7 + 7 = 0$

6)  $6 - 12$   
 $6 + (-12) = -6$

7)  $15 - (-7)$   
 $15 + 7 = 22$

8)  $-15 - 6$   
 $-15 + (-6) = -21$

9)  $-3 - 8$   
 $-3 + (-8) = -11$

10)  $-10 - 12$   
 $-10 + (-12) = -22$

11)  $13 - (-12)$   
 $13 + 12 = 25$

12)  $14 - (-22)$   
 $14 + 22 = 36$

13)  $10 - (-20)$   
 $10 + 20 = 30$

14)  $-16 - 14$   
 $-16 + (-14) = -30$

15)  $-25 - 25$   
 $-25 + (-25) = -50$

16)  $6 - (-31)$   
 $6 + 31 = 37$

17)  $-18 - (-40)$   
 $-18 + 40 = 22$

18)  $15 - (-61)$   
 $15 + 61 = 76$

Evaluate each expression if  $r = -4$ ,  $s = 10$ , and  $t = -7$ .

19)  $r - 7$   
 $-4 + (-7) = -11$

20)  $t - s$   
 $-7 + (-10) = -17$

21)  $s - (-8)$   
 $10 + 8 = 18$

22)  $t - r$   
 $-7 + 4 = -3$

23)  $s - t$   
 $10 + 7 = 17$

24)  $r - s$   
 $-4 + (-10) = -14$

## Subtracting Integers with Models

**25) FOOTBALL** A team gained 5 yards on their first play of the game. Then they lost 6 yards. Find the total change in yardage.

**26) CHECKING** Your checking account is overdrawn by \$50. You write a check for \$20. What is the balance in your account?

**27) TEMPERATURE** The average temperature in Calgary, Canada, is  $22^{\circ}\text{C}$  in July and  $-11^{\circ}\text{C}$  in January. Find the range of the highest and lowest temperatures in Calgary.

Evaluate each expression if  $x = -8$ ,  $y = 7$ , and  $z = -11$ .

28)  $x - 7$

29)  $-13 - y$

30)  $-11 - z$

31)  $x - z$

32)  $z - y$

33)  $y - x$

34)  $x - (-z)$

35)  $|y - z|$

36)  $x - z - y$

37)  $3 + -x$

| Problem            | Sum | With Counters | Number Line |
|--------------------|-----|---------------|-------------|
| 1) $3 - 2 =$       |     |               |             |
| 2) $-2 - (-1) =$   |     |               |             |
| 3) $4 - (-4) =$    |     |               |             |
| 4) $(-7) - (-4) =$ |     |               |             |
| 5) $6 - 10 =$      |     |               |             |
| 6) $-5 - (-2) =$   |     |               |             |
| 7) $-2 - (-3) =$   |     |               |             |
| 8) $2 - 4 =$       |     |               |             |
| 9) $1 - (-9) =$    |     |               |             |
| 10) $-2 - (-3) =$  |     |               |             |

What is the algorithm (rule) for subtracting integers?

# DAFFYNTION DECODER

TWIN: \_\_\_\_\_  
 -980 -7 5181 476 -7 534 19 542 73 -115 476 -382  
 CARROT JUICE: \_\_\_\_\_  
 -254 476 19 542 534 -129 -7 -980 -607  
 MALE SURFER: \_\_\_\_\_  
 60 476 -7 -129 633 542 19 -444 -129 476 19 -589

TO DECODE THESE THREE DAFFYNTIONS, FOLLOW THESE DIRECTIONS:

Work any problem below and find your answer in the code. Each time the answer appears in the code, write the letter of that problem above it.

KEEP WORKING AND YOU WILL DECODE DEFINE PRINT.

