Unit 5 IXL Log

Unit 5

Area & Volume

Area
Composite Area
Surface Area
Volume

Name: ______
Math Teacher:

	Required Skills			
		Your Score		
	CC.1	Identify and classify polygons		
f 1/27	FF.2	Area of rectangles and squares		
Week of 1/27	FF.3	Area of triangles (to 70)		
_	FF.5	Area of quadrilaterals		
2/3	FF.6	Area of compound figures		
Week of 2/3	FF.7	Area between two rectangles		
	FF.24	Area of compound figures with triangles		
Week of 2/10	EE.1	Identify polyhedra		
	EE.2	Which figure is being described?		
/eek o	EE.3	Nets of 3-dimensional figures		
>	FF.16	Surface area of cubes and rectangular prisms		
Week of 2/17	K.10	Multiply 3 or more fractions and whole numbers		
	K.13	Multiply mixed numbers		
Wee	FF.14	Volume of cubes and rectangular prisms		

Pg.1a pg.1b

Unit 5: Area & Volume Standards, Checklist and Concept Map

Georgia Standards of Excellence (GSE):

MGSE6.G.1: Find area of right triangles, other triangles, special quadrilaterals, and polygons by composing into rectangles or decomposing into triangles and other shapes; apply these techniques in the context of solving real-world and mathematical problems

 Find the area of a polygon (regular or irregular) by dividing it into squares, rectangles, and/or triangles and find the sum of the areas of those shapes

<u>MGSE6.G.2</u>: Find the volume of a right rectangular prism with fractional edge lengths by packing it with unit cubes of the appropriate unit fraction edge lengths, and show that the volume is the same as would be found by multiplying the edge lengths of the prism. Apply the formulas V = lwh and V = lwh to find volumes of right rectangular prisms with fractional edge lengths in the context of solving real-world and mathematical problems.

MGSE6.G.4: Represent three-dimensional figures using nets made up of rectangles and triangles, and use the nets to find the surface area of these figures. Apply these techniques in the context of solving real-world and mathematical problems.

What Will I Need to Learn??

I can find the area of a polygon by splitting it up into squares, rectangles, and/or triangles, and finding the sum of all of the areas
 I can find the volume of a right rectangular prism with fractional edges by packing it with unit cubes
 I can apply the formula $\mathbf{V} = \mathbf{l} \mathbf{w} \mathbf{h}$ to find the volume of a right rectangular prism with fractional edges
 I can represent 3-dimensional shapes with nets
 I can use nets to determine the surface area of 3- dimensional figures
 I can apply these concepts of area, volume, and surface area to solve real-world problems

Math 6 Unit 5 Calendar

Widdii o oiiio o odioiiddi					
1/27	1/28	1/29	1/30	1/31	
Unit 5 Pre-Test MSG Set Up Geometry Vocab Intro	Area	Area	Area	Area Quiz	
2/3	2/4	2/5	2/6	2/7	
Composite Area	Composite Area	Composite Area	Composite Area	Composite Area Quiz	
2/10	2/11	2/12	2/13	2/14	
Nets & Surface Area Lab	Computer Lab	Nets & Surface Area	Nets & Surface Area	Nets & Surface Area Quiz	
2/17	2/18	2/19	2/20	2/21	

WINTER BREAK! (3)

<u></u>				
2/24	2/25	2/26	2/27	2/28
Volume of Rectangular Prisms with Fractional Edges	Computer Lab	Volume of Rectangular Prisms with Fractional Edges	Surface Area vs. Volume	Volume Quiz
3/2	3/3	3/4	3/5	3/6
Review	Review	Unit 5 Mini Post-Test	Unit 5 Test	Unit 5 Test

Pg.2a pg. 2b

Unit 5 - Vocabulary

Term	Definition and/or Picture/Example
Area	
Base (of a triangle)	
Base (of a 3D figure)	
Congruent	
Cubic Units	
Edge	
Equilateral Triangle	

