# Unit 8

# **Operations** with Rational Numbers

**Adding Rational Numbers** Subtracting Rational Numbers Multiplying/Dividing Rational Numbers Converting Fractions & Decimals

Name:				
Math Teacher:				

# **Math 6/7**

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<b>Unit 8 Calendar</b>						
2/10	2/11	2/12	2/13	2/14		
Unit 8 Pre-test Coin Counters Addition Intro	Computer Lab	Adding Rational Numbers	Adding Rational Numbers	Adding Rational Numbers & Quiz		
	IXL Skills W	leek of 2/25:	N1, N2, N7			
2/17	2/18	2/19	2/20	2/21		
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2/24	2/25	2/26	2/27	2/28		
Subtracting Rational Numbers	Computer Lab	Subtracting Rational Numbers	Subtracting Rational Numbers	Subtracting Rational Numbers & Quiz		
IXL Skills Week of 3/4: N3, N4, N5, N6, P5						
3/2	3/3	3/4	3/5	3/6		
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Review

IXL Skills Week of 3/11: N8, N9, N10, N11, P6

**Review** 

**Unit 8 Test** 

Multiplying & Dividing

Rational

Numbers

Computer

Lab

# Unit 8: Operations with Rational Numbers Standards, Checklist and Circle Map

# **Georgia Standards of Excellence (GSE):**

MGSE7.NS.1a: Describe situations in which opposite quantities combine to make 0.

<u>MGSE7.NS.1b</u>: Understand p + q as the number located a distance |q| from p, in the positive or negative direction depending on whether q is positive or negative. Show that a number and its opposite have a sum of 0 (are additive inverses). Interpret sums of rational numbers by describing real-world contexts.

<u>MGSE7.NS.1c</u>: Understand subtraction of rational numbers as adding the additive inverse, p - q = p + (-q). Show that the distance between two rational numbers on the number line is the absolute value of their difference, and apply this principle in real-world contexts.

MGSE7.NS.1d: Apply properties of operations as strategies to add and subtract rational numbers.

MGSE7.NS.2a: Understand that multiplication is extended from fractions to rational numbers by requiring that operations continue to satisfy the properties of operations, particularly the distributive property, leading to products such as (-1)(-1) = 1 and the rules for multiplying signed numbers. Interpret products of rational numbers by describing real-world contexts.

<u>MGSE7.NS.2b</u>: Understand that integers can be divided, provided that the divisor is not zero, and every quotient of integers (with non-zero divisor) is a rational number. If p and q are integers, then -(p/q) = (-p)/q = p/(-q). Interpret quotients of rational numbers by describing real-world contexts

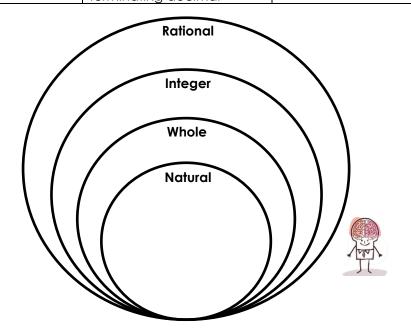
MGSE7.NS.2c: Apply properties of operations as strategies to multiply and divide rational numbers.

<u>MGSE7.NS.2d</u>: Convert a rational number to a decimal using long division; know that the decimal form of a rational number terminates in 0s or eventually repeats.

MGSE7.NS.3: Solve real-world mathematical problems involving the four operations with rational numbers.

What Will I Need to Learn??	Mark a check next to each concept as you m	aster them
I can show integer	addition and subtraction on a nun	nber line
I can understand t	hat the sum of opposites is zero	
I can add and subtra	act integers, including in real-life situa	tions
I understand that su	btracting is the same as adding the in	verse
I can multiply integ	gers (	
I can divide intege	rs	
I can convert fract	ions (rational numbers) to decimal	S
I can solve probler	ns with rational numbers	

Vocabulary Term	What does it mean? Definition	What does it look like? Picture/Example
Repeating decimal	A decimal that repeats the same digits infinitely	
Terminating decimal	A decimal that stops at a certain place value	
Positive number	A number greater than zero	
Negative number	A number less than zero	
Zero Pair	A pair of numbers whose sum is zero	
Natural numbers	"Counting numbers" from one to infinity	
Whole numbers	"Counting numbers" from zero to infinity (all natural numbers and zero)	
Integers	Whole numbers and their opposites	
Rational numbers	A real number that can be written as an integer, a fraction, or a repeating or terminating decimal	



# Unit 8 End of Unit Study Guide

## **Knowledge and Understanding**

- 1) What is the algorithm for adding with negative numbers?
- 2) a) What is the sum of two numbers that are the same distance from zero on the number line?
  - b) What are they called?
- 3) Model the problem -6 2 using + and counters:

## **Proficiency of Skills**

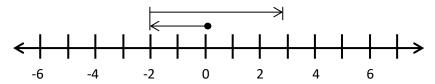
4) 10-(-7)=\_\_\_\_

- 5) (2)(12)(-5) = \_\_\_\_
- 6) (-150)÷(-15)=\_\_\_\_
- 7) (8.1)+(-1)+(-7.1)=
- 8) (-1.3) (-4.3) =
- 9) (-5)(2-8)=
- 10) Convert  $\frac{2}{9}$  to a decimal: \_\_\_\_\_
- 11) Convert 1.08 to a fraction: \_\_\_\_\_

## **Application**

- 12) Order from least to greatest:  $-\frac{1}{4}$ ,  $-\frac{6}{8}$ ,  $1\frac{4}{5}$ , -0.5, 1.4
- 13) If b represents a negative number, is  $b \cdot b$  a positive or negative number?