- |  |  |
|--|--|
| <p>(L) <math>-78 + -37 =</math></p> <p>(C) <math>-562 - 45 =</math></p> <p>(E) <math>-81 - -623 =</math></p> <p>(V) <math>762 + -129 =</math></p> <p>(Y) <math>17 - 399 =</math></p> <p>(D) <math>-808 + 219 =</math></p> <p>(T) <math>445 - -89 =</math></p> <p>(B) <math>356 + -800 =</math></p> <p>(I) <math>-490 + -490 =</math></p> <p>(H) <math>671 - 925 =</math></p> <p>*****</p> <p>(M) Temperature in Tahiti: <math>27^{\circ}\text{C}</math>.<br/>       Temperature in Siberia: <math>-33^{\circ}\text{C}</math>.<br/>       What is the difference in these temperatures?<br/>       _____<math>^{\circ}\text{C}</math></p> | <p>(P) Horatio Hornswoggle was born: 57 B.C.<br/>       Horatio Hornswoggle died: 16 A.D.<br/>       How old was Horatio when he died? _____ years</p> <p>(O) Bank account balance: \$357.<br/>       Check written for: \$486.<br/>       What was the new balance? \$_____</p> <p>(F) Altitude of mountain climber: 4572 meters.<br/>       Altitude of submarine commander: <math>-609</math> meters.<br/>       What is the difference in these altitudes? _____ meters</p> <p>(A) The Roman Republic was established: 509 B.C.<br/>       The Roman Empire fell 985 years later.<br/>       In what year did the Empire fall? _____ A.D.</p> <p>(R) Altitude of scuba diver: <math>-12</math> meters.<br/>       Altitude of shark: <math>-31</math> meters.<br/>       What is the difference in these altitudes? _____ meters</p> <p>(N) Temperature at 8:00 A.M.: <math>-15^{\circ}\text{C}</math>.<br/>       Temperature rose <math>8^{\circ}\text{C}</math> during the next hour. What was the temperature at 9:00 A.M.? _____<math>^{\circ}\text{C}</math></p> |
|--|--|

## Solving One-Step Equations +/-

Solving a one-step equation with integers requires you to create zero pairs to isolate the variable.

### Examples:

- |  |   |
|--|---|
| <p>#1 Solve: <math>r + 5 = -10</math></p> <p style="padding-left: 100px;"><math>-5 -5</math></p> <p style="padding-left: 100px;"><math>r = -15</math></p>  | <p>Check: <math>r + 5 = -10</math></p> <p style="padding-left: 100px;"><math>-15 + 5 = -10</math></p> <p style="padding-left: 100px;"><math>-10 = -10 \checkmark</math></p>   |
| <p>#2 Solve: <math>p - (-3) = -6</math></p> <p style="padding-left: 100px;"><math>p + 3 = -6</math></p> <p style="padding-left: 100px;"><math>-3 -3</math></p> <p style="padding-left: 100px;"><math>p = -9</math></p> | <p>Check: <math>p - (-3) = -6</math></p> <p style="padding-left: 100px;"><math>-9 - (-3) = -6</math></p> <p style="padding-left: 100px;"><math>-9 + 3 = -6</math></p> <p style="padding-left: 100px;"><math>-6 = -6 \checkmark</math></p> |

### You Try!

Solve each equation. Don't forget to check your answer.

- |                    |                    |                      |
|--------------------|--------------------|----------------------|
| 1. $x - 13 = -22$  | 2. $x - (-4) = 10$ | 3. $y + 16 = -2$     |
| 5. $z + (-5) = 12$ | 6. $t + (-7) = -5$ | 7. $r - (-12) = -17$ |
| 8. $j + 23 = 54$   | 9. $y - 14 = 9$    | 10. $e + (-13) = -2$ |

## Multiplying & Dividing Integers

SAME SIGN = POSITIVE

DIFFERENT SIGNS = NEGATIVE

$$4 \cdot 3 = 12$$

$$-4 \cdot 3 = -12$$

$$6 \div 2 = 3$$

$$-6 \div 2 = -3$$

$$-5 \cdot -2 = 10$$

$$5 \cdot -2 = -10$$

$$-18 \div -9 = 2$$

$$-18 \div 9 = -2$$



\* Remember, you cannot divide by zero!  
Dividing by zero is undefined.