Term	Definition and/or Picture/Example
Face	
Isosceles Triangle	
Lateral Faces	
Net	
Parallel	
Parallelogram	
Perpendicular	

Pg.3a pg.3b

Term	Definition and/or Picture/Example
Polygon	
Regular Polygon	
Irregular Polygon	
Polyhedron	
Prism	
Pyramid	
Quadrilateral	
Rectangle	

Term	Definition and/or Picture/Example
Rectangular Prism	
Right Triangle	
Scalene Triangle	
Square	
Surface Area	
Trapezoid	
Vertex (vertices)	
Volume	

Pg.4a pg.4b

Math 6 - Unit 5: Area & Volume Review

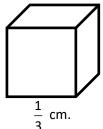
Knowledge & Understanding

1) How could you determine the area of a composite figure, such as the ones shown here?

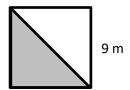
- 2) What types of units are used to describe area?
- 3) What types of units are used to describe volume? _____

Proficiency of Skills

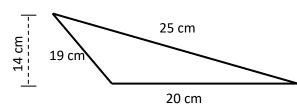
4) Determine the volume of the cube: _____



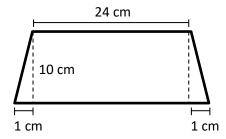
5) Find the area of the shaded section of the square: _____



6) Find the area of the triangle:

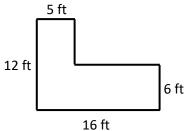


7) Determine the area of the trapezoid:



8) The surface area of a cube can be found by using the formula $SA = 6s^2$. Determine the surface area of a cube with a length of 8cm.

9) Find the area of the figure shown below: _____



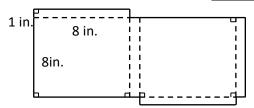
Application

- 10) If carpet costs \$4 per square yard, how much would it cost to carpet a rectangular room that is 6 yards wide and 10 yards long?
- 11) What is the area of the trapezoid?

12) A rectangular prism is filled with small cubes of the same size. The bottom layer consists of 9 cubes, each with a volume of 2 cubic inches. If there are 3 layers of cubes in the prism, what is the volume of the rectangular prism?



13) A box is made of cardboard with no overlap. The net of the box is shown below. How many square inches of cardboard is needed to make the box?



14) The triangular sides of the tent are equilateral, with a base of 20 inches and a height of 15 inches. The three rectangular sides of the tent are each 50 inches long and 20 inches wide. What is the surface area of the tent?

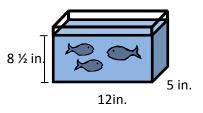


15) Mariah and Max are making a plaque to dedicate to the swaggerific saxophone players of the ECMS sixth-grade band. The center is a 10-inch square, and the edges of the frame measure 12 inches long and 12 inches wide. What is the area of the frame?

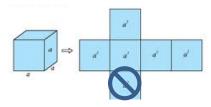


12 ft

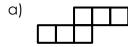
16) A fish tank is shown below. What is the volume of the water in the tank?

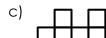


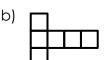
- 17) How many cubic feet are in a cubic yard?
- 18) The volume of a rectangular prism can be found by using the formula V=Bh. If the base of a prism is square with a side length of 3 inches and the height of the prism is 2 ½ inches, find the volume of the prism.
- 19) Andres is painting five faces of a storage cube (he isn't painting the bottom face). If each faces is 8 inches, how many square inches will he need to paint?

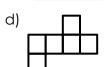


20) Which of the following nets could NOT be folded to form a cube?



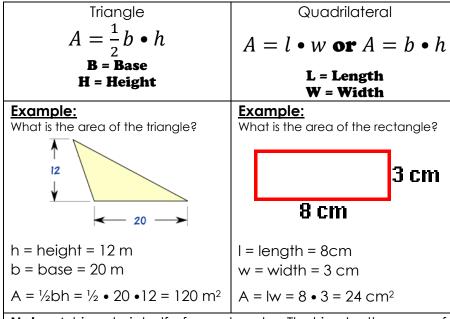






Area of Triangles and Quadrilaterals

Area is the amount of space INSIDE a figure. It is always measured in square units.