- 14) A submarine 530 feet below sea level descends an additional 100 feet before ascending 120 feet. What is the location of the submarine?
  - a) 750 ft below sea level
- b) 550 ft below sea level
- c) 510 ft below sea level
- d) 510 ft above sea level
- 15) Name two integers have a product of -30 and a sum of -7.
- 16) The temperature at 9 AM was 11°F. The temperature dropped 4 degrees per hour for the next three hours. What is the temperature at noon?
- a) -3°F
- b) -7°F
- c) -1°F
- d) -2°F
- 17) What addition expression is represented by the model below?



18) What subtraction expression is represented by the model pelow;



- 19) When the following fractions are converted to decimals, which one will result in a repeating decimal?
  - A.  $\frac{7}{10}$  B.  $\frac{5}{12}$  C.  $\frac{5}{8}$  D.  $\frac{3}{5}$

- 20) For your birthday, you decide to go parasailing over the ocean. You're peacefully sailing at 120 feet above sea level, and then you ascend 25 feet. Finally, you decide to dive into the ocean, and you fall 165 feet. Describe your new location. Justify your answer with an illustration, an equation, and/or complete sentences.

# Solve for x in each equation below. SHOW ALL STEPS:

$$21. x - 4.23 = -9.05$$

22. 
$$-8x = -60$$

23. 
$$x + 4 = -9 \frac{1}{4}$$

24. 
$$\frac{x}{-5} = -10$$

25. 
$$3\frac{1}{2}x = -70$$

26. 
$$x + 8 = -42$$

# 27. Fill in the table:

<u>Fraction</u>	<u>Decimal</u>	<u>Percent</u>
3 1/4		
	0.33	
- 1/8		
5/6		
	-5.375	
	16.4	
-8 3/11		

# **Adding/Subtracting Fraction Review**

**Adding Fractions with Like Denominators** 

 $\frac{1}{7} + \frac{3}{7}$  Add the numerators. Denominator is unchanged.  $\frac{1+3}{7}$   $\frac{4}{7}$ 

**Adding Fractions with Unlike Denominators** 

$$\frac{1}{8} + \frac{2}{3}$$

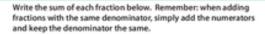
Rewrite with common denominator  $3 \times \frac{1}{8} + \frac{2}{3} \times 8$ 

Add the numerators  $\frac{3}{24} + \frac{16}{24}$ 

 $\frac{19}{24}$ 



# Adding Fractions with the same denominator





3 denominat

$$\frac{3}{5} + \frac{1}{5} = \frac{4}{5}$$

$$\frac{5}{5} + \frac{8}{5} =$$

$$\frac{3}{7} + \frac{1}{7} =$$

$$\frac{6}{3} + \frac{4}{3} =$$

$$\frac{7}{4} + \frac{8}{4} =$$

$$\frac{11}{9} + \frac{5}{9} =$$

$$\frac{9}{8} + \frac{9}{8} =$$

$$\frac{10}{12} + \frac{12}{12} =$$

$$\frac{17}{22} + \frac{3}{22} =$$

$$\frac{22}{50} + \frac{15}{50} + \frac{17}{50} =$$

$$\frac{35}{100} + \frac{6}{100} + \frac{79}{100} + \frac{14}{100} =$$



# Subtraction Fractions with UNLIKE denominators

 Find the LCM of the denominators. This is your new denominator.

> Multiples of 6 = 6, 12, 18 Multiples of 9 = 9, 18, 27

2. Rewrite the problem using the LCM.

$$\frac{5}{6} \times 3 - \frac{3}{9} \times 2 = \frac{15}{18} - \frac{6}{18}$$

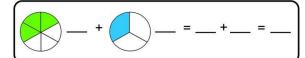
Subtract the numerators. The denominator stays the same.

$$\frac{15}{18} - \frac{6}{18} = \frac{9}{18}$$

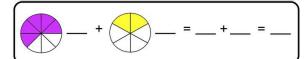
4. Simplify

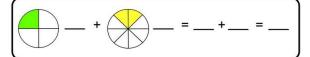
Divide by the Greatest Common Factor,

 $\underline{\text{\bf Directions}}\colon$  Write the fraction for each  $\overline{\text{\bf d}}\text{iagram}.$  Then, add the fractions. Make sure the denominators are the same.









# **Adding Fractions Practice**

# **Subtracting Fractions Practice**

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t the Dollar at the bottom of the pag	
Why Did Airhead Eat the Dollar He Brought to School3 Do each exercise and find your answer at the bottom of the page. Write the letter of the exercise in the box above the answer.	
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# Adding Integers

**Adding the SAME Sign** 

**Adding DIFFERENT Signs** 

# **Adding Rational Numbers**

To add rational numbers with the same sign, add their absolute values. The sum is:

- positive if both integers are positive.
- negative if both integers are negative.

To add rational numbers with different signs, subtract their absolute values.

The sum is:

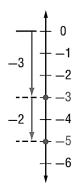
- positive if the positive integer's absolute value is greater.
- negative if the negative integer's absolute value is greater.
- **Remember:** What do you have more of, positives or negatives, and how many more do you have?