### Try These!

1)  $-8 \cdot -3 =$

2)  $16 \div -4 =$

3)  $-20 \cdot 5 =$

4)  $72 \div 8 =$

5)  $-56 \div 7 =$

6)  $12 \cdot -12 =$

7)  $-90 \div -6 =$

8)  $-18 \cdot -3 =$

9)  $-10 \cdot -10 =$

10)  $-99 \div 9 =$

11)  $-120 \div -12 =$

12)  $15 \cdot -60 =$

13)  $1000 \div -50 =$

14)  $-25 \cdot -16 =$

15)  $-51 \div 3 =$

## Multiplying & Dividing Rational #'s

SAME SIGN = POSITIVE

DIFFERENT SIGNS = NEGATIVE

$$4 \times 3 = 12$$

$$-4 \times 3 = -12$$

$$-6 \div (-2) = 3$$

$$-6 \div 2 = -3$$

$$\frac{-2}{5} \xrightarrow{\times} \frac{2}{3} = \frac{4}{15}$$



$$\frac{-2}{5} \xrightarrow{\times} \frac{2}{3} = -\frac{4}{15}$$

$$-\frac{1}{18} \div -\frac{1}{9} = \frac{1}{2}$$

$$-\frac{1}{18} \div -\frac{1}{9} = \frac{1}{2}$$

### Try These!

1)  $-8 \times -3 =$

2)  $16 \div -4 =$

3)  $-20 \times 0.5 =$

4)  $0.72 \div 8 =$

5)  $-56 \div 7 =$

6)  $12 \times -12 =$

7)  $-90 \div -6 =$

8)  $-18 \times -3 =$

9)  $-\frac{1}{4} \cdot \frac{2}{3} =$

10)  $\frac{1}{3} \div -5 =$

11)  $-\frac{2}{3} \div -\frac{1}{2} =$

12)  $15 \times -60 =$

13)  $-1\frac{1}{2} \cdot \frac{3}{4} =$

14)  $-25 \times -16 =$

15)  $-51 \div 3 =$



# Multiplying Rational Numbers

The **PRODUCT** of two rational numbers with the same sign is always positive.

Examples:

1)  $2(6) = 12$                       2)  $-10(-6) = 60$                       3)  $(-4)^2 = 16$

You Try:

1)  $-12(-4) =$                       2)  $(-5)^2 =$                       3)  $6(7) =$   
 4)  $-34(-2) =$                       5)  $-20(-8) =$                       6)  $(-2)^4 =$

The **PRODUCT** of two rational numbers with different signs is always negative.

Examples:

1)  $6(-4) = -24$                       2)  $-5(7) = -35$

You Try:

1)  $-7(11) =$                       2)  $(-3)^3 =$                       3)  $-2(14) =$   
 4)  $(-3)(-4)(-5) =$                       5)  $(-9)(-1)(-5) =$                       6)  $8(-12) =$

*Evaluate each expression if  $a = -6$ ,  $b = -4$ ,  $c = 3$ , and  $d = 9$ . Show all work including substitution and computation.*

7)  $-5c =$                       8)  $b^2 =$                       9)  $2a =$   
 10)  $bc =$                       11)  $abc =$                       12)  $abc^3 =$   
 13)  $-3a^2 =$                       14)  $-cd^2 =$                       15)  $-2a + b =$

## MULTIPLYING INTEGERS - A

### EXAMPLE #1

$$4 \cdot (-6) = 4 \times 6 = 24 = (-24)$$

YOU HAVE A POSITIVE FOUR AND A NEGATIVE SIX.

MULTIPLY THE NUMBERS,  $4 \times 6 = 24$ .

WHEN MULTIPLYING, A "+" AND A "-" MAKES A NEGATIVE NUMBER.

MULTIPLY AND DIVIDE RULES  
 IF THE SIGNS ARE THE SAME, THE ANSWER IS POSITIVE. IF THE SIGNS ARE DIFFERENT, THE ANSWER IS NEGATIVE.

### EXAMPLE #2

$$(-3) \cdot (-2) = (3)(2) = 6 = +6$$

YOU HAVE A NEGATIVE THREE AND A NEGATIVE TWO.

MULTIPLY THE NUMBERS,  $3 \times 2 = 6$ .

WHEN MULTIPLYING, A "-" AND A "-" MAKES A POSITIVE NUMBER.

EXAMPLES  
 $(+4)(+3) = +12$   
 $(-4)(-3) = +12$   
 $(+4)(-3) = -12$   
 $(-4)(+3) = -12$

SOLVE.

1.  $3 \cdot 6 =$  \_\_\_\_\_

THE SIGNS ARE THE SAME.

2.  $(-5) \cdot +7 =$  \_\_\_\_\_

THE SIGNS ARE DIFFERENT.