Note: A triangle is half of a rectangle. That is why the area of a triangle is half the area of a rectangle.

You Try:

Triangle	Square	Rectangle
h = 6ft b = 5ft	side = 8in	1 = 9cm w = 3cm
Formula:	Formula:	Formula:

How do you calcı	Formulas for Area	
Area is the	of	Square:
units need	ed to fill a	
	Or, the amount	Rectangle:
ofi	n a polygon.	
To calculate area, you	Triangle:	
all the		
Area is always measure		

You Try:

1) When calculating area, you can count the square units in a polygon. How many square units are there?	2) What is the area of this shape?	3) What is the area of this shape?
4) You can also use the formulas above to calculate the area of shapes. 3 mm 6 mm	5) What is the area of this shape? 5 in 5 in	6) What is the area of this shape?

Area of Squares, Rectangles, Parallelograms, Triangles, and Trapezoids

<u>Shape</u>	<u>Formula</u>	<u>Example</u>	WHY/HOW does this work?
Square		1 cm 1 cm A = s ² A = 4 ² A = 16	
Rectangle		1 2 3 4 5 A = 5(2) 10 9 8 7 6 A = 10	
Parallelogram		The base is 6 units, and the height is 8 units. $A = bh$ $A = 6 \cdot 8$ $A = 48$	
Triangle		$A = \frac{1}{2}bh$ $A = \frac{1}{2}(6)(4)$ $A = \frac{1}{2}(24)$ $A = 12$	
Trapezoid		$A = h(\frac{b_1 + b_2}{2})$ $A = 3(\frac{2+6}{2})$ $A = 3(4)$ $A = 12$	

Area of Parallelograms

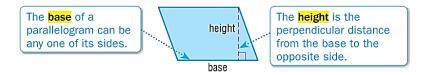
Area of a Parallelogram

Words

The area A of a parallelogram is the product of its base b and its height h.

Model

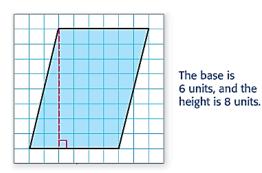
Symbols A = bh



Parallelograms include special quadrilaterals, such as rectangles, squares, and rhombi.

Examples:

Find the area of the parallelogram.



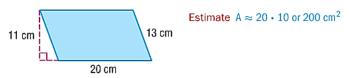
A = bh Area of parallelogram

 $A = 6 \cdot 8$ Replace b with 6 and h with 8.

A = 48 Multiply.

The area is 48 square units or 48 units².

Find the area of the parallelogram.



A = bh Area of parallelogram

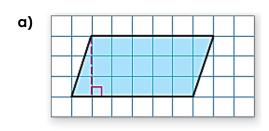
 $A = 20 \cdot 11$ Replace b with 20 and h with 11.

A = 220 Check for Reasonableness 220 ≈ 200 ✓

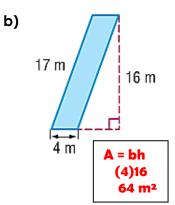
The area is 220 square centimeters or 220 cm².

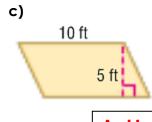


YOU TRY! Remember to write the formula, substitute, and solve!

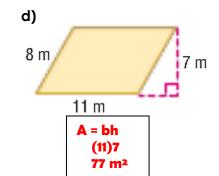


A = bh (6)3 18 u²





A = bh (10)5 50 ft²



Area of Triangles

Area of a Triangle

Words The area A of a triangle is one

half the product of the base b

and its height $\it h$.

Symbols
$$A = \frac{1}{2}bh \text{ or } A = \frac{bh}{2}$$

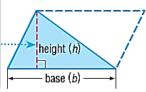
Model



Congruent figures are figures that are the same shape and size.