## **Examples:**

1. Find 
$$-3 + (-2)$$
.

Start at 0. Move 3 units down to show -3.

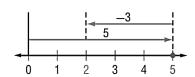
From there, move 2 units down to show -2.



So, 
$$-3 + (-2) = -5$$
.

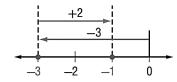
**2.** Find 
$$-26 + (-17)$$
.  $-26 + (-17) = -43$ 

3. Find 
$$5 + (-3)$$
.



So, 
$$5 + (-3) = 2$$
.

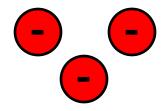
**4.** Find 
$$-3 + 2$$
.

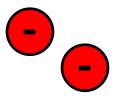


So, 
$$-3 + 2 = -1$$
.

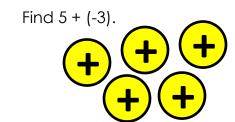
# Find the sum using two-color counters.

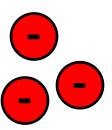
Find -3 + (-2).



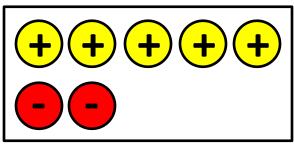


Three negatives (-3) plus another two negatives (-2) gives you five negatives (-5).



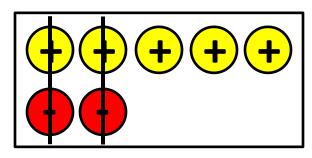


First, match up your zero pairs.



\*\*Remember that the sum of a number and its opposite is always 0. A number and its opposite are zero pairs.\*\*

Then cross out your zero pairs.



There are three positives left so, 5 + (-2) = 3.

# **Adding Integers with Models**

Problem	Sum	With Counters	Number Line
1) 3 + (-5) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
2) 2 + (-8) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 *1 *2 *3 *4 *5 *6 *7 *8 *9 *10
3) 4 + (-4) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
4) (-7) + 4 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
5) (-6) + 5 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10

What is the algorithm (rule) for adding integers with DIFFERENT signs?

Problem	Sum	With Counters	Number Line
1) -5 + -2 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
2) -2 + -3 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
3) -2 + -4 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
4) 7 + 4 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
5) -2 + -3 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10

What is the algorithm (rule) for adding integers with the <u>SAME</u> signs?

## You Try:

Use (+) and (-) counters or a number line to find the sum.

Use any method to find the sum.

19) 
$$\frac{5}{8} + \frac{1}{8}$$

**20)** 
$$-\frac{1}{4} + \frac{3}{4}$$

**20)** 
$$-\frac{1}{4} + \frac{3}{4}$$
 **21)**  $-\frac{7}{15} + (-\frac{4}{15})$ 

Write an addition expression to describe each situation. Then find each sum.

- 28) HAWK A hawk is in a tree 100 feet above the ground. It flies down to the ground.
- 29) RUNNING Leah ran 6 blocks north then back 4 blocks south.

# **More Adding Rational Numbers**

If a = -3, b = -5 and c = 5, find the sum.

4) 
$$a + b + c$$

If x = -10, y = 2 and z = -1, find the sum.

**8)** 
$$|z| + x$$

**12)** 
$$|x + y| + z$$

Write an addition expression to describe each situation. Then find each sum.

13) FOOTBALL A team gains 20 yards. Then they lose 7 yards.

**14) MONEY** Roger owes his mom \$5. He borrows another \$6 from her.

15) HOT AIR BALLOON A balloon rises 340 feet into the air. Then it descends 130 feet.

16) CYCLING A cyclist travels downhill for 125 feet. Then she travels up a hill 50 feet.

## ADDING INTEGERS

LINE ENDS

NAME:

ANSWER THE PROBLEMS BELOW AND CONNECT THE DOTS IN THE ORDER YOU CREATED. I STARTED THE PATTERN FOR YOU...NOW YOU DO THE REST.

## NOTE: PATTERNS ARE NOT CONNECTED TOGETHER PATTERN #1 41 + 9 = 50(-9) + (-17) = (-26)(-20) + (-11) = (-5) + 4 =(-14) + 7 =(-3) + 8 =13 + 13 = (-14) + (-16) =27 (-7) + 20 = $(-10)_{-}$ (-26) (-4) + 7 =\_(-30) + (-6) = (-28) + (-9) = 17 + 13 = 22 ● 11 = 8 12 + 12 = 30 11 + (-3) = (-17)31 (-13)11 + 17 = + 11 = (-8)(-10) + (-14) =(-11) 5 + (-14) = (-20) + (-20) =(-3) + 20 =(-10) + (-22) =2 + 19 =

PATTERN #2 (-18) + 8(-3) + 5 =(-10) + (-6) =(-11) + (-11) =+ (-2) = + (-18) = (-18) +5 = 0 = + (-25) = + (-2) = (-9) + (-2) =(-3) + (-2) =+ 3 = (-20) + 8 =(-3) + (-11) = 35 + (-10) = 20 + 19 = + 3 = (-19) + (-9) =+ 21 = (-4) + (-16) =(-30) + (-5) =+ 20 = 25 + (-50) = (-5) + (-10) =(-5) + (-22) =

LINE ENDS

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## ADDING INTEGERS

NAME:

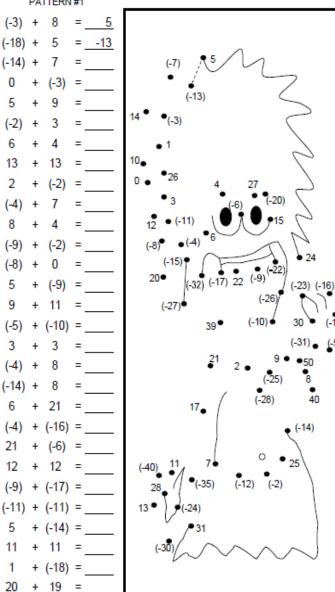
PATTERN #2

ANSWER THE PROBLEMS BELOW AND CONNECT THE DOTS IN THE ORDER YOU CREATED. I STARTED THE PATTERN FOR YOU...NOW YOU DO THE REST. NOTE: PATTERNS ARE NOT CONNECTED TOGETHER

PATTERN #1

(-10) + (-22) =

LINE ENDS



(-18) + 8 =+ (-50) = 3 = + (-3) = (-20) + (-11) = 17 + 13 = + (-25) = (-10) + (-6) =(-5) + 4 =(-3) + (-2) =+ 20 = (-19) + (-9) = (-3) + (-11) =+ (-10) = + (-5) = (-20) +8 = (-14) + (-16) = (-7) + 20 =(-20) + (-20) =+ 17 = + 11 = (-10) + (-14) = (-30) + (-5) =

(-3) + 20 =

(-5) + (-22) =

+ 19 =

LINE ENDS

# ~ Subtracting Integers ~



Example 1: Subtract  $5 - (-8) \rightarrow$  Instead of subtracting -8, ADD positive 8

Example 2: Subtract  $-3 - (4) \rightarrow$  Instead of subtracting 4, ADD negative 4

Example 3: Subtract -7 - (-2) → Instead of subtracting -2, ADD positive 2

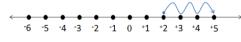
# Why does this work?? Take a look at the visuals below:



### Using a number line:

### 2- (-3) =

If you were subtracting 2 – 3, you would start at 2 and move back 3. But since you're subtracting a negative 3, you'll do the opposite!!



$$2 - 3 = 2 + 3 = 5$$

## Using counters:

## 5 – (-3) =

Begin with 5 positive counters.

You don't have 3 negatives to take away, so you must add in enough zero pairs to be able to take 3 away. That leaves you with 8 positives!!

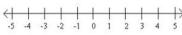


# ~ Subtracting Integers Practice ~

For #s 1-4, illustrate the subtraction on a number line.

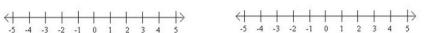












## For #s 5-8, draw counters to illustrate the subtraction. Remember to use zero pairs if needed!

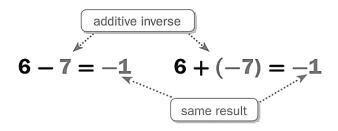


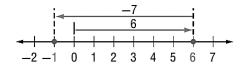
Evaluate the following problems, and SHOW your WORK:

# **Subtracting Rational Numbers**

Are you able to add rational numbers? Then you are able to subtract integers.

To subtract an integer, add its additive inverse. In other words, you subtract rational numbers by adding the opposite.





# **Examples:**

# **1.** Find 8 - 13.

$$8 - 13 = 8 + (-13)$$
 To subtract 13, add -13.  
= -5 Simplify.

Check by adding 
$$-5 + 13 \stackrel{?}{=} 8$$
  
 $8 = 8 \checkmark$ 

# **2.** Find -10 - 7.

$$-10 - 7 = -10 + (-7)$$
 To subtract 7, add -7.  
= -17 Simplify.

Check by adding 
$$-17 + 7 \stackrel{?}{=} -10$$
  
 $-10 = -10 \checkmark$ 

# You Try:

## Subtract.

Evaluate each expression if r = -4, s = 10, and t = -7.

- **25) FOOTBALL** A team gained 5 yards on their first play of the game. Then they lost 6 yards. Find the total change in yardage.
- **26) CHECKING** Your checking account is overdrawn by \$50. You write a check for \$20. What is the balance in your account?
- **27) TEMPERATURE** The average temperature in Calgary, Canada, is 22°C in July and –11°C in January. Find the range of the highest and lowest temperatures in Calgary.

Evaluate each expression if x = -8, y = 7, and z = -11.

**29)** 
$$-13 - y$$

**34)** 
$$\times - (-z)$$

**35)** 
$$|y-z|$$

**36)** 
$$X - Z - Y$$

# **Subtracting Integers with Models**

Problem	Sum	With Counters	Number Line
1) 3 - 2 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
2) -2 - (-1) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
3) 4 - (-4) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
4) (-7) - (-4) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
5) 6 – 10 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
6) -5 - (-2) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
7) -2 - (-3) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
8) 2 – 4 =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
9) 1 – (-9) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 +1 +2 +3 +4 +5 +6 +7 +8 +9 +10
10) -2 - (-3) =			-10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 *1 *2 *3 *4 *5 *6 *7 *8 *9 *10

What is the algorithm (rule) for subtracting integers?