3.  $(-8) \cdot 4 =$  \_\_\_\_\_

5.  $9 \cdot (+4) =$  \_\_\_\_\_

7.  $-6 \cdot (-6) =$  \_\_\_\_\_

9.  $0 \cdot (-8) =$  \_\_\_\_\_

11.  $3 \cdot +7 =$  \_\_\_\_\_

13.  $(-2) \cdot 13 =$  \_\_\_\_\_

15.  $-8 \cdot (-7) =$  \_\_\_\_\_

17.  $5 \cdot -1 =$  \_\_\_\_\_

19.  $(+5) \cdot (-3) =$  \_\_\_\_\_

21.  $8 \cdot 0 =$  \_\_\_\_\_

23.  $(-4) \cdot (-9) =$  \_\_\_\_\_

25.  $11 \cdot -5 =$  \_\_\_\_\_

27.  $(-3) \cdot 8 =$  \_\_\_\_\_

29.  $12 \cdot +12 =$  \_\_\_\_\_

29.  $(-7) \cdot 5 =$  \_\_\_\_\_

4.  $(-6) \cdot +8 =$  \_\_\_\_\_

6.  $4 \cdot -6 =$  \_\_\_\_\_

8.  $9 \cdot (-9) =$  \_\_\_\_\_

10.  $(-9) \cdot (-9) =$  \_\_\_\_\_

12.  $-5 \cdot 3 =$  \_\_\_\_\_

14.  $(-7) \cdot (-6) =$  \_\_\_\_\_

16.  $+9 \cdot 13 =$  \_\_\_\_\_

18.  $12 \cdot (-5) =$  \_\_\_\_\_

20.  $(-4) \cdot (-4) =$  \_\_\_\_\_

22.  $-7 \cdot (-9) =$  \_\_\_\_\_

24.  $+5 \cdot -6 =$  \_\_\_\_\_

26.  $0 \cdot (-4) =$  \_\_\_\_\_

28.  $6 \cdot (+7) =$  \_\_\_\_\_

30.  $-9 \cdot (-9) =$  \_\_\_\_\_

30.  $(+2) \cdot 13 =$  \_\_\_\_\_

# Dividing Rational Numbers

The **QUOTIENT** of two rational numbers with the same sign is always positive.

**Examples:**

1)  $80 \div (10) = 8$       2)  $\frac{-66}{-11} = 6$       3)  $-42 \div (-6) = 7$

**You Try:**

1)  $-14 \div (-7) =$       2)  $\frac{-80}{-20} =$       3)  $-420 \div (-3) =$

4)  $\frac{540}{45} =$       5)  $-24 \div (-8) =$       6)  $100 \div (-0) =$

The **QUOTIENT** of two rational numbers with different signs is always negative.

**Examples:**

1)  $80 \div (-10) = -8$       2)  $\frac{-66}{11} = -6$       3)  $-42 \div 6 = -7$

**You Try:**

1)  $-12 \div 4 =$       2)  $\frac{18}{-2} =$       3)  $-10 \div 10 =$

4)  $350 \div (-25) =$       5)  $\frac{-256}{16} =$       6)  $-12 \div (4) =$

**Evaluate each expression if  $d = -24$ ,  $e = -4$ , &  $f = 8$ . Show all work including substitution and computation.**

7)  $12 \div e$       8)  $40 \div f$       9)  $d \div 6$

10)  $d \div e$       11)  $f \div e$       12)  $e^2 \div f$

13)  $\frac{-d}{e}$       14)  $ef \div 2$       15)  $\frac{f+8}{-4}$

## DIVIDING INTEGERS - A

EXAMPLE #1

$$24 \div (-6) = 24 \div 6 = 4 = (-4)$$

YOU HAVE A POSITIVE 24 AND A NEGATIVE 6.

DIVIDE THE NUMBERS,  $24 \div 6 = 4$ .

WHEN DIVIDING, A "+" AND A "-" MAKES A NEGATIVE NUMBER.

MULTIPLY AND DIVIDE RULE  
IF THE SIGNS ARE THE SAME THE ANSWER IS POSITIVE. IF THE SIGNS ARE DIFFERENT THE ANSWER IS NEGATIVE.

EXAMPLE #2

$$(-32) \div (-8) = 32 \div 8 = 4 = +4$$

YOU HAVE A NEGATIVE THIRTY-TWO AND A NEGATIVE EIGHT.

DIVIDE THE NUMBERS,  $32 \div 8 = 4$ .

WHEN DIVIDING, A "-" AND A "-" MAKES A POSITIVE NUMBER.

EXAMPLES  
 $(+12) \div (+3) = +4$   
 $(-12) \div (-3) = +4$   
 $(+12) \div (-3) = -4$   
 $(-12) \div (+3) = -4$

SOLVE.

1.  $21 \div 3 =$  \_\_\_\_\_  
THE SIGNS ARE THE SAME.

2.  $+40 \div (-4) =$  \_\_\_\_\_  
THE SIGNS ARE DIFFERENT.