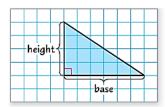
A parallelogram can be formed by two congruent triangles. Since congruent triangles have the same area, the area of a triangle is one half the area of the parallelogram.

The base of a triangle can be any one of its sides. The height is the perpendicular distance from that base to the opposite vertex.



Examples:

Find the area of the triangle.



By counting, you find that the measure of the base is 6 units and the height is 4 units.

$$A = \frac{1}{2}bh$$
 Area of a triangle

$$A = \frac{1}{2}(6)(4)$$
 Replace b with 6 and h with 4.

$$A = \frac{1}{2}(24)$$
 Multiply.

$$A = 12$$
 Multiply.

The area of the triangle is 12 square units.

Find the area of the triangle.

$$A = \frac{1}{2}bh$$
 Area of a triangle Area of a triangle Replace b with 12.1 and h with 6.4.

12.1 m

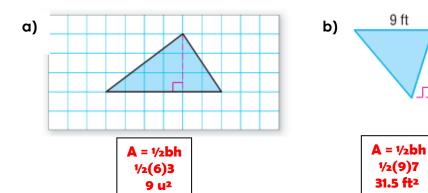
$$A = \frac{1}{2}(77.44)$$
 Multiply.

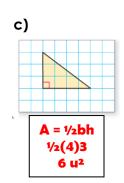
$$A = 38.72$$
 Divide. $\frac{1}{2}(77.44) = 77.44 \div 2$, or 38.72

The area of the triangle is 38.72 square meters.

FORMULA: $A = \frac{1}{2}bh$

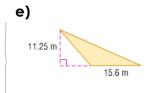
YOU TRY! Remember to write the formula, substitute, and solve!



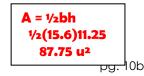








7 ft

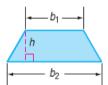


Area of Trapezoids

Area of a Trapezoid

Words

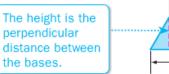
The area A of a trapezoid is one half the product of the height h and the sum of the bases b_1 and b_2 .

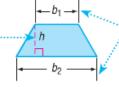


Symbols

$$A = \frac{1}{2}h(b_1 + b_2)$$

A trapezoid has two bases, b_1 and b_2 . The height of a trapezoid is the distance between the bases.





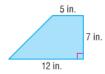
The two bases are parallel. They will always be the same distance apart.

Model

When finding the area of a trapezoid, it is important to follow the order of operations. In the formula, the bases are to be added before multiplying by $\frac{1}{2}$ of the height h.

You Try:

Find the area of the trapezoid.



The bases are 5 inches and 12 inches.

The height is 7 inches.

$$A = \frac{1}{2}h(b_1 + b_2)$$
 Area of a trapezoid

$$A = \frac{1}{2}$$
(7)(5 + 12) Replace *h* with 7, *b*₁ with 5, and *b*₂ with 12.

$$A = \frac{1}{2}(7)(17)$$
 Add 5 and 12.

$$A = 59.5$$
 Multiply.

The area of the trapezoid is 59.5 square inches.

Find the area of the trapezoid.

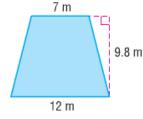
$$A = \frac{1}{2}h(b_1 + b_2)$$

Area of a trapezoid

$$A = \frac{1}{2}(9.8)(7 + 12)$$

Replace h with 9.8,

$$b_1$$
 with 7, and b_2 with 12.



$$A = \frac{1}{2}(9.8)(19)$$

Add 7 and 12.

$$A = 93.1$$

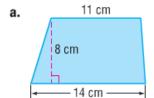
Multiply.

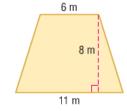
So, the area of the trapezoid is 93.1 square meters.

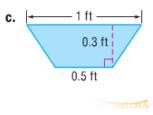
b.