# DAFFYNITION DECODER

-980 -7 5181 476 -7 534 19 542 73 -115 476 -382 CARROT JUICE: 476 19 542 534 -129-980 -607MALE SURFER:

60 476 -7 -129 633 542 19 -444 -129 476 19 -589

TO DECODE THESE THREE DAFFYNITIONS, FOLLOW THESE DIRECTIONS:

Work any problem below and find your answer in the code. Each time the answer appears in the code, write the letter of that problem above it.

.

KEEP WORKING AND YOU WILL DECODE DEFINE PRINT.

- $^{-78} + ^{-37} =$
- $^{-}562 45 =$
- -81 -623 =
- 762 + -129 =
- 17 399 =
- $^{-808} + 219 =$
- 445 89 =
- 356 + -800 =
- $^{-490} + ^{-490} =$
- 671 925 =
- Temperature in Tahiti: 27°C. Temperature in Siberia: "33°C. What is the difference in these temperatures?

\*\*\*\*\*\*\*\*\*\*\*\*

- Horatio Hornswoggle was born: Horatio Hornswoggle died: 16 A.D. How old was Horatio when he died?
- \_years Bank account balance: \$357. Check written for: \$486. What was the new balance?
- Altitude of mountain climber: 4572 meters. Altitude of submarine commander: ~609 meters. What is the difference in these altitudes? .meters
- The Roman Republic was established: 509 B.C. The Roman Empire fell 985 vears later. In what year did the Empire fall?
- Altitude of scuba diver: -12 meters. Altitude of shark: "31 meters. What is the difference in these altitudes? meters
- Temperature at 8:00 A.M.: -15°C. Temperature rose 8°C during the next hour. What was the temperature at 9:00 A.M.?

# **Solving One-Step Equations +/-**

Solving a one-step equation with integers requires you to create zero pairs to isolate the variable.

## **Examples:**

#1 Solve: 
$$r + 5 = -10$$
 Check:  $r + 5 = -10$ 

$$-5 -5 -5 -15 + 5 = -10$$

$$r = -15 -10 = -10 \checkmark$$

#2 Solve: 
$$p - (-3) = -6$$
 Check:  $p - (-3) = -6$ 

$$p + 3 = -6$$

$$-9 - (-3) = -6$$

$$-9 + 3 = -6$$

$$p = -9$$

$$-6 = -6 \checkmark$$

# You Try!

Solve each equation. Don't forget to check your answer.

**1.** 
$$x - 13 = -22$$

**2.** 
$$x - (-4) = 10$$

**3.** 
$$y + 16 = -2$$

**5.** 
$$z + (-5) = 12$$

**6.** 
$$t + (-7) = -3$$

**8.** 
$$i + 23 = 54$$

**9.** 
$$y - 14 = 9$$

# Multiplying & Dividing Integers

# SAME SIGN = POSITIVE

# **DIFFERENT SIGNS = NEGATIVE**

$$4 \cdot 3 = 12$$

$$6 \div 2 = 3$$

$$-6 \div 2 = -3$$

$$-5 \cdot -2 = 10$$

$$5 \cdot -2 = -10$$

$$-18 \div -9 = 2$$





Remember, you cannot divide by zero!
 Dividing by zero is undefined.

# Try These!

15) 
$$-51 \div 3 =$$

# Multiplying & Dividing Rational #'s

SAME SIGN = POSITIVE

DIFFERENT SIGNS = NEGATIVE

$$4 \times 3 = 12$$

$$-4 \times 3 = -12$$

$$-6 \div (-2) = 3$$

$$-6 \div 2 = -3$$

$$-\frac{2}{5} \xrightarrow{\mathsf{x}} -\frac{2}{3} = \frac{4}{15}$$



$$-\frac{2}{5} \xrightarrow{\mathsf{X}} \frac{2}{3} = -\frac{4}{15}$$

$$-\frac{1}{18} \div -\frac{1}{9} = \frac{1}{2}$$

$$-\frac{1}{18} \div -\frac{1}{9} = -\frac{1}{2}$$

# Try These!

$$9 - \frac{1}{4} \cdot \frac{2}{3} =$$

10) 
$$\frac{1}{3} \div -5 =$$

11) 
$$-\frac{2}{3} \div -\frac{1}{2} =$$

13) 
$$-1\frac{1}{2} \cdot \frac{3}{4} =$$

# **Multiplying Rational Numbers**

The PRODUCT of two rational numbers with  $\underline{\text{the same sign}}$  is always positive.

# **Examples:**

1) 2(6) = 12

- 2) -10 (-6) = 60
- 3)  $(-4)^2 = 16$

# You Try:

- 1) -12 (-4) =
- 2)  $(-5)^2 =$

3) 6 (7) =

- 4) -34 (-2) =
- 5) -20 (-8) =
- 6) (-2)4

The PRODUCT of two rational numbers with <u>different signs</u> is always negative.

## **Examples:**

- 1) 6 (-4) = -24
- 2) -5 (7) = -35

## You Try:

1) -7 (11) =

2)  $(-3)^3 =$ 

3) -2 (14) =

- 4) (-3) (-4) (-5) =
- 5) (-9) (-1) (-5) =
- 6) 8 (-12) =

Evaluate each expression if a = -6, b = -4, c = 3, and d = 9. Show all work including substitution and computation.