3.  $(-12) \div +6 =$  \_\_\_\_\_

4.  $33 \div (-3) =$  \_\_\_\_\_

5.  $12 \div (-8) =$  \_\_\_\_\_

6.  $(-81) \div (-9) =$  \_\_\_\_\_

7.  $(-35) \div (-7) =$  \_\_\_\_\_

8.  $(+16) \div +4 =$  \_\_\_\_\_

9.  $(+36) \div 9 =$  \_\_\_\_\_

10.  $(-27) \div -3 =$  \_\_\_\_\_

11.  $(-49) \div (+7) =$  \_\_\_\_\_

12.  $54 \div 9 =$  \_\_\_\_\_

13.  $15 \div 5 =$  \_\_\_\_\_

14.  $+42 \div (-6) =$  \_\_\_\_\_

15.  $-28 \div 4 =$  \_\_\_\_\_

16.  $(-18) \div (-6) =$  \_\_\_\_\_

17.  $0 \div -8 =$  \_\_\_\_\_

18.  $39 \div (-3) =$  \_\_\_\_\_

19.  $(-32) \div +4 =$  \_\_\_\_\_

20.  $(-60) \div 5 =$  \_\_\_\_\_

21.  $(-12) \div (-2) =$  \_\_\_\_\_

22.  $(-8) \div (-1) =$  \_\_\_\_\_

23.  $72 \div (-9) =$  \_\_\_\_\_

24.  $22 \div -2 =$  \_\_\_\_\_

25.  $(-30) \div +3 =$  \_\_\_\_\_

26.  $(+25) \div 5 =$  \_\_\_\_\_

27.  $48 \div (-8) =$  \_\_\_\_\_

28.  $+36 \div (-4) =$  \_\_\_\_\_

29.  $-14 \div (-7) =$  \_\_\_\_\_

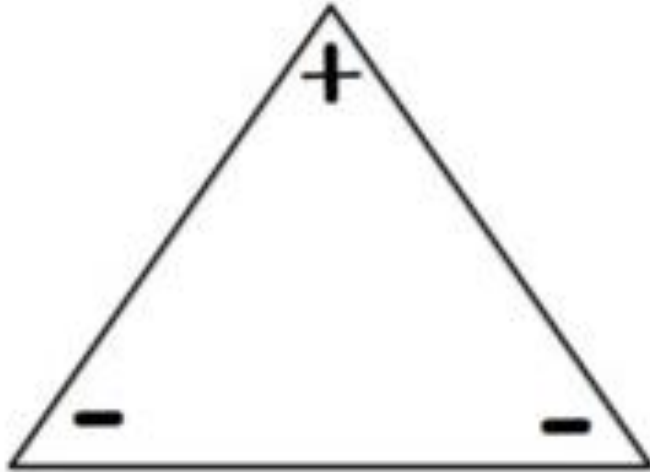
30.  $(-45) \div (+9) =$  \_\_\_\_\_

31.  $16 \div (+8) =$  \_\_\_\_\_

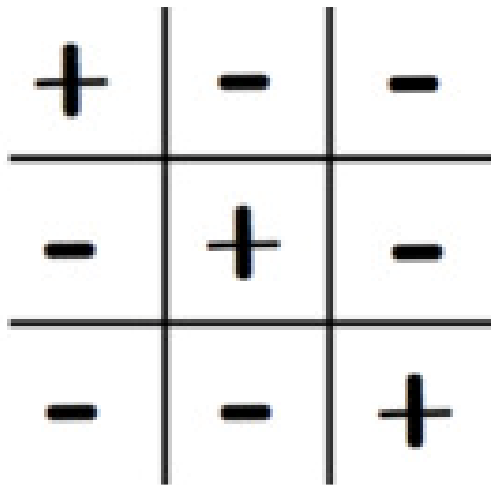
32.  $-24 \div 12 =$  \_\_\_\_\_

# MULTIPLYING AND DIVIDING INTEGERS RULES

(ONLY USED FOR MULTIPLICATION AND DIVISION)

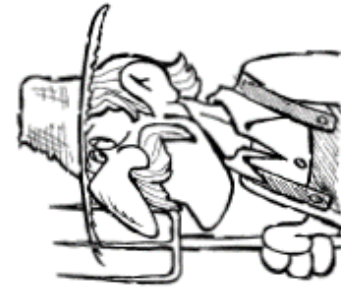


Put your fingers over the two signs of the numbers in your problem. The remaining sign is the sign of the answer.



Cover the two signs in any row column or diagonal the remaining sign is the sign of your answer.

## Multiplying and Dividing Puzzle



# FAMOUS FARMING EXPRESSION\*\*

The multiplication table below contains 42 mistakes. Shade in each box that contains a mistake. Please use pencil so you can erase if necessary.