FORMULA:

YOU TRY! Remember to write the formula, substitute, and solve!







Practice with Area

Name of Polygon				
Picture	22 cm	10 in 9 in 12 in	9 4 5	6 7 4 8
Write the formula				
Substitute for the variables (Show work)				
Solve. Include square units in your answer.				

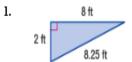
Skills Practice

Find the area of each polygon. Show all steps!

\$tep 1: Write your formula.

\$tep 2: Substitute for the base(s) and height.

\$tep 3: Solve. Include units in your answer!



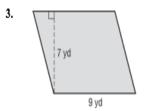


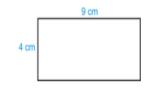
2.

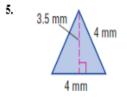
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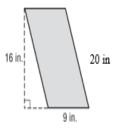
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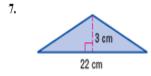
8.

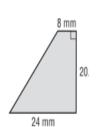










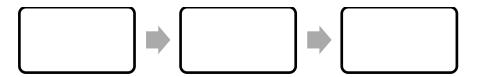


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Area Error Analysis



Fill in the Flow Map with the 3 steps to solving problems on area:



Silly Sally has struck again! Analyze her work in Column #1, and <u>circle her mistake</u>. In Column #2, explain what she did wrong. In Column #3, work out the problems correctly, showing ALL work!

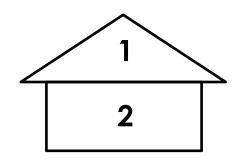
Silly Sally's Work (Circle her mistake):	What did Silly Sally do wrong?	Show Silly Sally how it's done! (Show ALL steps!)
A = IW 12 • 8 20 m ²		
$A = \frac{1}{2} b h$ $\frac{1}{2} \cdot 4 \cdot 6$ $24 cm^{2}$		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		

Area of Composite Figures

A composite figure is a figure made of two or more two-dimensional figures. The composite figure shown to the right is made of two rectangles.



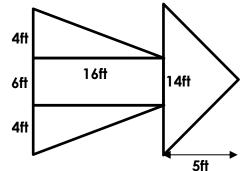
The figure below is a composite figure. How would you find its area?



The house is made up of two shapes that you are familiar with – a triangle and a rectangle. You can "decompose" or "take apart" the figure to find the area of each piece and then find the sum of those areas to get the total area.

Try This:

Find the area of the rocket figure below.

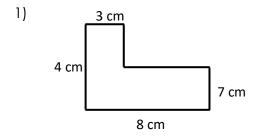


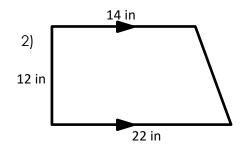
1) Find the area of each polygon that makes up the shape. Write the areas inside each polygon.

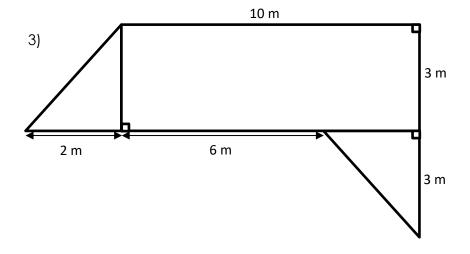
2) What is the TOTAL area of the shape? _____

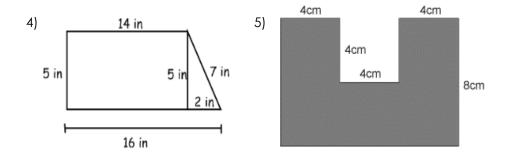
Area of Composite Figures Practice

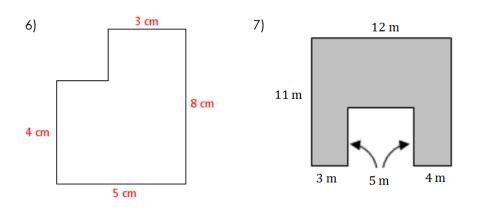
Find the area of each composite figure. Remember to show all work! (Hint: Often, you will have to draw in lines to decompose the figure. Pay careful attention to the side lengths that are given so you can figure out the side lengths that are missing!)