7) -5c =

8)  $b^2 =$ 

9) 2a =

10) bc =

- 11) abc =
- 12)  $abc^3 =$

13) 
$$-3a^2 =$$

- 14)  $-cd^2 =$
- 15) -2a + b =

## MULTIPLYING INTEGERS - A

## EXAMPLE #1

4 + (-6) = 4 x 6 = 24 = (-24)

YOU HAVE A
POSITIVE FOUR AND
A NEGATIVE SIX.

MULTIPLY THE WHEN MULTIPLYING, A "+" AND A "-" MAKES A NEGATIVE NUMBER

IF THE SIGNS ARE THE SAME, THE ANSWER IS POSITIVE. IF THE SIGNS ARE DIFFERENT, THE ANSWER IS NEGATIVE.

MULTIPLY AND DIVIDE RULES

## EXAMPLE #2

YOU HAVE A NEGATIVE THREE AND A NEGATIVE TWO. MULTIPLY THE NUMBERS, 3 X 2 = 6. WHEN MULTIPLYING, A "-" AND A "-" MAKES A POSITIVE NUMBER. EXAMPLES (+4)(+3) = +12 (-4)(-3) = +12 (+4)(-3) = -12

(-4)(+3) = -12

## SOLVE.

- 1. 3 6 =
  THE SIGNS ARE THE SAME.
- 3. (-8) 4 =
- 5. 9 (+4) =
- 7. -6 (-6) =
- \_\_\_\_

0 • (-8) =

3 + +7 =

- \_\_\_\_
- 13. (-2) 13 =
- 15. -8 (-7) =
- 17. 5 -1 = \_\_\_\_\_
- 19. (+5) (-3) =
- 21. 8 0 =
- 23. (-4) (-9) =
- 25. 11 -5 =
- 27. (-3) 8 =
- 29. 12 +12 =
- 29. (-7) 5 =

- (-5) + +7 =
   THE SIGNS ARE DIFFERENT.
  - (-8) + +8 =
- 6. 4 -6 =
- 8. 9 + (-9) =
- 10. (-9) + (-9) =
- 12. -5 3 =
- 14. (-7) (-6) =
- l6. +9 + 13 =
- 18. 12 + (-5) =
- 20. (-4) (-4) =
- 22. -7 + (-9) =
- 24. +5 + -6 =
- 26. 0 (-4) =
- 28. 6 (+7) =
- 30. -9 + (-9) =
- 30. (+2) + 13 =

# **Dividing Rational Numbers**

The QUOTIENT of two rational numbers with the same sign is always positive.

# **Examples:**

2) 
$$\frac{-66}{-11} = 6$$

3) 
$$-42 \div (-6) = 7$$

# You Try:

2) 
$$\frac{-80}{-20}$$
 =

3) 
$$-420 \div (-3) =$$

4) 
$$\frac{540}{45}$$
 =

The QUOTIENT of two rational numbers with different signs is always negative.

## **Examples:**

1) 
$$80 \div (-10) = -8$$

2) 
$$\frac{-66}{11} = -6$$

3) 
$$-42 \div 6 = -7$$

## You Try:

2) 
$$\frac{18}{-2}$$
 =

3) 
$$-10 \div 10 =$$

5) 
$$\frac{-256}{16}$$
 =

Evaluate each expression if d = -24, e = -4, & f = 8. Show all work including substitution and computation.

10) 
$$d \div e$$

11) 
$$f \div e$$

12) 
$$e^2 \div f$$

13) 
$$\frac{-d}{e}$$

15) 
$$\frac{f+8}{-4}$$

## **DIVIDING INTEGERS - A**

## EXAMPLE #1

POSITIVE 24 AND A NEGATIVE 6.

DIVIDE THE NUMBERS, 24+6=4.

WHEN DIVIDING, A "+" AND A "-" MAKES A NEGATIVE NUMBER.

MULTIPLY AND DIVIDE RULE IF THE SIGNS ARE THE SAME THE ANSWER IS POSITIVE. IF THE SIGNS ARE DIFFERENT THE ANSWER IS NEGATIVE.

## EXAMPLE #2

YOU HAVE A NEGATIVE THIRTY-TWO AND A NEGATIVE EIGHT.

DIVIDE THE NUMBERS, 32+8=4.

WHEN DIVIDING. A "-" AND A "-" MAKES A POSITIVE NUMBER.

16.

**EXAMPLES**  $(+12) \div (+3) = +4$  $(-12) \div (-3) = +4$ (+12) + (-3) = -4 $(-12) \div (+3) = -4$ 

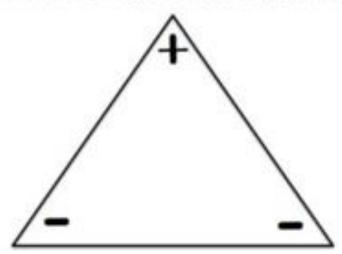
### SOLVE.

27.

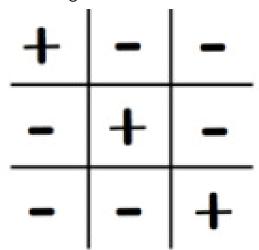
48 + (-8) =

# MULTIPLYING AND DIVIDING INTEGERS RULES

(ONLY USED FOR MULTIPLICATION AND DIVISION)



Put your fingers over the two signs of the numbers in your problem. The remaining sign is the sign of the answer.



Cover the two signs in any row column or diagonal the remaining sign is the sign of your answer.