YOU WILL END UP WITH A FAMOUS FARMING EXPRESSION!

| X  | 2   | -4  | -9  | 6   | 3   | 8   | -1 | 4  | -8  | -2  | -6  | 7   | -5  | 9   | -7  |
|----|-----|-----|-----|-----|-----|-----|----|----|-----|-----|-----|-----|-----|-----|-----|
| -3 | 6   | -12 | -27 | -18 | 9   | -24 | -3 | 12 | -24 | 6   | -18 | -21 | -15 | 27  | -21 |
| 9  | -18 | -36 | -81 | 54  | -27 | 72  | 9  | 36 | -72 | -18 | 54  | 63  | 45  | 81  | 63  |
| -6 | 12  | -24 | 54  | -36 | 18  | -48 | -6 | 24 | 48  | 12  | -36 | -42 | -30 | -54 | -42 |
| 5  | -10 | -20 | -45 | 30  | -15 | 40  | 5  | 20 | -40 | -10 | 30  | 35  | 25  | 45  | 35  |
| -7 | 14  | -28 | -63 | -42 | 21  | -56 | -7 | 28 | -56 | 14  | -42 | -49 | -35 | 63  | -49 |

# Multiplying and Dividing Practice

Multiply and/or Divide.

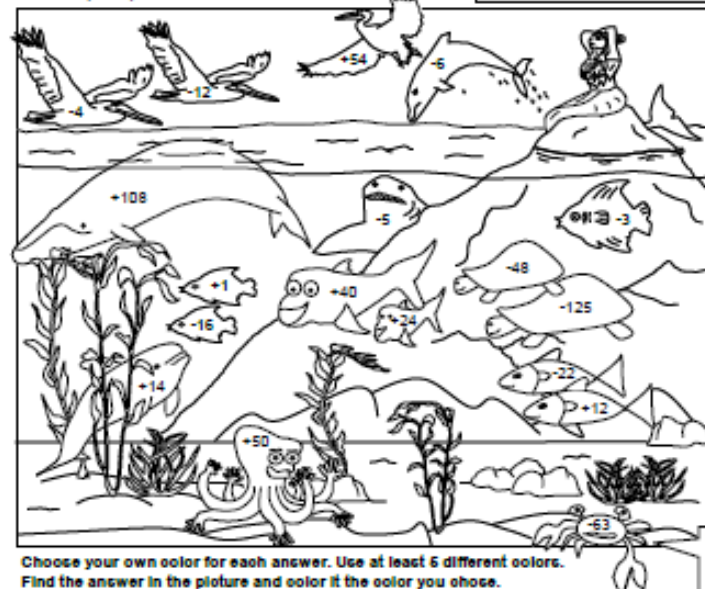
- |                       |                         |                         |
|-----------------------|-------------------------|-------------------------|
| 1) $-15 \div 3 =$     | 2) $-30(5) =$           | 3) $22 \div (-2) =$     |
| 4) $-14(-6) =$        | 5) $-8 \div (-8) =$     | 6) $-7(15) =$           |
| 7) $225 \div (-15) =$ | 8) $7(-3) =$            | 9) $-38 \div 2 =$       |
| 10) $-2(-10) =$       | 11) $-500 \div (-50) =$ | 12) $-3(-3)(4) =$       |
| 13) $(-5)^2 =$        | 14) $-24 \div (-8) =$   | 15) $20(-6) =$          |
| 16) $-49 \div (-7) =$ | 17) $(-13)^2 =$         | 18) $\frac{-36}{-4} =$  |
| 19) $-3(4) =$         | 20) $\frac{0}{-9} =$    | 21) $3(-3) =$           |
| 22) $\frac{64}{4} =$  | 23) $(-5)(-3)(4) =$     | 24) $-189 \div (-21) =$ |

Evaluate each expression if  $m = -32$ ,  $n = 2$ , and  $p = -8$ . Show all your work!