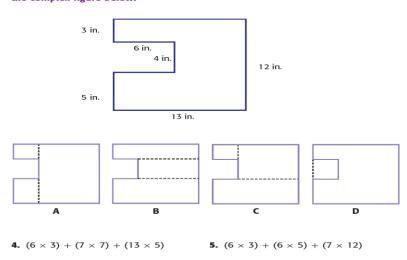






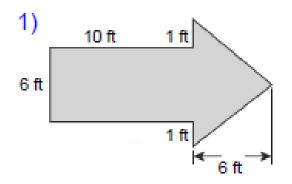


Match each math sentence with the correct division of the complex figure below.

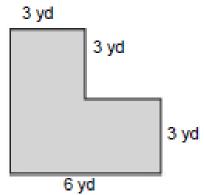


7.
$$(13 \times 3) + (7 \times 4) + (13 \times 5)$$

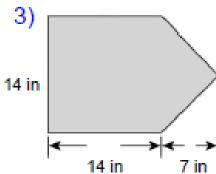
Composite Area Practice



2)



3)

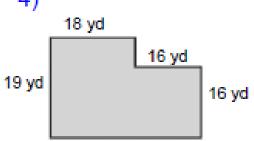


Area: _____

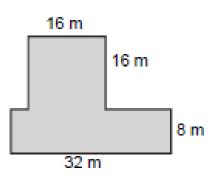
Area: _____

Area: _____

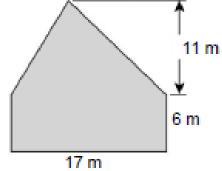
4)



5)



6)



Area: _____

Area: _____

Area: _____

Nets

PRISM A net is a flat shape that can be folded into a 3D solid. **CUB**≡

Nets of 3-Dimensional Figures

<u>Face</u> is a flat	of a solid figure) .
Edge is a r	segment where two	o faces of a
Vertex is a	where	or more
edges of a solid figure	meet or the pointed end of	a cone opposite of

FIGURE	FACES Look	BASE	How many	NET
	Like		faces?	
Cube				
Rectangular				
Prism				
Triangular				
Prism				
Square				
Pyramid				
Triangular				
Pyramid ^				
Cylinder				
Cone				

Surface Area Notes

So... what exactly IS surface area, anyway?

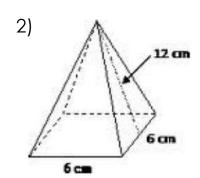
To calculate the surface area of a 3D figure...

Surface Area Practice

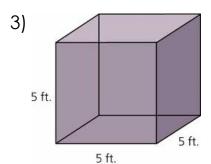
1) 2 cm 6 cm

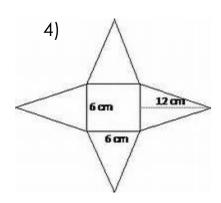
3 cm

3 cm



Examples of surface area:







Draw a cube **and** its net. Label its dimensions 4 inches. Then, determine the surface area.



Draw a square pyramid **and** its net. Label the dimensions of the base as 4 inches, and the height of the triangular faces 3 inches. Then, determine the surface area.



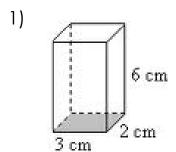
Draw a rectangular prism **and** its net. Label its dimensions 4 inches, 2 inches, and 5 inches. Then, determine the surface area.

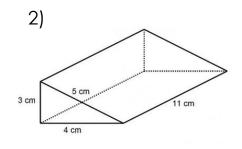


Draw a triangular pyramid **and** its net. Label the dimensions of the base as 4 inches, and the height of the triangular faces 3 inches. Then, determine the surface area.

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Surface Area Practice





7) E 00 cm

8) Find the Surface Area of a cube with side length 4cm.