# **Multiplying and Dividing Puzzle**



# FAMOUS FARMING EXPRESSION\*\*

The multiplication table below contains 42 mistakes. Shade in each box that contains a mistake. Please use pencil so you can erase if necessary.

YOU WILL END UP WITH A FAMOUS FARMING EXPRESSION!

<b>L</b> -	-21	63	-42	35	-49
6	27	81	-54	45	63
-2	-15	45	-36 -42 -30 -54 -42	25	-35
7	-21	63	-42	35	-49
9_	-18 -21	54	-36	30	-42
.2	9	-18	12	10	14
8	-24	-72 -18	48	-40 -10	-56 14
4	12	36	24	20	28
1-	3	6	9_	2	-7
8	-24	72	-48	40	99-
3	6	54 -27		-15	21
9	-18	54	-36 18	30	-42
6-	-12 -27 -18	-81	54	-45	-63
-4	-12	-36 -81	-24	-20 -45 30 -15 40	-28 -63 -42
7	9	-18	12	-10	14
×	-3	6	9_	5	_7

# **Mulitiplying and Dividing Practice**

Multiply and/or Divide.

1) 
$$-15 \div 3 =$$

$$-30(5) =$$

2) 
$$-30(5) =$$
 3)  $22 \div (-2) =$ 

4) 
$$-14(-6) =$$

5) 
$$-8 \div (-8) =$$

7) 
$$225 \div (-15) =$$

8) 
$$7(-3) =$$

$$10) -2(-10) =$$

11) 
$$-500 \div (-50) = 12) -3(-3)(4) =$$

13) 
$$(-5)^2 =$$

14) 
$$-24 \div (-8) =$$
 15)  $20(-6) =$ 

$$16) -49 \div (-7) =$$

17) 
$$(-13)^2 = 18)^{\frac{-36}{4}} =$$

18) 
$$\frac{-36}{-4}$$
 =

19) 
$$-3(4) =$$

20) 
$$\frac{0}{-9}$$
 =

20) 
$$\frac{0}{-9}$$
 = 21) 3(-3) =

22) 
$$\frac{64}{4}$$
 =

23) 
$$(-5)(-3)(4) = 24) -189 \div (-21)$$

Evaluate each expression if m = -32, n = 2, and p = -8. Show all your work!

25) 
$$m \div n =$$

26) 
$$p \div 4 =$$

26) 
$$p \div 4 = 27$$
)  $p^2 \div m =$ 

28) 
$$m \div p =$$

29) 
$$\frac{-p}{n} =$$

29) 
$$\frac{-p}{n} =$$
 30)  $p \div (-n^2) =$ 

31) 
$$\frac{p}{4n} =$$

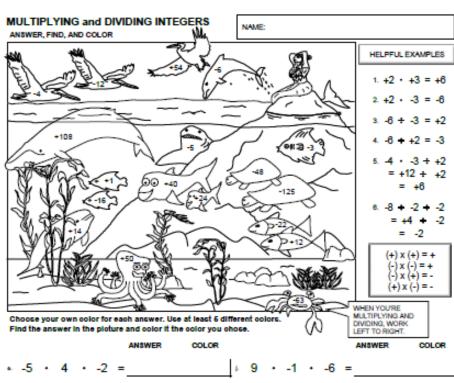
32) 
$$\frac{18-n}{-4} =$$
 33)  $\frac{m+8}{-4} =$ 

33) 
$$\frac{m+8}{-4} =$$

34) 
$$\frac{m+n}{6} =$$

35) 
$$mnp =$$

36) 
$$m \div n =$$



	ANSWER COLOR							ANSWER	COLOR
· -5 · 4 · -2 =		ı,	9	•	-1	•	-6	=	

# **\$olving One-\$tep Equation\$ x/÷**

Solving a one-step equation with integers requires you to create zero pairs to isolate the variable.

## **Examples:**

- #1 Solve: -2x = 12
- Check: -2x = 12
- ÷-2 ÷-2
- -2(-6) = -12

x = -6

-12 = -12 ✓

- #2
- Solve:  $\frac{x}{-5} = -7$  Check:  $\frac{x}{-5} = -7$ 
  - $(-5) \frac{x}{-5} = -7 \ (-5)$   $\frac{-35}{-5} = -7$

- x = 35
- --7 = -7 ✓

## You Try!

Solve each equation. Don't forget to check your answer.

Solve	Check
1) $\frac{x}{5} = -2$	
2) -40 = -5 <i>p</i>	
3) $-2 = \frac{m}{16}$	
4) -11k = 22	
5) $\frac{a}{29} = 5$	
6) -22a = -418	

# **Mixed Operation Practice**

Add, Subtract, Multiply or Divide.