- |                       |                         |                        |
|-----------------------|-------------------------|------------------------|
| 25) $m \div n =$      | 26) $p \div 4 =$        | 27) $p^2 \div m =$     |
| 28) $m \div p =$      | 29) $\frac{-p}{n} =$    | 30) $p \div (-n^2) =$  |
| 31) $\frac{p}{4n} =$  | 32) $\frac{18-n}{-4} =$ | 33) $\frac{m+8}{-4} =$ |
| 34) $\frac{m+n}{6} =$ | 35) $mnp =$             | 36) $m \div n =$       |

## MULTIPLYING and DIVIDING INTEGERS ANSWER, FIND, AND COLOR

NAME: \_\_\_\_\_



**HELPFUL EXAMPLES**

- $+2 \cdot +3 = +6$
- $+2 \cdot -3 = -6$
- $-6 \div -3 = +2$
- $-6 \div +2 = -3$
- $-4 \cdot -3 \div +2 = +12 \div +2 = +6$
- $-8 \div -2 \div -2 = +4 \div -2 = -2$

**Sign Rules:**

- $(+) \times (+) = +$
- $(-) \times (-) = +$
- $(-) \times (+) = -$
- $(+) \times (-) = -$

Choose your own color for each answer. Use at least 6 different colors. Find the answer in the picture and color it the color you chose.

| ANSWER                   | COLOR | ANSWER                   | COLOR |
|--------------------------|-------|--------------------------|-------|
| $-5 \cdot 4 \cdot -2 =$  | _____ | $9 \cdot -1 \cdot -6 =$  | _____ |
| $48 \div -4 =$           | _____ | $-42 \div 14 =$          | _____ |
| $-2 \cdot -4 \cdot -6 =$ | _____ | $+32 \div -2 =$          | _____ |
| $4 \cdot -9 \div -3 =$   | _____ | $+5 \cdot +2 \cdot +5 =$ | _____ |
| $6 \cdot -2 \cdot -2 =$  | _____ | $+3 \cdot -12 \div 6 =$  | _____ |
| $-50 \div -5 \div -2 =$  | _____ | $-1 \cdot +1 \cdot -1 =$ | _____ |
| $-1 \cdot +9 \cdot +7 =$ | _____ | $12 \div -6 \cdot +2 =$  | _____ |
| $-8 \cdot -7 \div 4 =$   | _____ | $+88 \div 2 \div -2 =$   | _____ |
| $5 \cdot -5 \cdot +5 =$  | _____ | $-9 \cdot 4 \cdot -3 =$  | _____ |



# CRYPTIC QUIZ

SHOW WORK HERE:

1. What Did the Sardine Say When a Submarine Went By?

\_\_\_\_\_

-56 36 36 -33 -35 -12 -12 7 -35 -12 -96 -35 130 36 31 39 9 36 39 -56 9

2. What Happened to the Grocer Who Stacked All the Liquid Detergents on a High Shelf?

\_\_\_\_\_

7 9 -6 -35 5 25 -24 -15 39 -8 130 28 31 36 100 25 36 -69

TO DECODE THE ANSWERS TO THESE QUESTIONS:

Solve any equation below and find the solution in the code. Each time it appears, write the letter of the exercise above it. Keep working and you will decode the two answers.

Ⓘ  $n + 12 = 4$

Ⓔ  $4x = 36$

Ⓚ  $\frac{v}{3} = -11$

Ⓕ  $w - 9 = 22$

Ⓦ  $-7t = 42$

Ⓡ  $-\frac{1}{5}y = -20$

Ⓣ  $-32 = x + (-20)$

Ⓤ  $-48 = 2q$

Ⓝ  $13 = \frac{n}{10}$

Ⓨ  $-50 = 19 + p$

Ⓢ  $-15r = -75$

Ⓛ  $14 = \frac{-u}{4}$

Ⓖ  $x - (-16) = 44$

ⓗ  $42 = 6d$

Ⓒ  $\frac{1}{8}y = -12$

Ⓜ  $-4 = 11 + m$

Ⓐ  $-x = 35$

Ⓟ  $-3 = \frac{-a}{13}$

Ⓞ  $-18 + z = 18$

Ⓜ  $-125 = -5k$

# Converting Fractions to Decimals

To convert from a fraction to a decimal, you \_\_\_\_\_ the \_\_\_\_\_ by the \_\_\_\_\_.