Surface Area in the Real World

Solve each of the problems by drawing a net and finding the surface area.

1) A pizza box is 15 inches wide, 14 inches long, and 2 inches tall. How many square inches of cardboard were used to create the

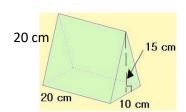


2) Angelo is making a replica of an Egyptian pyramid. He is making a square pyramid with a base that is 3 feet long and 3 feet wide. The triangular sides of the pyramid each have a height of 14 feet. How much material will Angelo need to cover the pyramid?



3) Sydney is painting a rectangular toy box for her little brother. She will paint all 4 sides and the top (she will NOT paint the bottom). If the toy box is 20 inches tall, 12 inches wide, and 25 inches long, how many square inches will she need to paint?

4) DeAndre is making a tent for his hamster. It is 20 cm long, and the triangular bases are 15 cm high and 10 cm wide (see picture below). How much material will he need to make the tent?



Volume of Rectangular Prisms

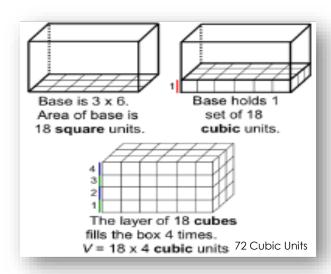
Volume is the amount of space inside a 3D object, measured in cubic units.



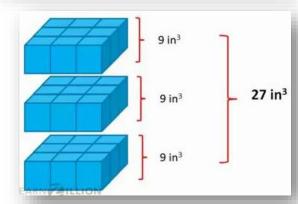
Ever wonder WHY volume is measured in *cubic units*??

Since volume measures the amount of space INSIDE a figure, it's like you're packing the figure with little tiny cubes!!

Here's a visual of a <u>rectangular</u> <u>prism</u> being packed with unit cubes...



Here's a visual of a <u>cube</u> being packed with unit cubes...



Volume is the _____ of ___ units needed to fill the space in a three dimensional (3D) figure.

Volume is always measured in cubic units.

We calculate volume you must find the area of the ______.

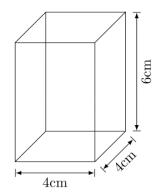
then multiply it by the ______.

This can be written as ______.

OR • for a rectangular prism.

Example:

Find the volume of the rectangular prism below.



$$V = B \bullet h$$

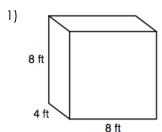
$$V = I \bullet W \bullet h$$

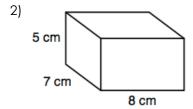
$$V = 4 \cdot 4 \cdot 6$$

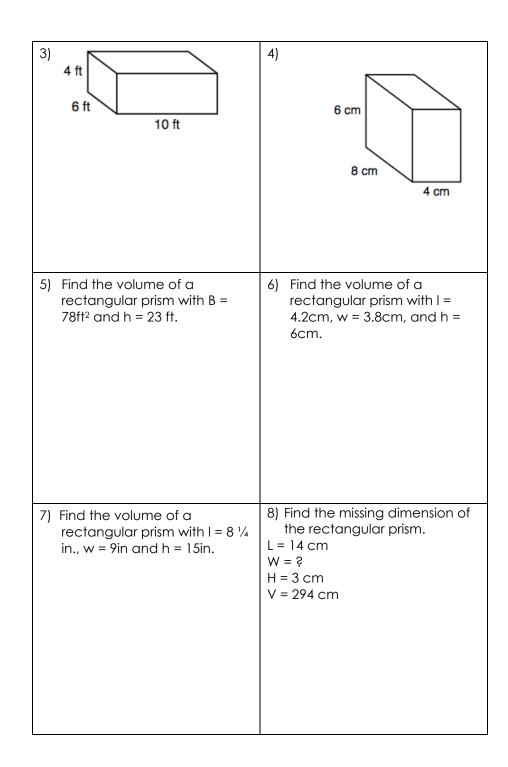
$$V = 96 \text{ cm}^3$$

You Try:

Find the volume.