1)4-19=

 $2) -1820 \div (-20) =$ 

3)-44+(-95)=

4)38-54=

5)82 • 86 =

6) -3675 ÷ (-75) =

7)-14-2=

8)46-60=

9)82 • 65 =

10) 56 • (-41) =

11) 13 • 62 =

12) 57 • (-7) =

13)  $-1860 \div (-31) =$ 

14) 74 - (-78) =

15) 80 + 63 =

16) 43 • (-79) =

17) 31 + (-60) =

18) -6 + 64 =

19) 17 + 89 =

20) 5 - 8 =

21) 7161 ÷ (-77) =

22) 38 + 53 =

23) -56 • (-55) =

 $24) - 1260 \div (-30) =$ 

25) -18 - 98 =

26) 71 • 77 =

27) 1610 ÷ 46 =

28) 56 + (-20) =

29) 47 + (-88) =

 $30) -168 \div 2 =$ 

# CRYPTIC QUIZ

## 1. What Did the Sardine Say When a Submarine Went By?

-56 36 36 -33 -35 -12 -12 7 -35 -12 -96 -35 130 36 31 39 9 36 39 -56 9

## 2. What Happened to the Grocer Who Stacked All the Liquid Detergents on a High Shelf?

7 9 -6 -35 5 25 -24 -15 39 -8 130 28 31 36 100 25 36 -69

## TO DECODE THE ANSWERS TO THESE QUESTIONS:

Solve any equation below and find the solution in the code. Each time it appears, write the letter of the exercise above it. Keep working and you will decode the two answers.

① 
$$n + 12 = 4$$

$$\triangle 4x = 36$$

$$\frac{\mathbf{v}}{3} = -11$$

$$\mathbf{W}^{-7}t = 42$$

$$\Re \frac{-1}{5} y = -20$$

$$\mathbf{\hat{T}}$$
 -32 =  $\mathbf{x}$  + (-20)

$$\mathbf{0}^{-48} = 2q$$

N 13 = 
$$\frac{n}{10}$$

$$\mathbf{\hat{Y}}^{-}$$
50 = 19 +  $\mathbf{p}$ 

$$\$$$
  $-15r = -75$ 

① 
$$14 = \frac{-u}{4}$$

$$\mathbf{H}$$
 42 = 6**d**

$$\bigcirc \frac{1}{8} y = -12$$

$$\mathbf{M}^{-4} = 11 + \mathbf{m}$$

$$\mathbf{A}^{-}\mathbf{x} = 35$$

$$\bigcirc -3 = \frac{-a}{13}$$

$$\bigcirc$$
 -18 + z = 18

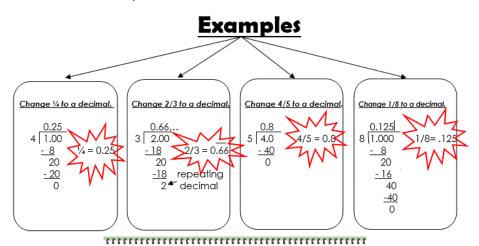
$$3 - 125 = -5k$$

# **SHOW WORK HERE:**

# **Converting Fractions to Decimals**

To convert from a fraction to a decimal, you \_\_\_\_\_ the

\_\_\_\_\_ by the \_\_\_\_\_.



$$\frac{\frac{3}{4} \rightarrow 3 \div 4}{4)3 \stackrel{?}{00}} = 0.75$$

$$\frac{\frac{3}{4} = 0.75}{20}$$

$$\frac{-28 \downarrow}{20}$$

$$-20$$

## You Try:

1) 
$$\frac{2}{5} =$$
\_\_\_\_\_

2) 
$$\frac{2}{8} =$$
\_\_\_\_\_

1) 
$$\frac{2}{5} =$$
 \_\_\_\_\_ 2)  $\frac{2}{8} =$  \_\_\_\_ 3)  $\frac{13}{20} =$  \_\_\_\_

4) 
$$1\frac{1}{2} =$$
\_\_\_\_\_

5) 
$$\frac{5}{7} =$$

4) 
$$1\frac{1}{2} =$$
 \_\_\_\_\_ 6)  $\frac{1}{9} =$  \_\_\_\_\_

# **Converting Decimals to Fractions**

If you can \_\_\_\_\_ it as a decimal, you can \_\_\_\_ it as

a fraction. Say the decimal using the correct place value, write

as a fraction and simplify.

## **Examples:**

n. Change 1.04 to a fraction.	Change 2.001 to a
	fraction.
Say "one and four	
hundredths."	Say "two and one
	thousandth."
$1 \frac{4}{-} \div \frac{4}{-} = 1 \frac{1}{-}$	
100 ÷ 4 25	$2\frac{1}{4000}$
	1000
	,

## You Try:

# Fractions, Decimals & Percents

# **EXAMPLE** Changing a Percent to a Fraction

Express 35% as a fraction.

• Change the percent directly to a fraction with a denominator of 100. The number of the percent becomes the numerator of the fraction.

$$35\% = \frac{35}{100}$$

• Simplify, if possible.

$$\frac{35}{100} = \frac{7}{20}$$

35% expressed as a fraction is  $\frac{7}{20}$ .

# **EXAMPLE** Changing Decimals to Percents

Express 0.7 as a percent.

$$0.7 \times 100 = 70$$

• Multiply the decimal by 100.

• Add the percent sign.

So, 0.7 expressed as a percent is 70%.

# **EXAMPLE** Changing Percents to Decimals

Change 4% to a decimal.

• Express the percent as a fraction with 100 as the denominator.

$$4\% = \frac{4}{100}$$

• Change the fraction to a decimal by dividing the numerator by the denominator.

$$4 \div 100 = 0.04$$

So, 
$$4\% = 0.04$$
.

# **Converting Practice**

Percent	Decimal	Fraction
32%	0.32	$\frac{32}{100}   \frac{\div}{\div}  \frac{4}{4} = \frac{8}{25}$
	0.81	
40%		
		$\frac{4}{5}$
52%		
	1.25	
		1 9/11
		12 16
144%		
	0.06	