## Examples

|  |   |   |   |
|--|---|---|---|
| <p><u>Change 1/4 to a decimal.</u></p> $\begin{array}{r} 0.25 \\ 4 \overline{) 1.00} \\ \underline{-8} \phantom{0} \\ 20 \\ \underline{-20} \\ 0 \end{array}$ <p><math>1/4 = 0.25</math></p> | <p><u>Change 2/3 to a decimal.</u></p> $\begin{array}{r} 0.666\dots \\ 3 \overline{) 2.00} \\ \underline{-18} \phantom{0} \\ 20 \\ \underline{-18} \\ 2 \end{array}$ <p><math>2/3 = 0.666\dots</math><br/>repeating decimal</p> | <p><u>Change 4/5 to a decimal.</u></p> $\begin{array}{r} 0.8 \\ 5 \overline{) 4.0} \\ \underline{-40} \\ 0 \end{array}$ <p><math>4/5 = 0.8</math></p> | <p><u>Change 1/8 to a decimal.</u></p> $\begin{array}{r} 0.125 \\ 8 \overline{) 1.000} \\ \underline{-8} \phantom{00} \\ 20 \\ \underline{-16} \\ 40 \\ \underline{-40} \\ 0 \end{array}$ <p><math>1/8 = 0.125</math></p> |
|--|---|---|---|

$\frac{3}{4} \rightarrow 3 \div 4$

$$\begin{array}{r} .75 \\ 4 \overline{) 3.00} \\ \underline{-28} \\ 20 \\ \underline{-20} \\ 0 \end{array}$$

**$\frac{3}{4} = 0.75$**

### You Try:

- 1)  $\frac{2}{5} =$  \_\_\_\_\_    2)  $\frac{2}{8} =$  \_\_\_\_\_    3)  $\frac{13}{20} =$  \_\_\_\_\_
- 4)  $1\frac{1}{2} =$  \_\_\_\_\_    5)  $\frac{5}{7} =$  \_\_\_\_\_    6)  $\frac{1}{9} =$  \_\_\_\_\_

# Converting Decimals to Fractions

If you can \_\_\_\_\_ it as a decimal, you can \_\_\_\_\_ it as a fraction. Say the decimal using the correct place value, write it

as a fraction and simplify.

### Examples:

|  |  |   |   |
|--|--|---|---|
| <p>Change 0.25 to a fraction.</p> <p>Say "twenty-five hundredths."</p> $\frac{25}{100} \div \frac{25}{25} = \frac{1}{4}$ | <p>Change 0.4 to a fraction.</p> <p>Say "four tenths."</p> $\frac{4}{10} \div \frac{2}{2} = \frac{2}{5}$ | <p>Change 1.04 to a fraction.</p> <p>Say "one and four hundredths."</p> $1\frac{4}{100} \div \frac{4}{4} = 1\frac{1}{25}$ | <p>Change 2.001 to a fraction.</p> <p>Say "two and one thousandth."</p> $2\frac{1}{1000}$ |
|--|--|---|---|

### You Try:

- 1)  $0.3 =$  \_\_\_\_\_    2)  $0.45 =$  \_\_\_\_\_    3)  $7.1 =$  \_\_\_\_\_
- 4)  $3.5 =$  \_\_\_\_\_    5)  $0.625 =$  \_\_\_\_\_    6)  $2.002 =$  \_\_\_\_\_
- 7)  $1.125 =$  \_\_\_\_\_    8)  $10.01 =$  \_\_\_\_\_    9)  $1.20 =$  \_\_\_\_\_



# Fractions, Decimals & Percents

## EXAMPLE Changing a Percent to a Fraction

Express 35% as a fraction.

- Change the percent directly to a fraction with a denominator of 100. The number of the percent becomes the numerator of the fraction.

$$35\% = \frac{35}{100}$$

- Simplify, if possible.

$$\frac{35}{100} = \frac{7}{20}$$

35% expressed as a fraction is  $\frac{7}{20}$ .

## EXAMPLE Changing Decimals to Percents

Express 0.7 as a percent.

$$0.7 \times 100 = 70$$

- Multiply the decimal by 100.

$$0.7 \rightarrow 70\%$$

- Add the percent sign.

So, 0.7 expressed as a percent is 70%.

## EXAMPLE Changing Percents to Decimals

Change 4% to a decimal.

- Express the percent as a fraction with 100 as the denominator.

$$4\% = \frac{4}{100}$$

- Change the fraction to a decimal by dividing the numerator by the denominator.

$$4 \div 100 = 0.04$$

So, 4% = 0.04.

# Converting Practice

| Percent | Decimal | Fraction   |
|---------|---------|--|
| 32%     | 0.32    | $\frac{32}{100} \div \frac{4}{4} = \frac{8}{25}$ |
|         | 0.81    |  |
| 40%     |         |  |
|         |         | $\frac{4}{5}$                                    |
| 52%     |         |  |
|         | 1.25    |  |
|         |         | $1\frac{9}{11}$                                  |
|         |         | $\frac{12}{16}$                                  |
| 144%    |         |  |
|         | 0.06    |  |