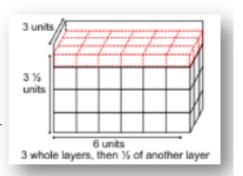
Volume of Rectangular Prisms with Fractional Edges

Let's calculate the volume of a rectangular prism with a length of 6 units, a width of 3 units, and a height of 3 ½ units.

Look at the picture! →

The bottom layer contains 6 units across and 3 units back, for a total of 18 units.

Then, there are 3 ½ layers of 18 units. (You have 3 layers, and then half of another layer.)



So, the total volume of this figure is 18 + 18 + 18 + 9 = 63 cubic units.

Let's calculate the amount of water that Nora can pour into her fish tank that is 10 inches long, 6 inches wide, and 5 ¼ inches deep.

The bottom of the tank is 10 inches long and 6 inches wide, so the bottom layer is 60 cubic inches.

Then, there are 5 ¼ layers of 60 units. The volume of the tank is...



You Try:

Find the volume of a rectangular prism with a length of 3cm, a width of 2 $\frac{1}{2}$ cm, and a height of 4 cm.

Volume Error Analysis



Sally is a silly little girl that makes silly mistakes! Analyze her work in Column #1, and <u>circle her mistake</u>. In Column #2, explain what she did wrong. In Column #3, show how Silly Sally should work out the problem. Show ALL work!

Silly Sally's Work (Circle her mistake):	What did Silly Sally do wrong?	Show Silly Sally how it's done! (Show ALL steps!)
$V = I w h$ $V = 4 \cdot 4 \cdot 4$ $V = 12 \text{ m}^3$		
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		
$V = I w h$ $V = \frac{2}{3} \cdot \frac{2}{3} \cdot \frac{2}{3}$ $V = \frac{6}{9} = \frac{2}{3} in^{3}$ $V = \frac{6}{9} = \frac{2}{3} in^{3}$		
$V = I w h$ $8 \frac{1}{4} yd V = 8 \frac{1}{4} \cdot 2 \frac{1}{2} \cdot 3$ $V = 16 \frac{1}{8} \cdot 3$ $2 \frac{1}{4} yd V = 48 \frac{1}{8} yd^{3}$		
$V = 1 \text{ w h}$ $4^{\frac{1}{2}\text{yd}} V = 4^{\frac{1}{2}} \cdot 1^{\frac{1}{2}} \cdot 2$ $V = \frac{8}{2} \cdot \frac{3}{2} \cdot 2$ $V = \frac{14}{2} \cdot 2$ $V = 12 \text{ yd}^{3}$		

More Volume Practice

Determine the Volume of each rectangular prism or cube below. Include units and show your work!

1. A cube that is 1 1/8 yards wide

2. The box with dimensions of 6 ft • 4 ft • 1 ½ ft

3. Determine the Volume of a rectangular truck bed that is 12 feet long, $5 \frac{1}{4}$ feet wide, and $3 \frac{1}{5}$ feet deep.

4. How much water can be poured into a cubic tank that is 2 ½ feet long?

5. What is the volume of a gift box that is 3 ½ inches wide, 2 inches tall, and 6 inches long?

SURFACE AREA AND YOUME PRACTICE

3 ½ m	2 in 5 in 5	3 blocks high 4 blocks deep wide	Son Stone	Rectangular Prism:
7) SA =	= VS (5	= A2 (E	1) SA =	Surface Area (thing help to draw a net)
8) V =	= A (9	4) V =	2) V =	Volume (Show work and circle your answer.) V=lwh OR V=Bh

Circle the choices that relate to volume. Underline the choices that relate to surface area.

Wrapping a present

The amount of cereal in a box

Painting a doghouse

Filling a pool with water

 Name 2 ways surface area and volume are different. 10) How are surface area and volume alike?

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